

Electromechanical devices MM2EMD

Lecture 8 - Analog-to-digital and digital-to-analog converters.

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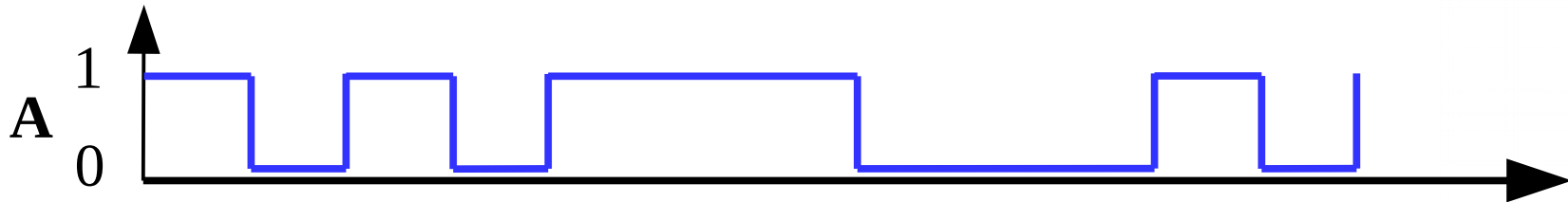
- **No recap of last lecture :)**
- Recap of digital signals
- Converting between digital and analog
 - Digital to analog converters
 - Analog to digital converters
 - Flash converters for high speed video
- Summary



Outline of the lecture

- No recap of last lecture :)
- **Recap of digital signals**
- Converting between digital and analog
 - Digital to analog converters
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- In lectures 1-3 I taught you about digital electronic.
- In digital electronics signals can either be **on** (1) or **off** (0) and all information is transmitted and stored using binary numbers.



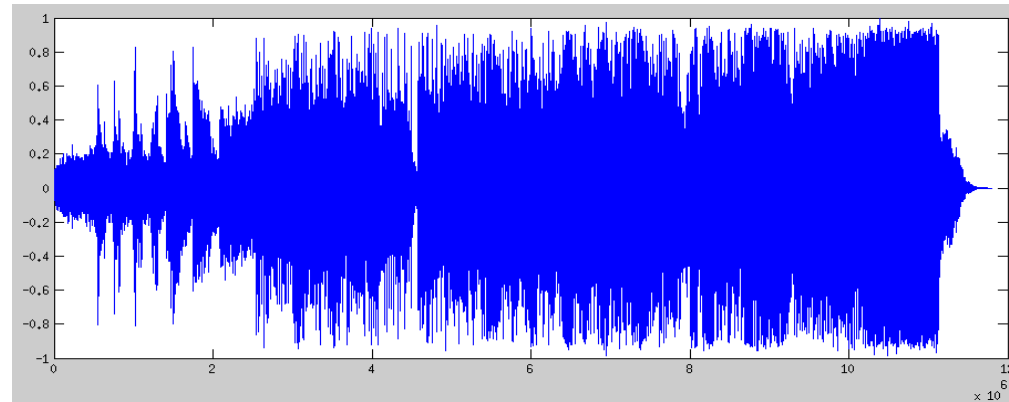
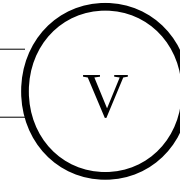
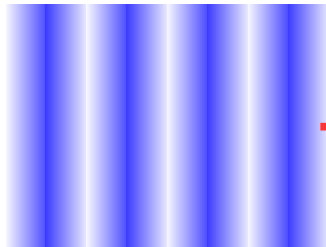
- In L4 we learnt that the **real world** is not binary.....



Analog signals recap



- Your guitar produces compression waves in the air that a microphone can pick up.

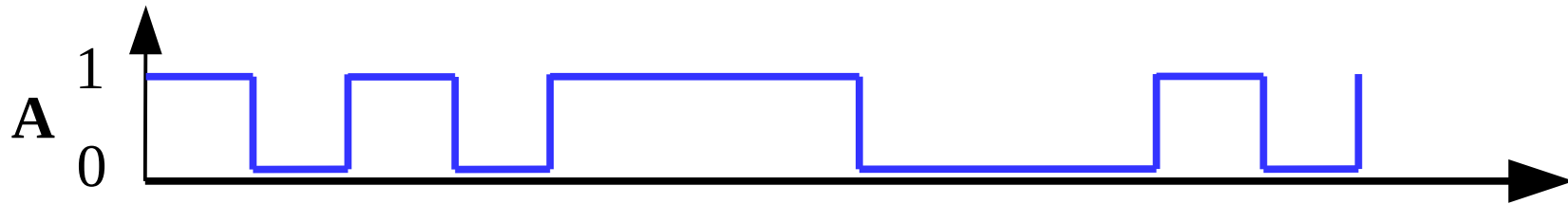


- These signals can have any value and are called **analog signals**.

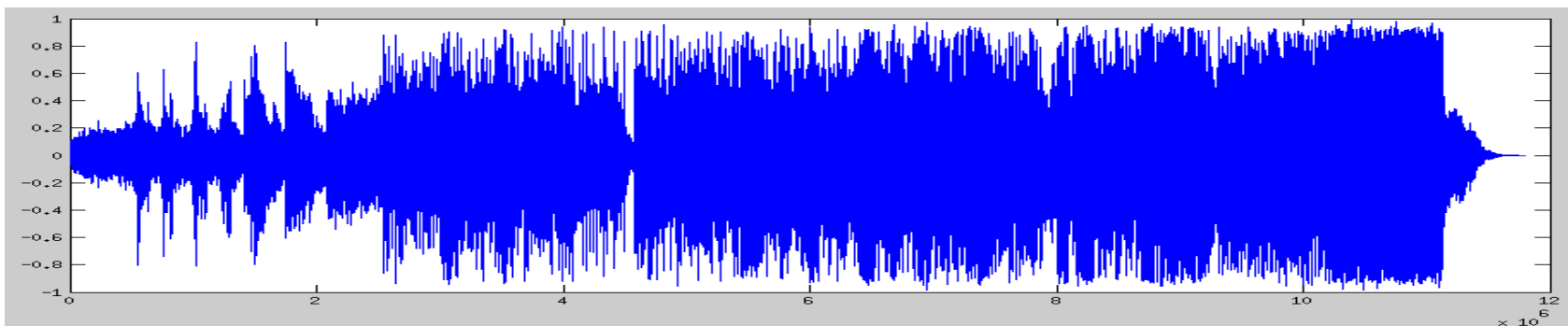
Digital v.s. analog signals



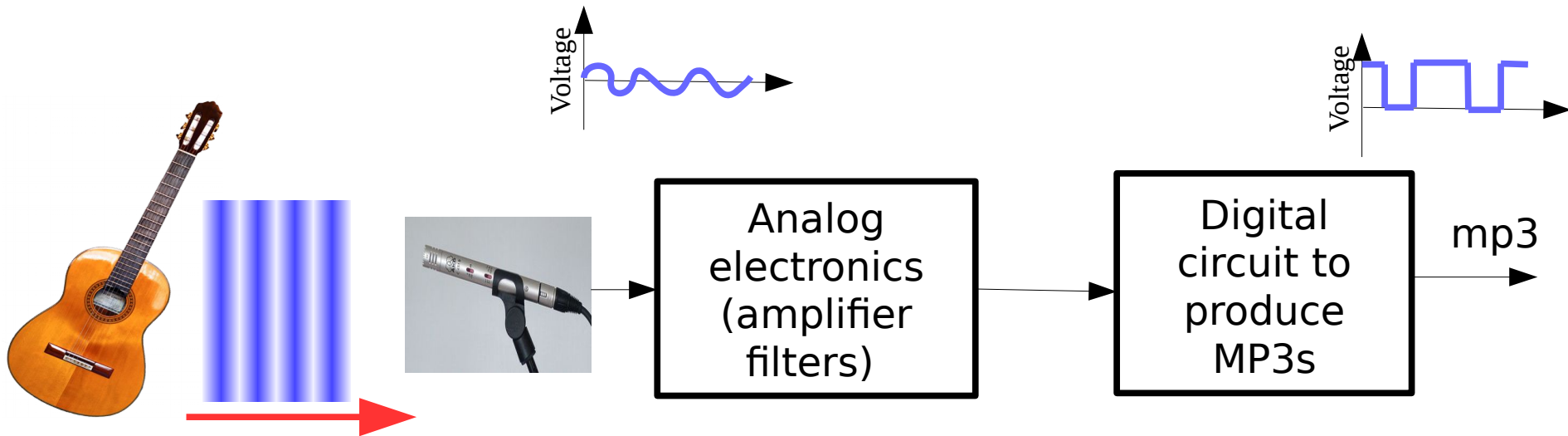
- A digital signal



- An analog signal

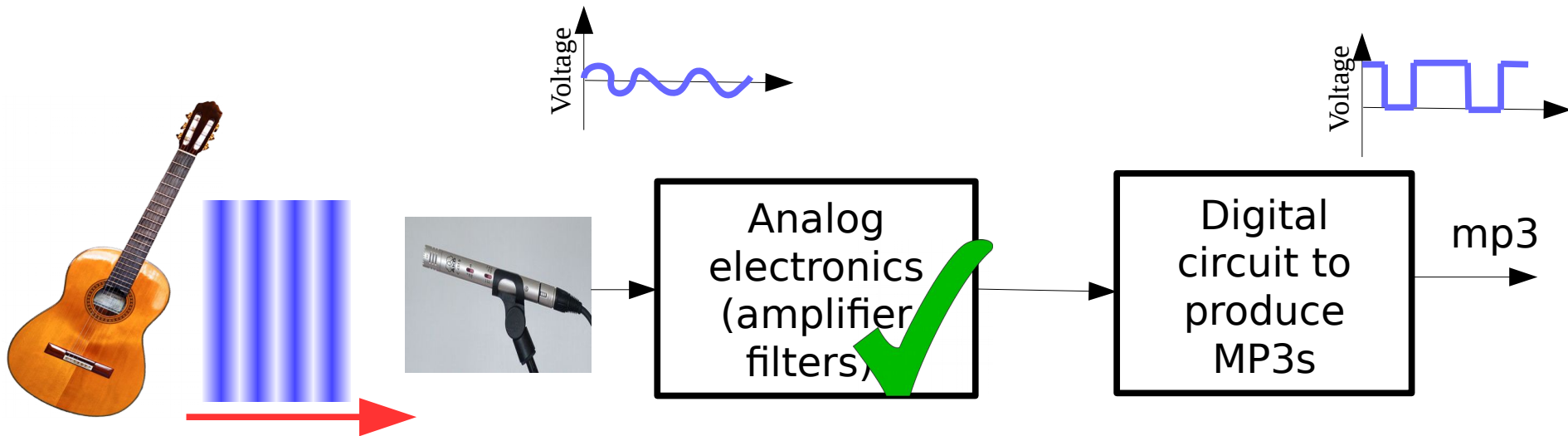


The MP3 recorder example



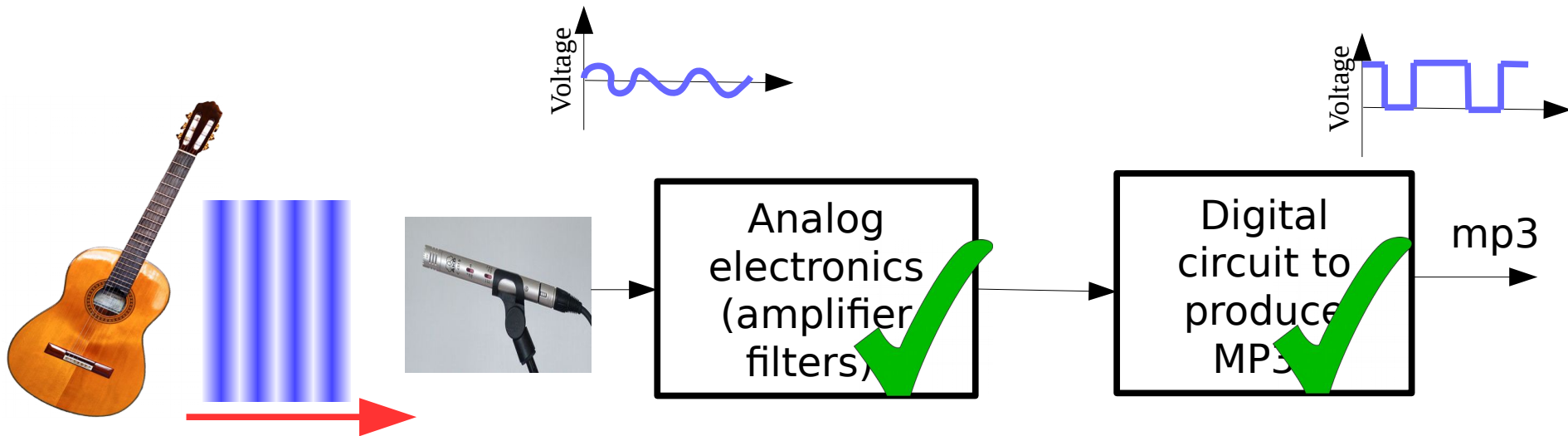
- An MP3 recorder as an example of a modern analog and digital electronics system.

The MP3 recorder example



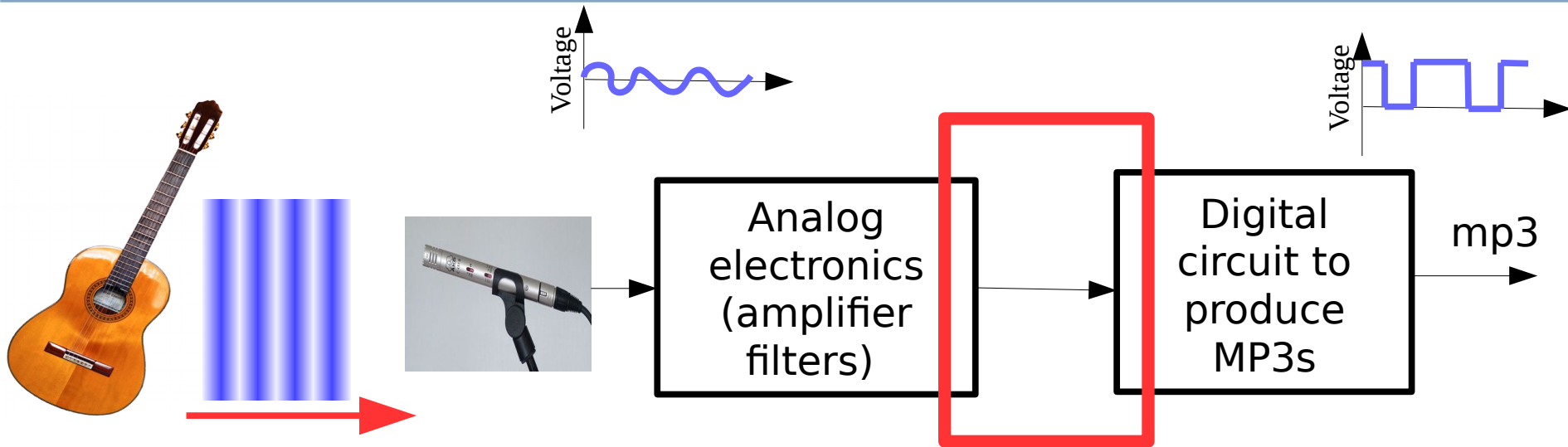
- You now know all about digital electronics (well quite a lot anyway)

The MP3 recorder example



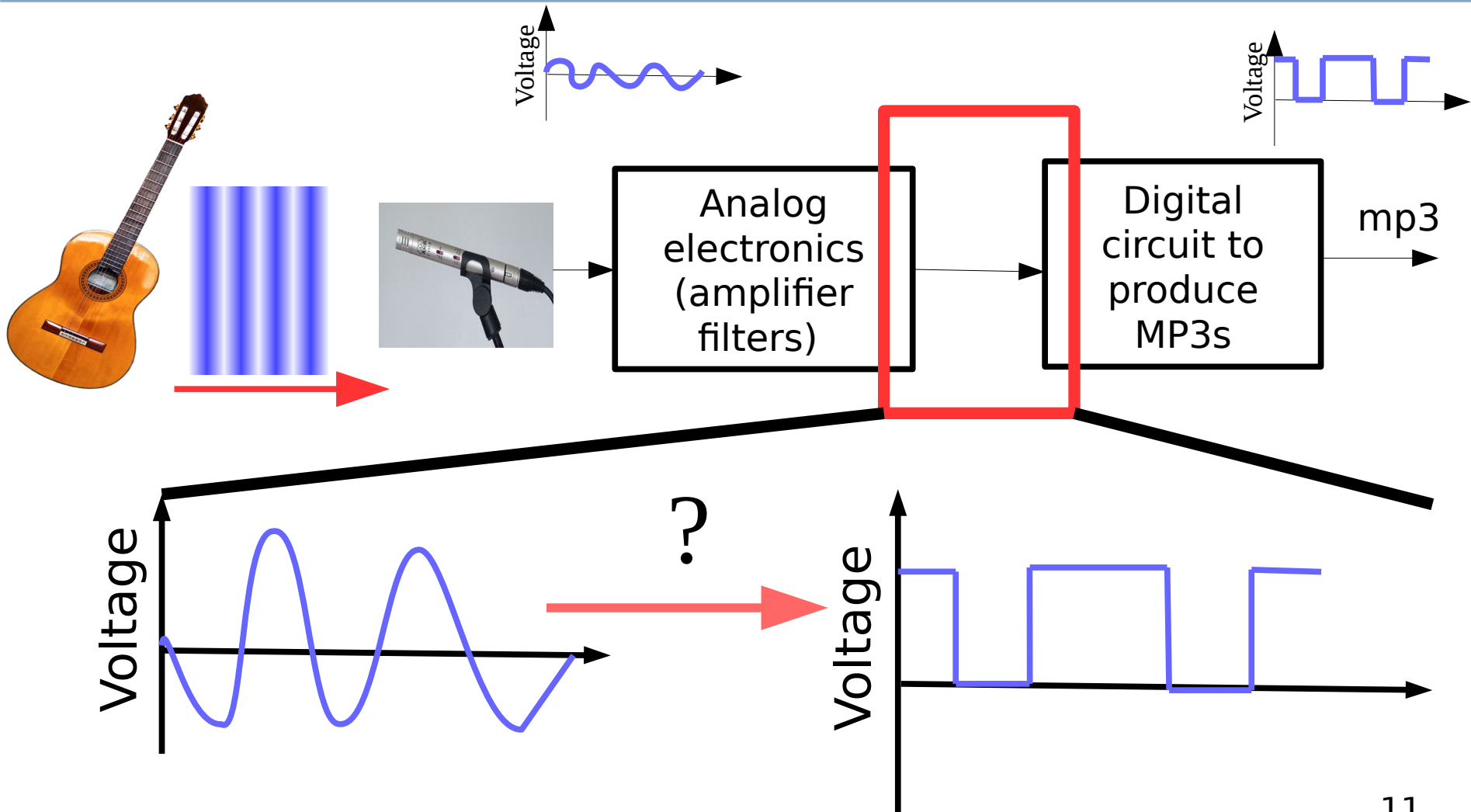
- You now know all about digital electronics
- You also know all about analog electronics. (well quite a lot anyway)

The analog/digital divide

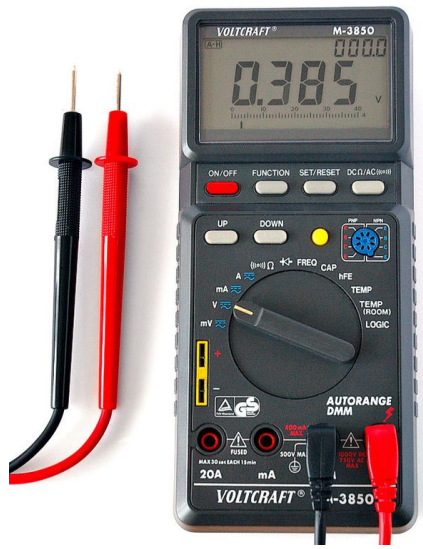
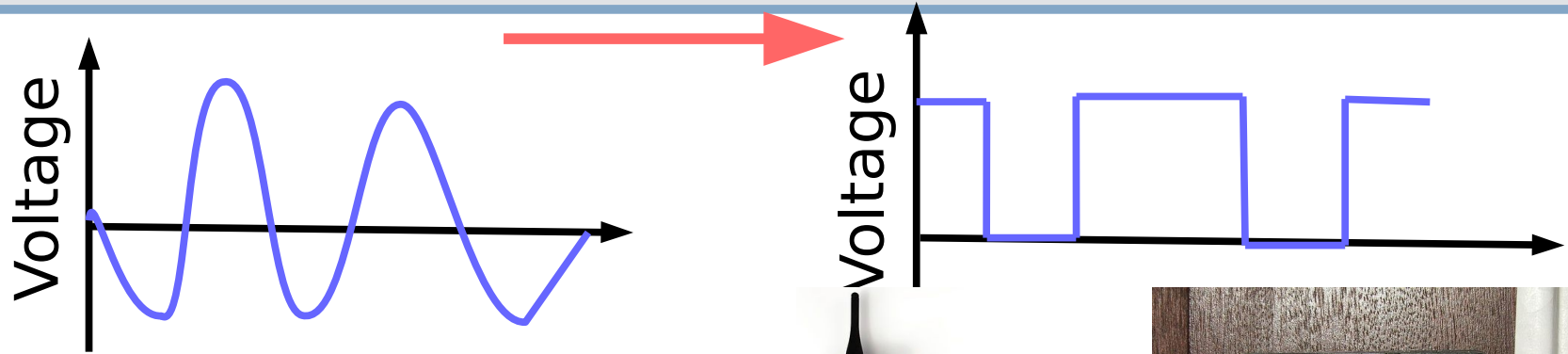


- But what you don't know yet is how to convert analog signals in to binary or digital codes.

Converting analog signals into binary signals.



Analog to digital converter



Andre Karwath



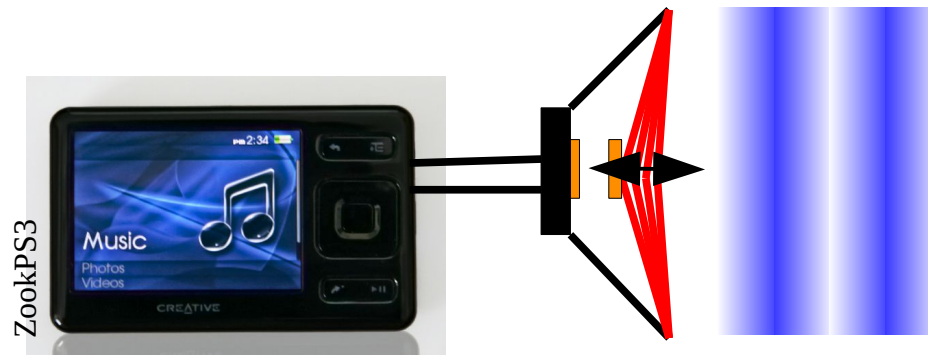
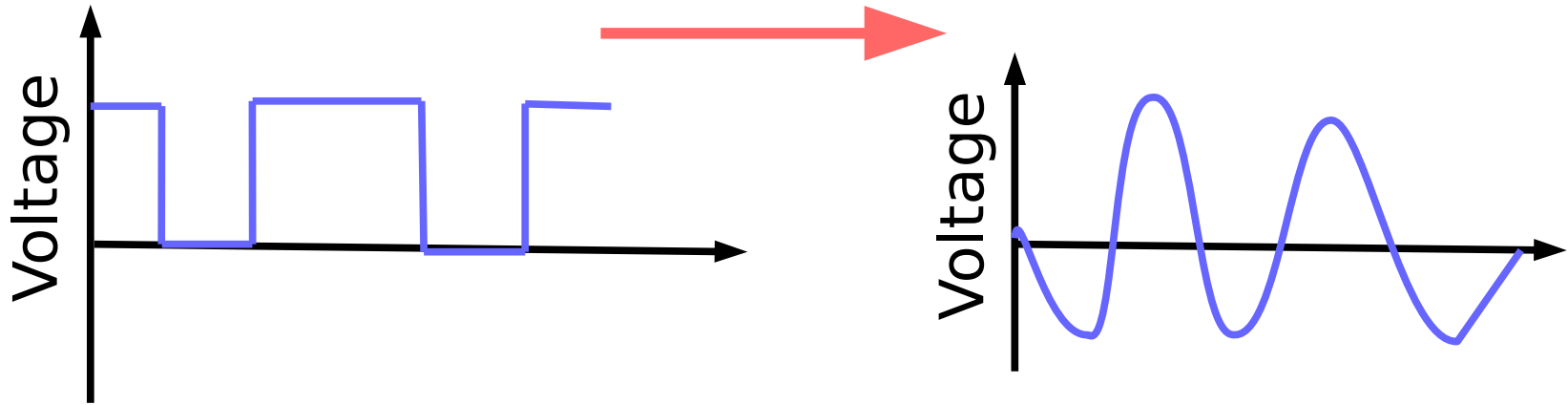
• Every time you want a computer to interact with the real world you will need an analog to digital converter.



Outline of the lecture

- No recap of last lecture :)
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Digital to analog converter



- Before we look at something complex like music, let's look at just converting on number.

10000 \longrightarrow 0.5 V

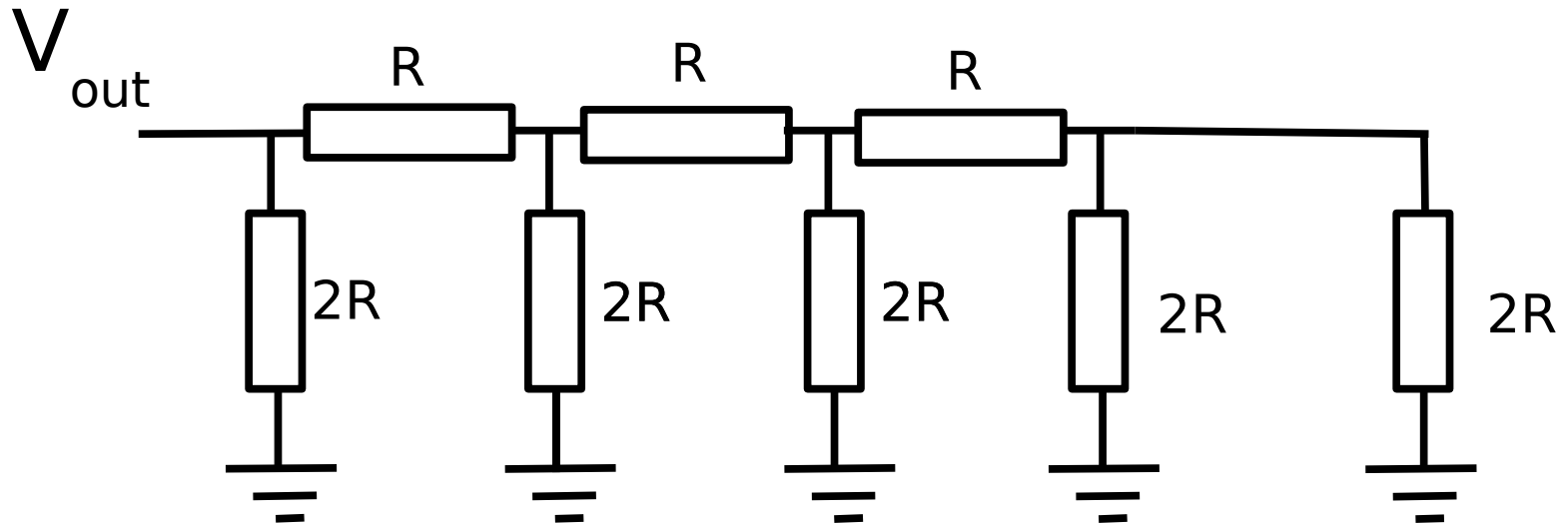
01000 \longrightarrow 0.25 V

- And this is the circuit we use to do this convert one binary number to a analog number....

The R2R ladder



- This is THE circuit used to convert all digital signals to analog signals.

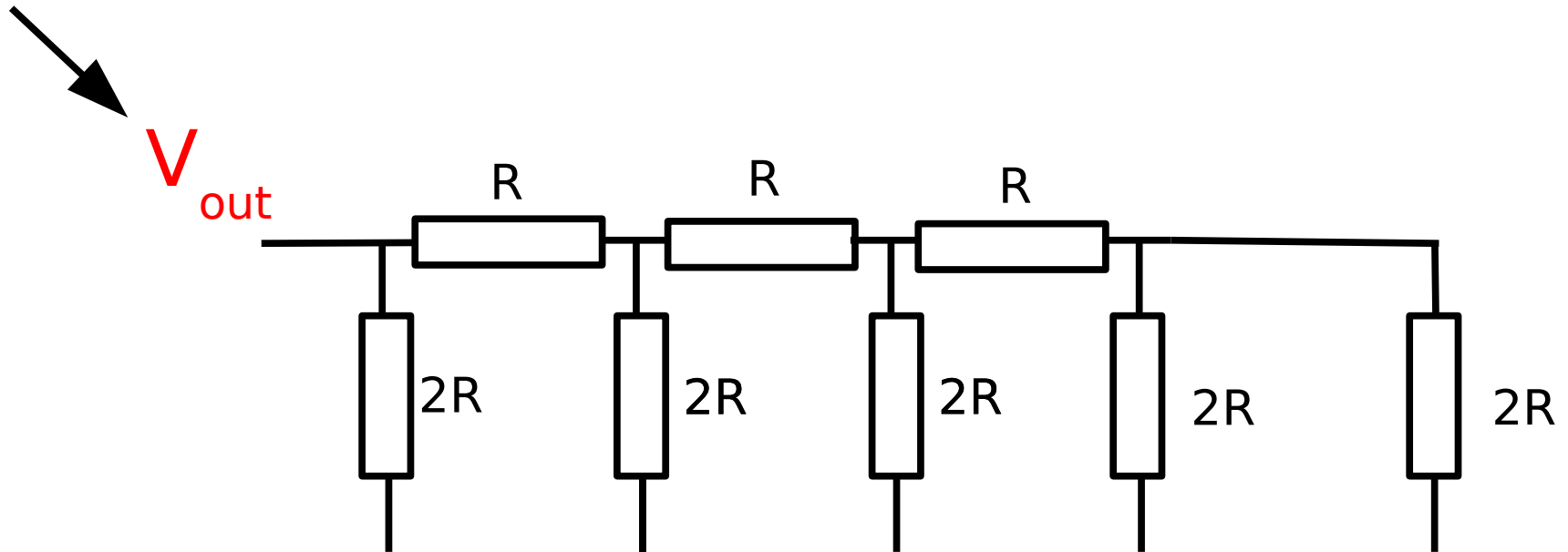


- It is also very elegant

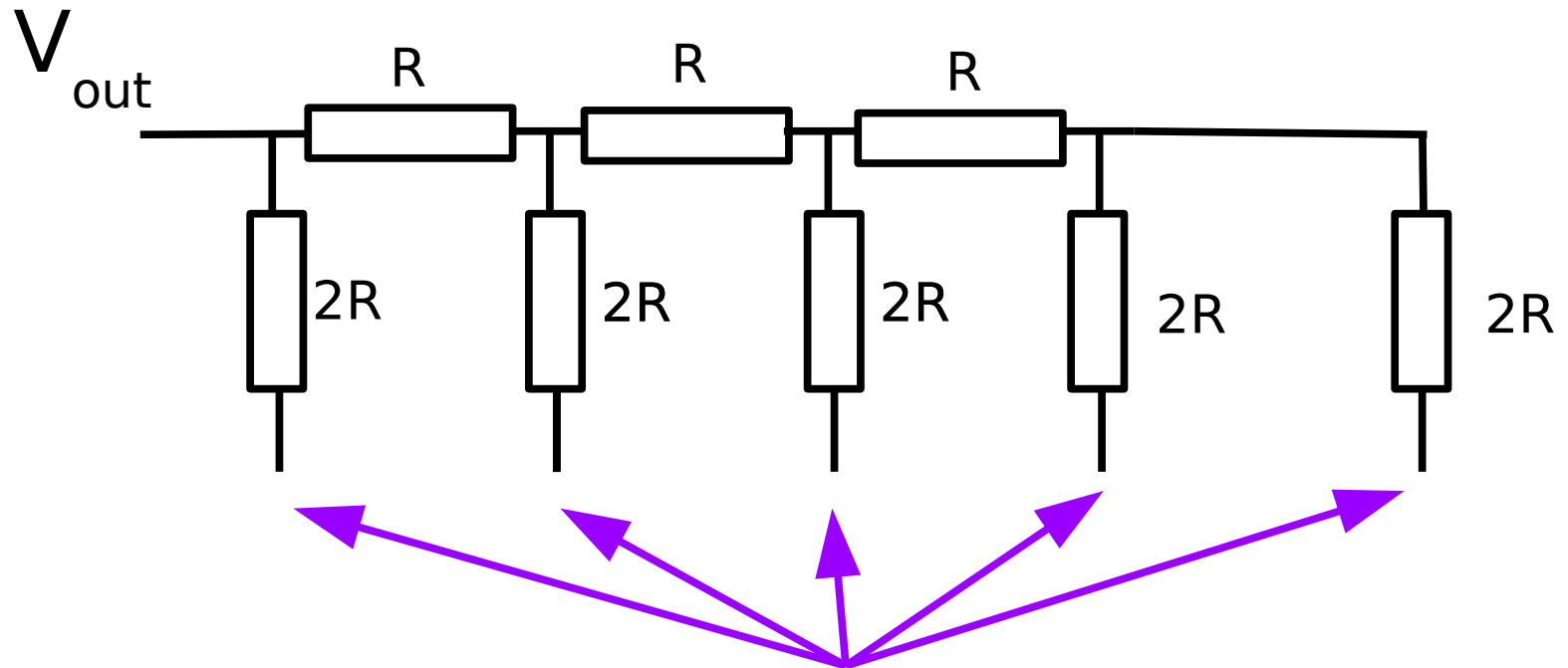
The R2R ladder



- This is the analog output of the circuit.

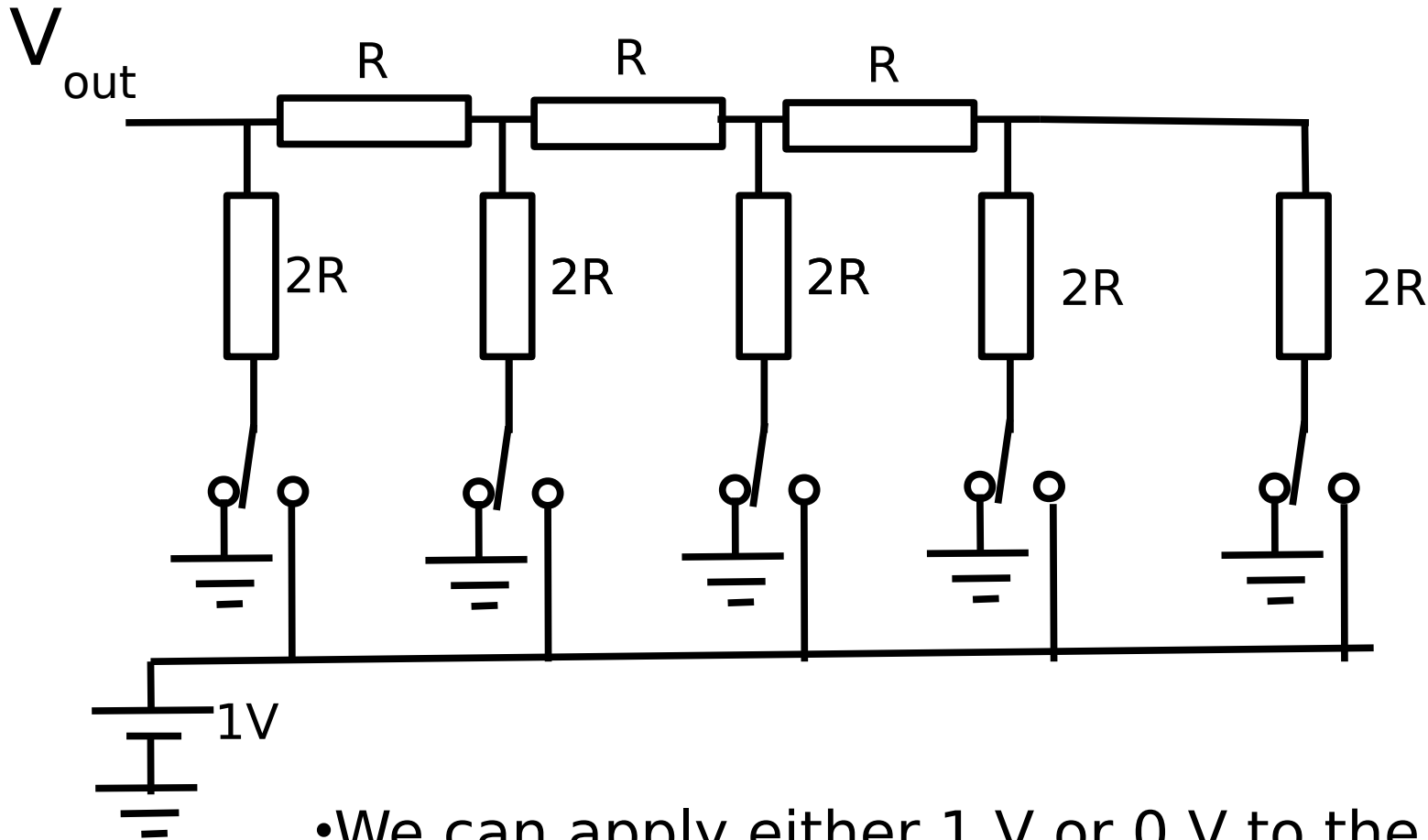


The R2R ladder



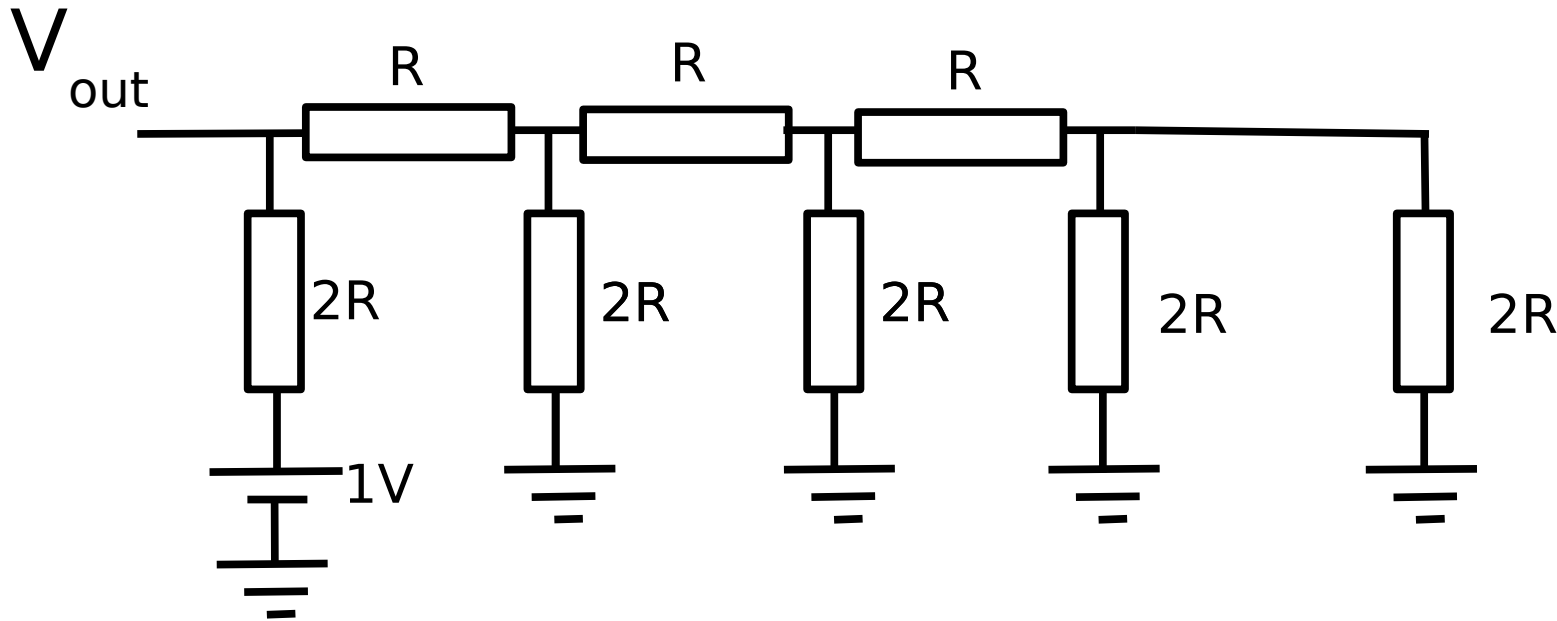
These are the digital inputs to the circuit.

The R2R ladder



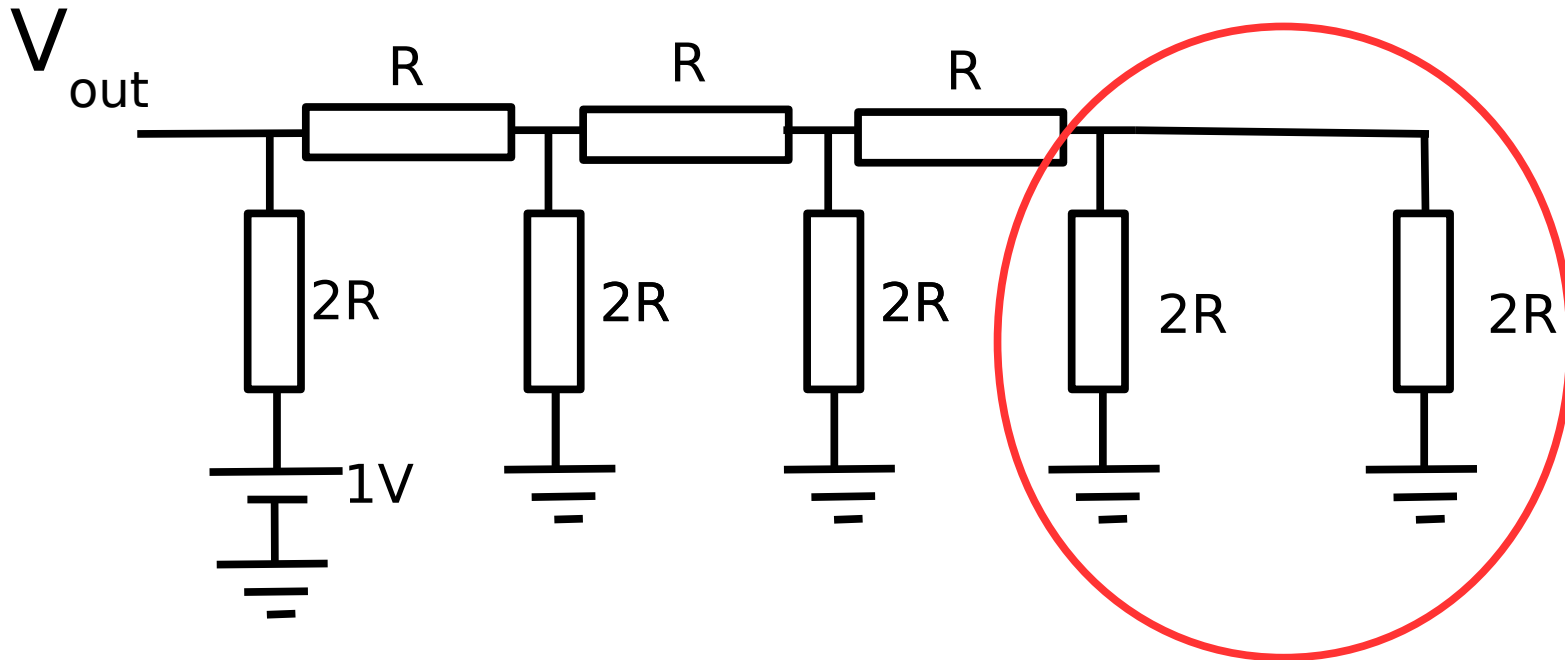
- We can apply either $1V$ or $0V$ to the inputs.
- This would represent 00000

Let's look at pin 1



- Let's apply 1V to the first input and see what output we get at V_{out} .
- This would represent the binary number 10000
- To do this we need to analyze the circuit.

Analyze the last two resistors

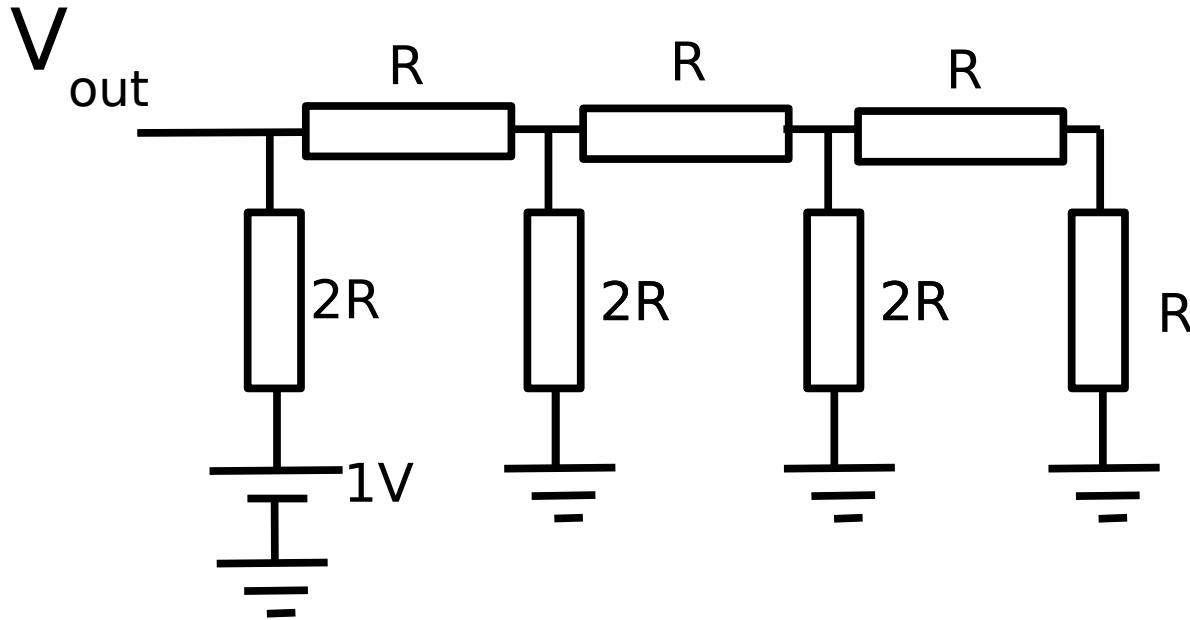


- They are in parallel
SO...

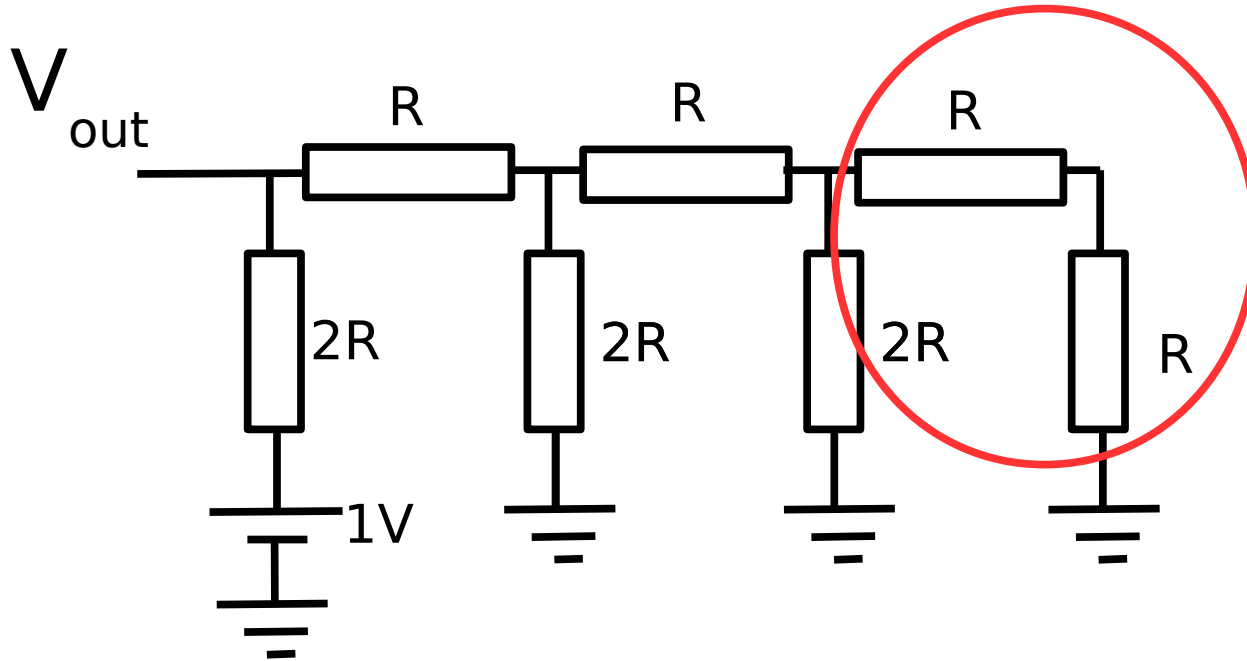
$$\frac{1}{R_{new}} = \frac{1}{2R} + \frac{1}{2R}$$

$$R_{new} = R$$

We can represent them using one resistor with value R

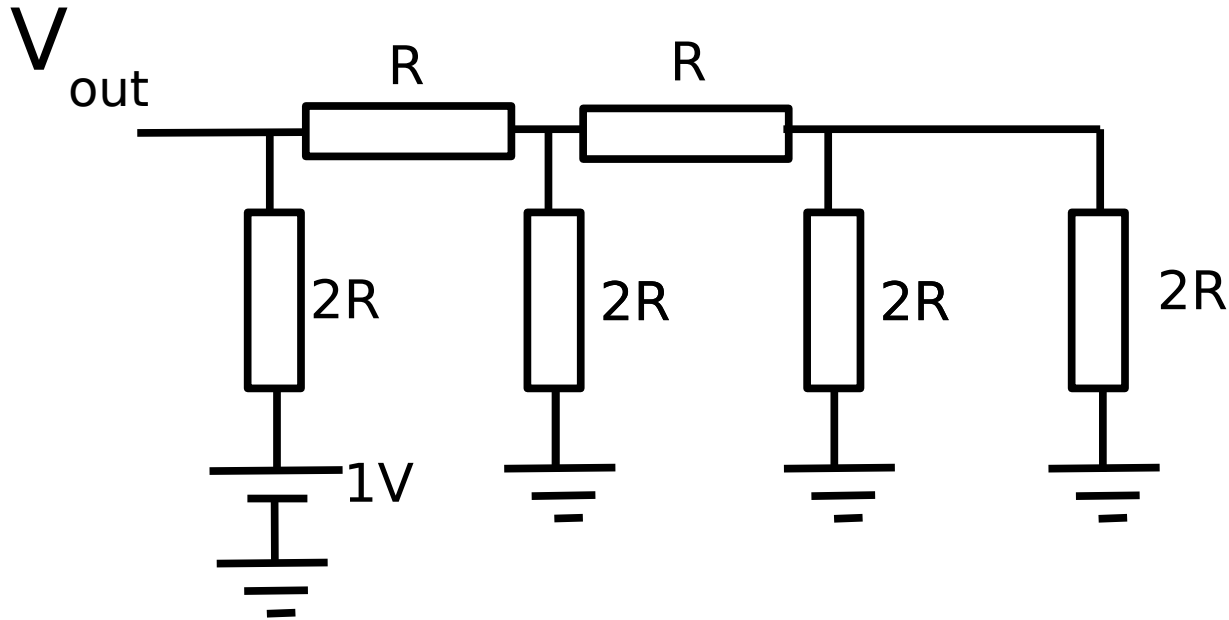


Now look at these two resistors on the end.

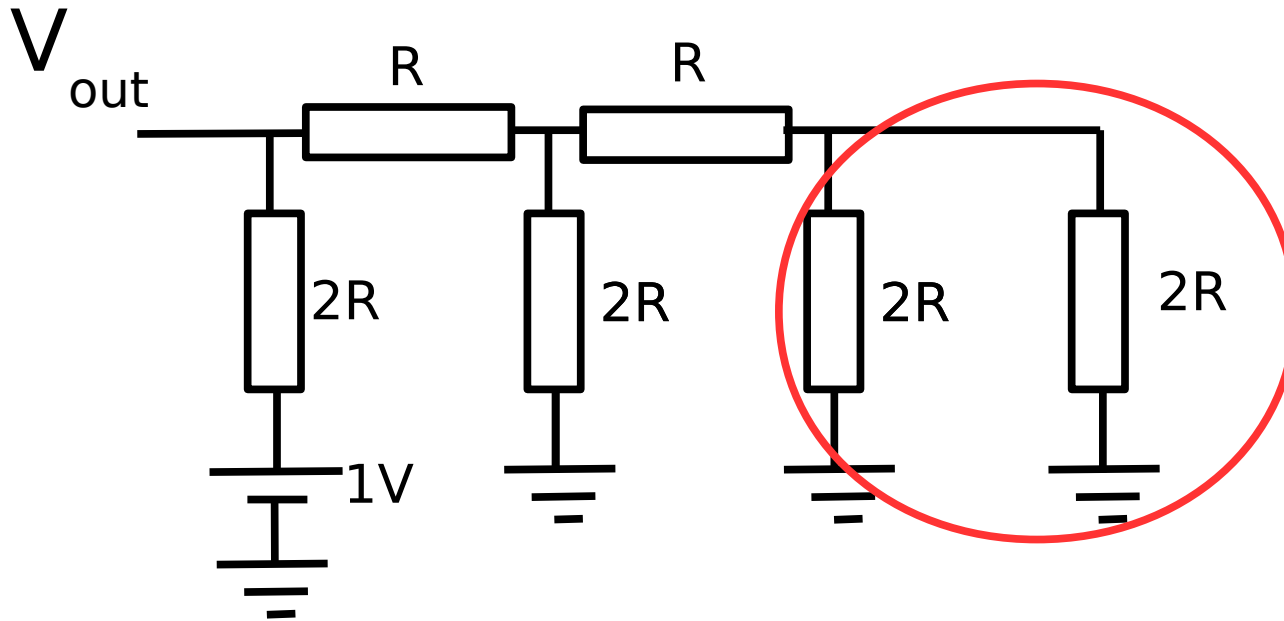


- We can turn them into one resistor with value $2R$

Giving...



Another two parallel resistors...

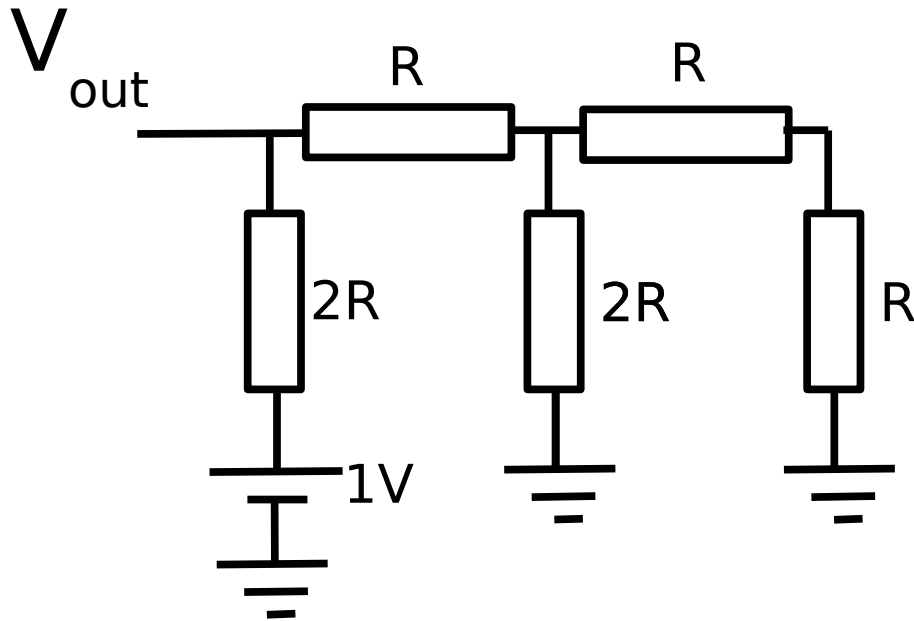


• Now let's turn these two parallel resistors into one resistor.

$$\frac{1}{R_{new}} = \frac{1}{2R} + \frac{1}{2R}$$

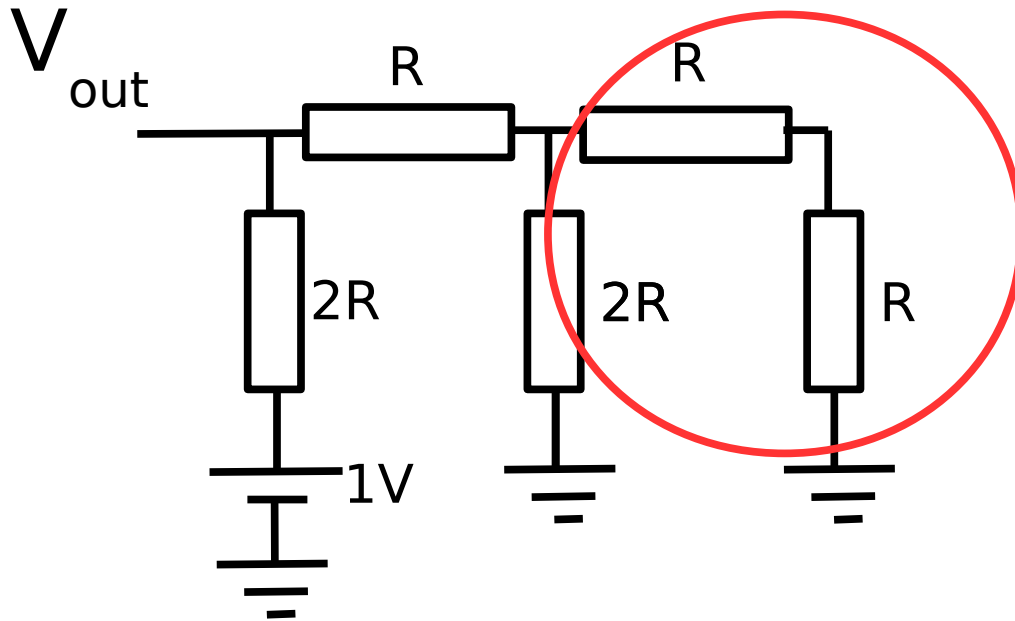
$$R_{new} = R$$

Gives...



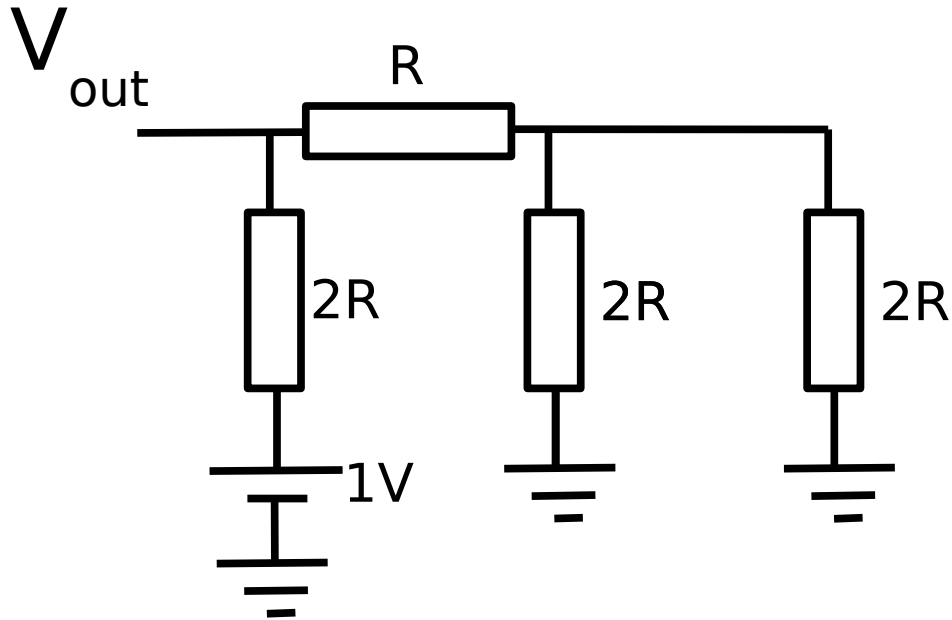
- Which can be converted into one resistor....

Two resistors in series..

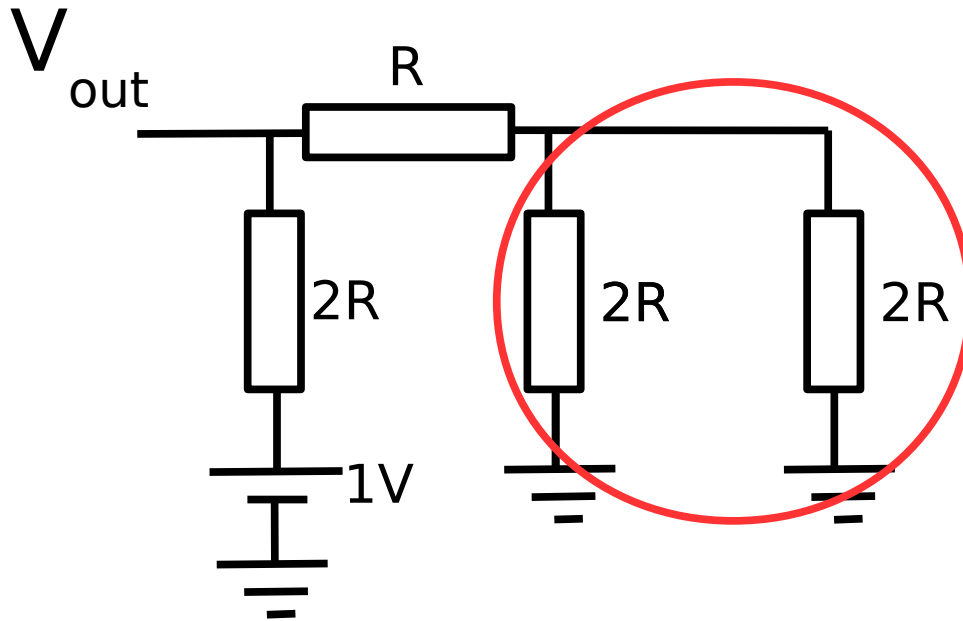


- Which can be converted into one resistor....

What voltage will we get if we put



Another two resistors in parallel

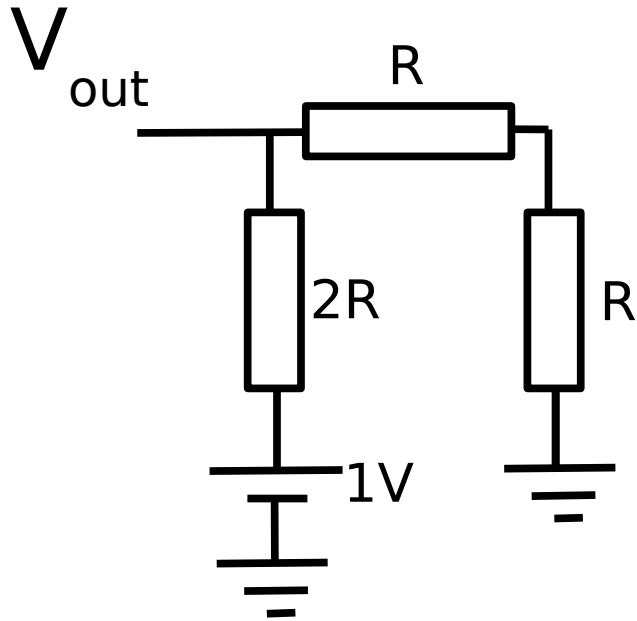


- Which again gives one resistor with a value of R .

$$\frac{1}{R_{\text{new}}} = \frac{1}{2R} + \frac{1}{2R}$$

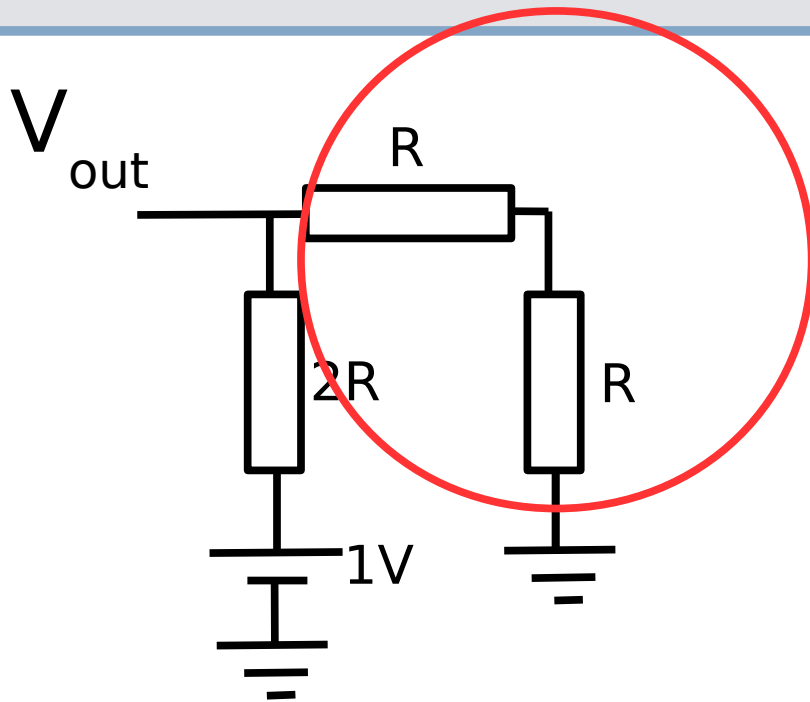
$$R_{\text{new}} = R$$

Leaving us with.....



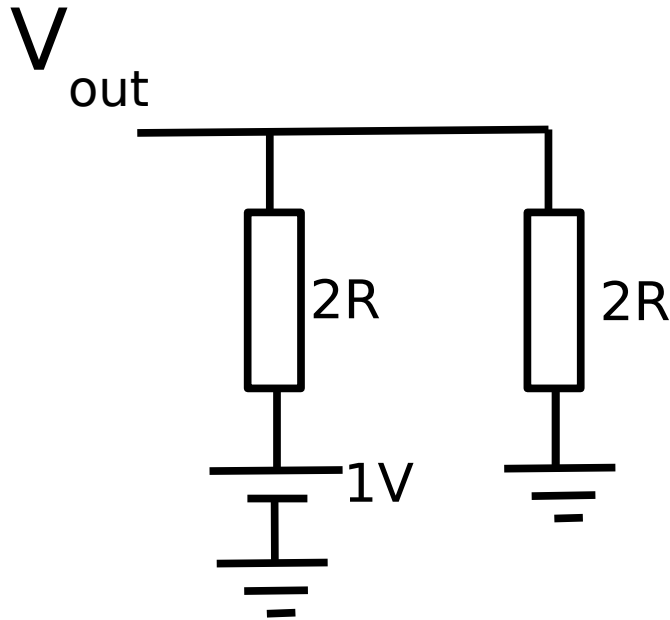
- What can we do now??

Leaving us with.....



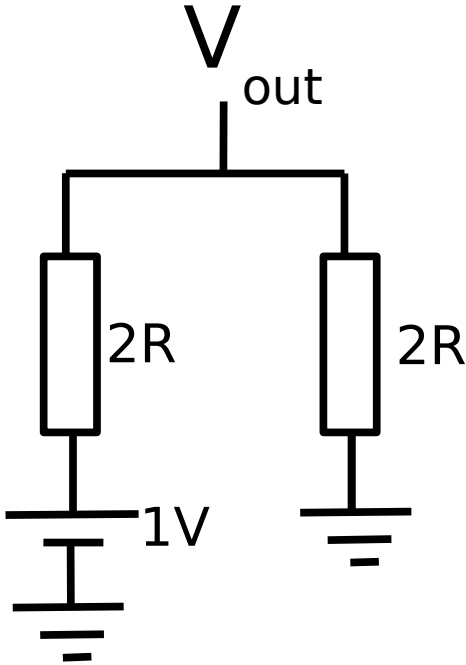
- Join these two resistors together.

And we now have...



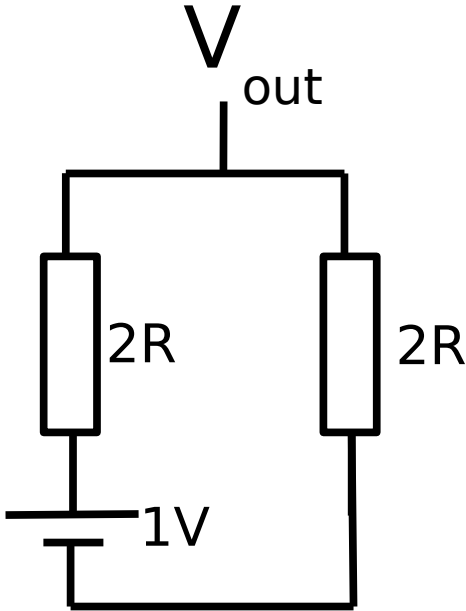
- This looks complicated so let's just move things around to make them less scary.

Move V_{out} to the top - why not?



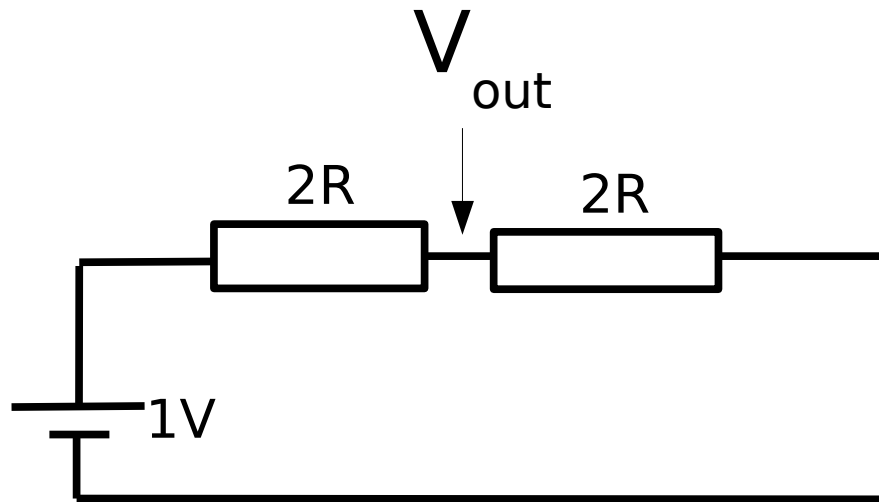
- Looking a bit like a potential divider now.
- Let's get rid of the grounds.

A more simple circuit

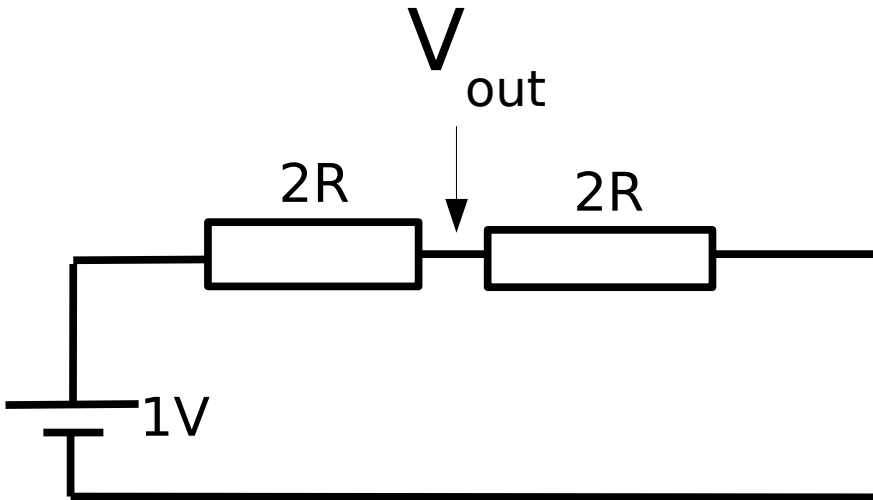


Now let's rearrange this circuit to make it look like something we may understand.

What does this remind you of?



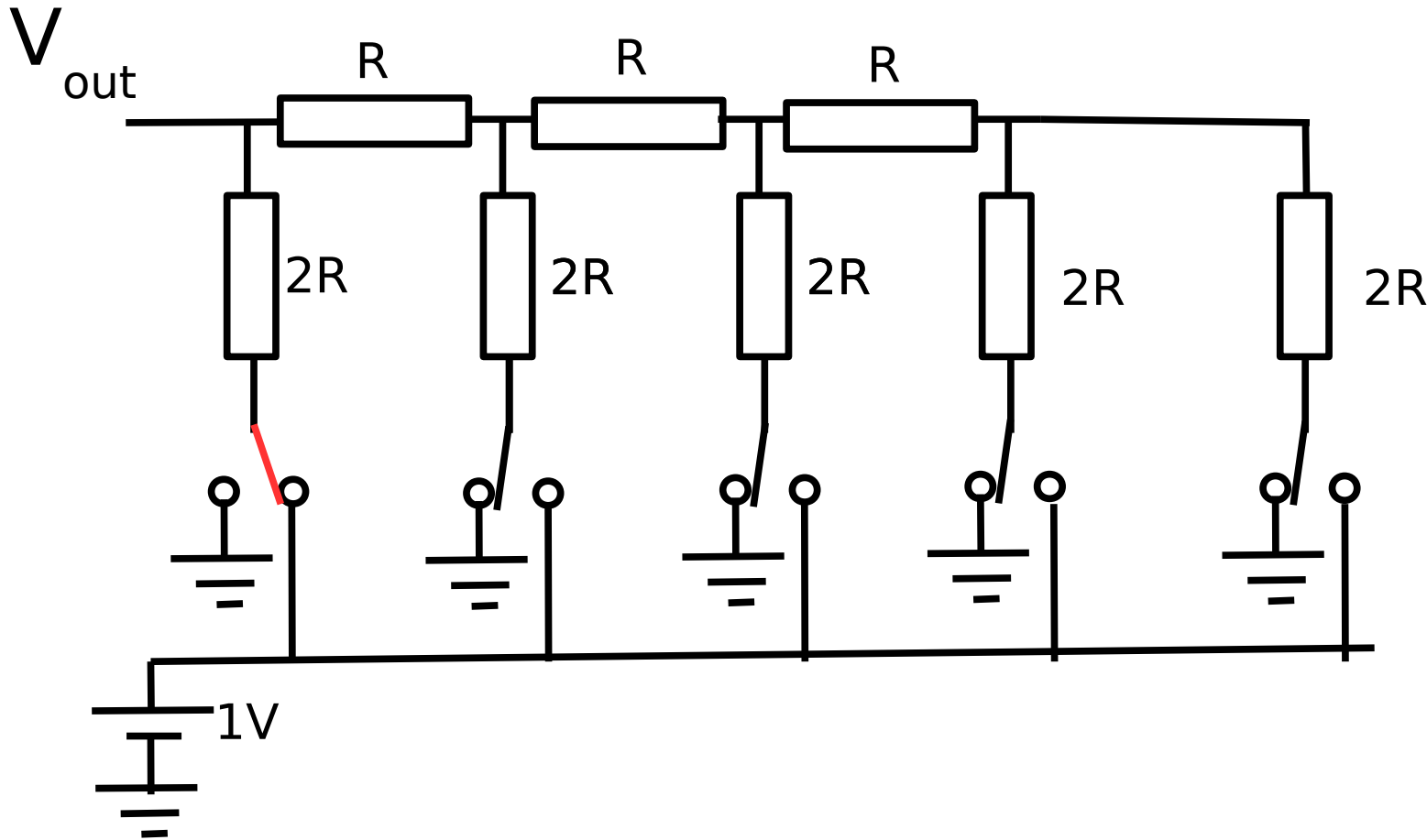
It's a potential divider



$$V_{out} = 1V * \frac{2R}{2R + 2R}$$

Therefore, $V_{out} = 0.5V$

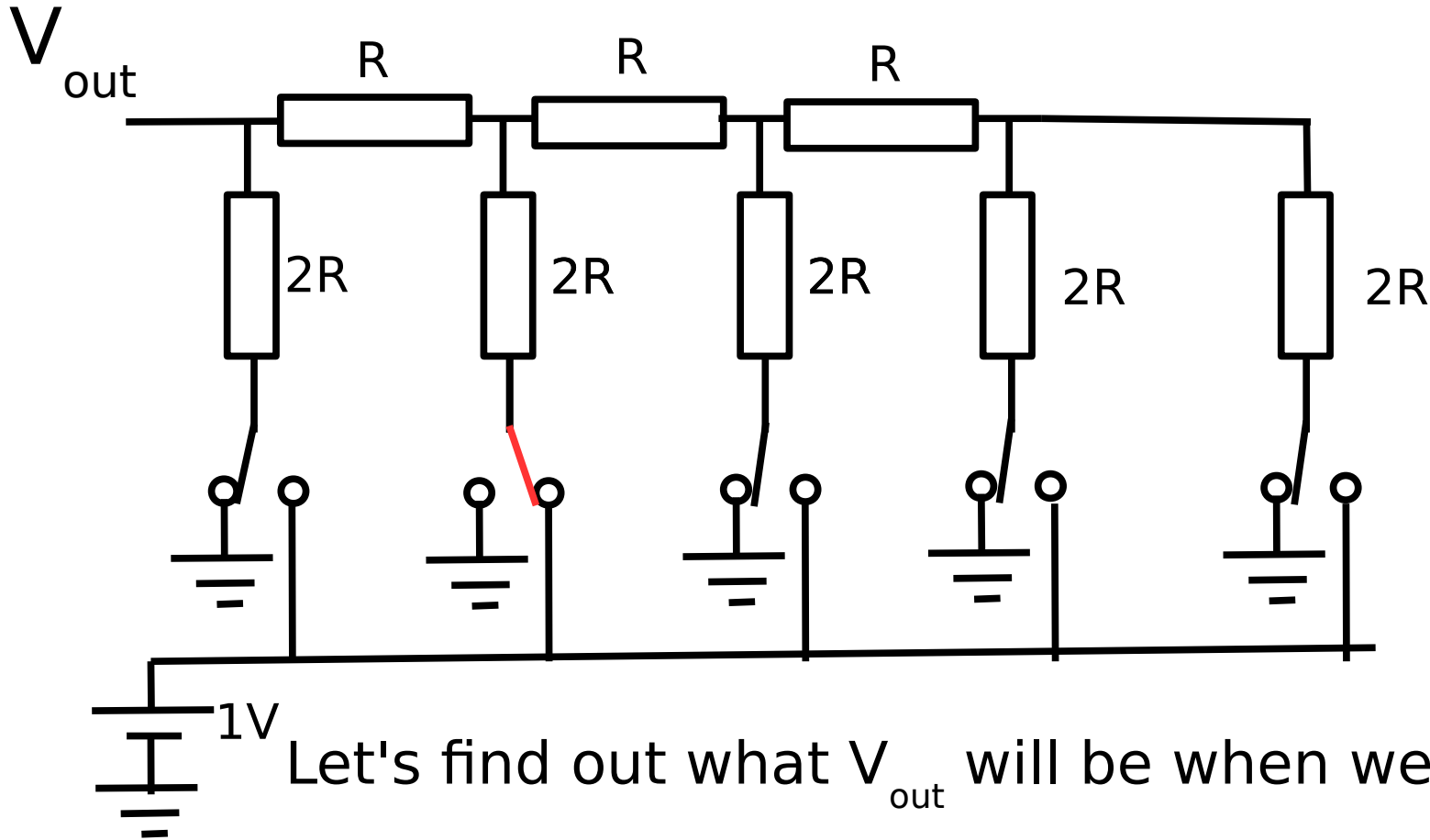
If the first resistor is switched on we get $V_{out} = 0.5$ on the output.



$$V_{out} = 0.5$$

<-Remember this at least for the next 15 min

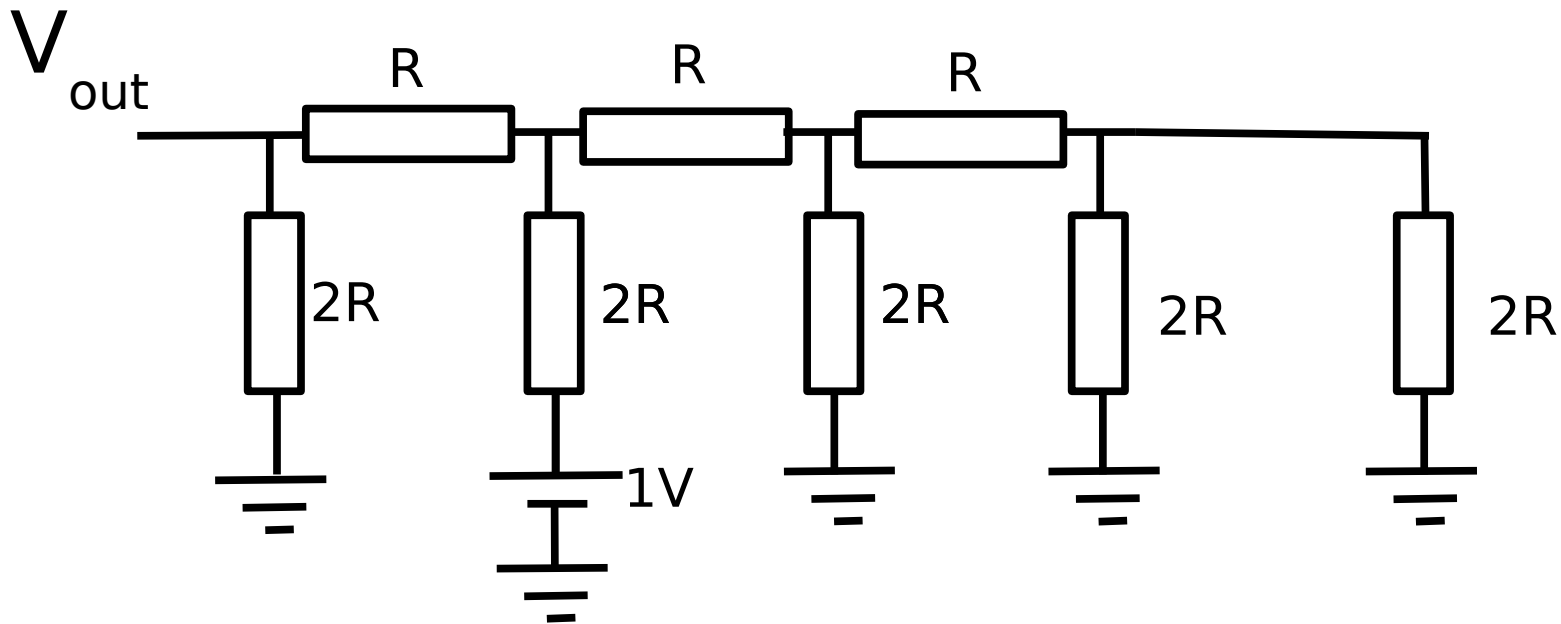
Now lets look at the second digital input.



Let's find out what V_{out} will be when we turn this on.

- This would represent the binary number 01000

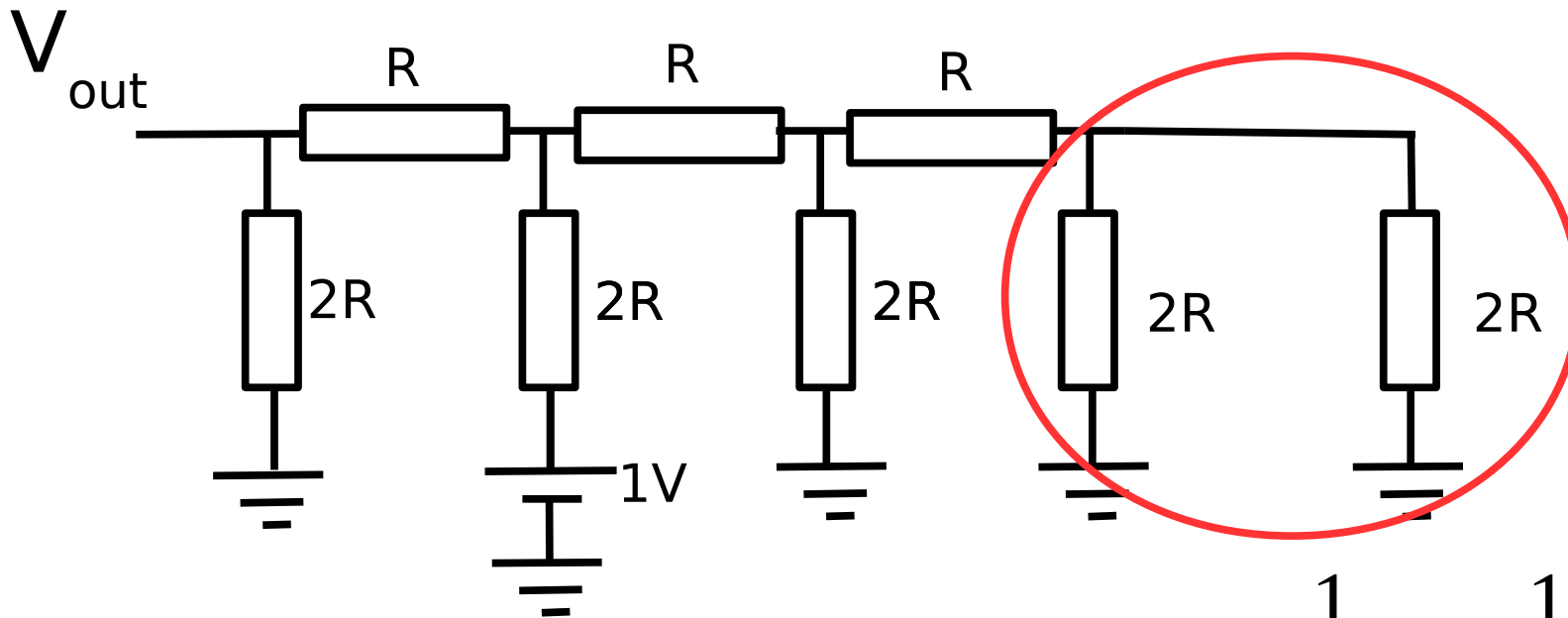
Let's look at input 2 (This is the last pin we will examine)



Starting from the right hand side again.



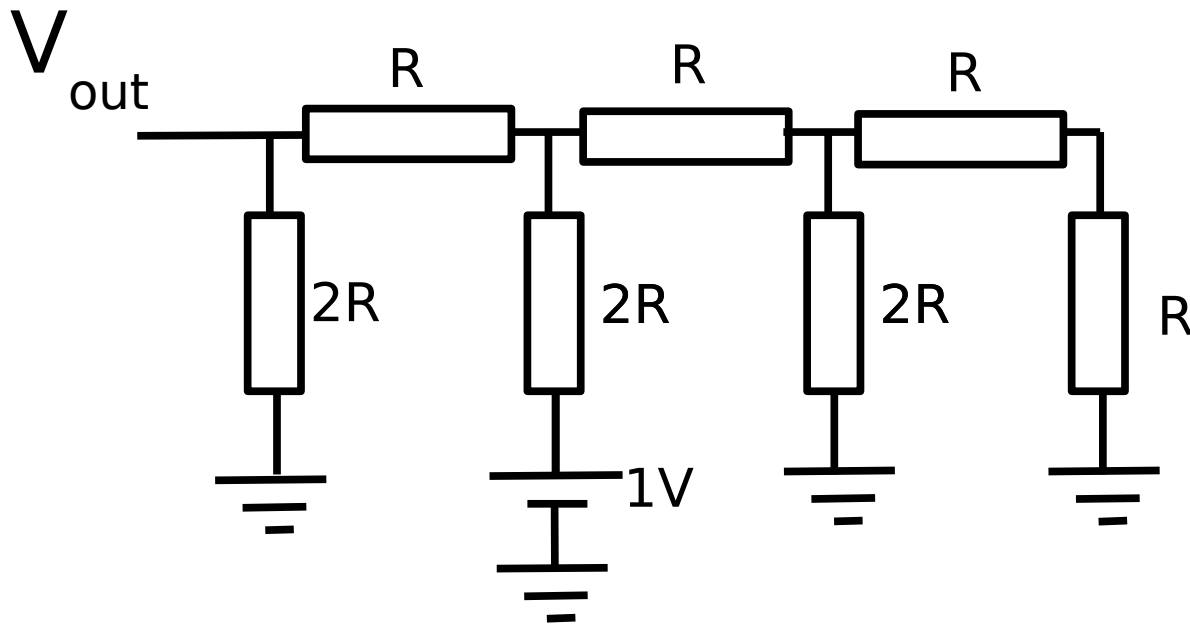
Two resistors in parallel



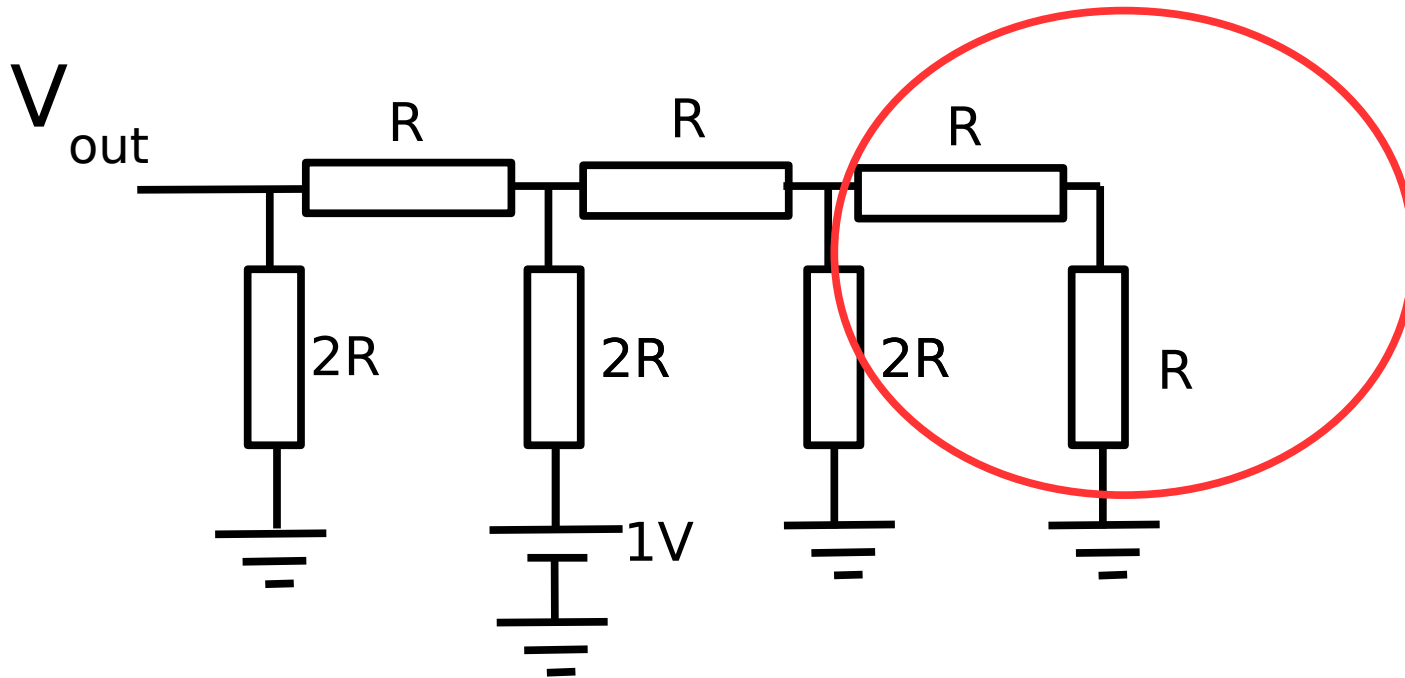
$$\frac{1}{R_{new}} = \frac{1}{2R} + \frac{1}{2R}$$

$$R_{new} = R$$

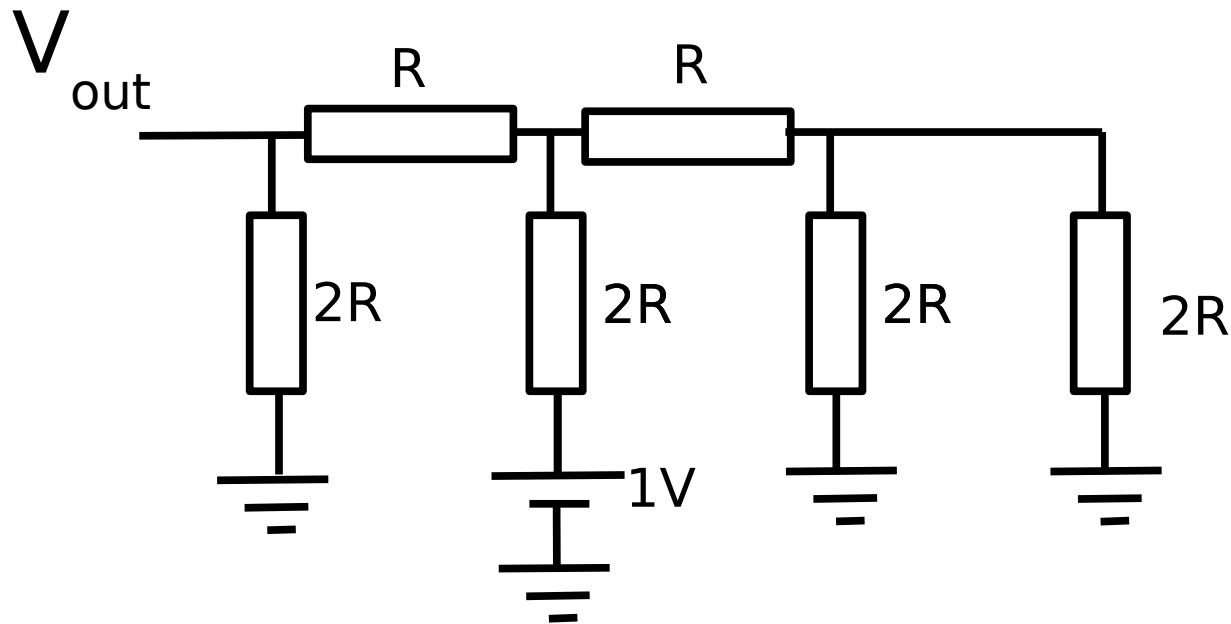
Gives....



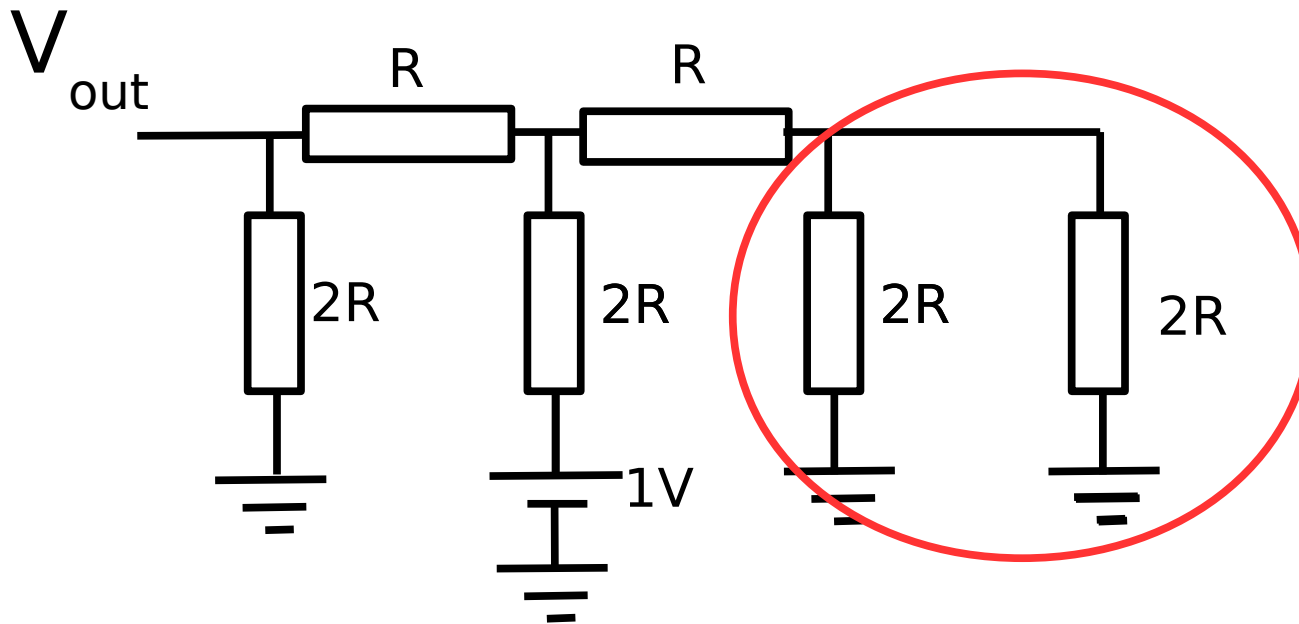
R + in series gives..



Gives $2R$



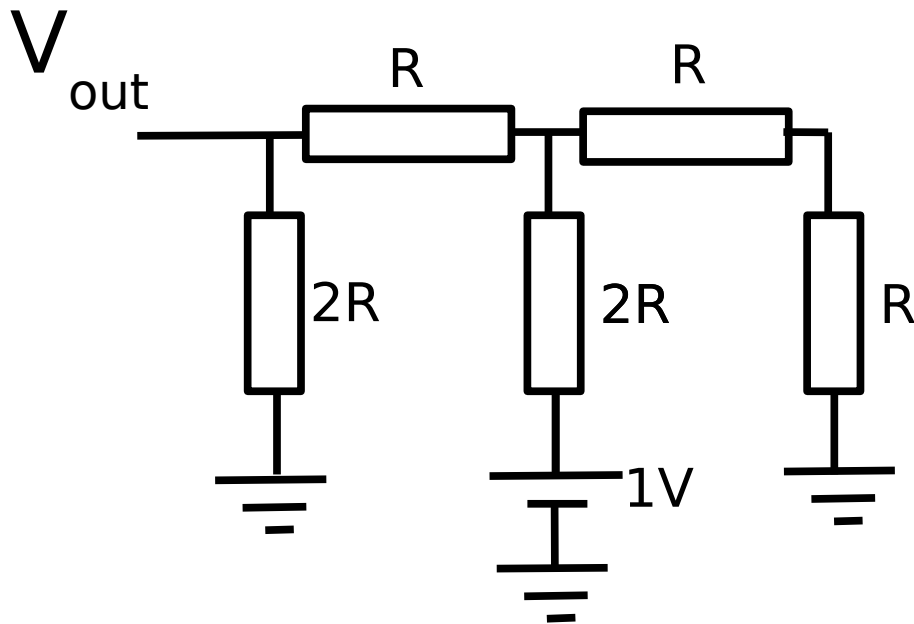
2R and 2R in parallel gives



$$\frac{1}{R_{new}} = \frac{1}{2R} + \frac{1}{2R}$$

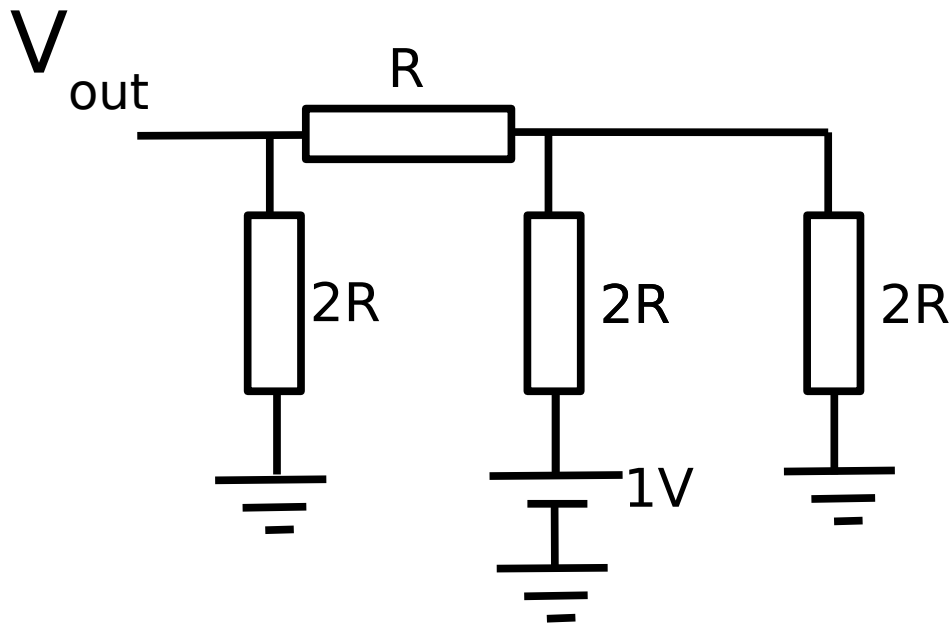
$$R_{new} = R$$

This gives R



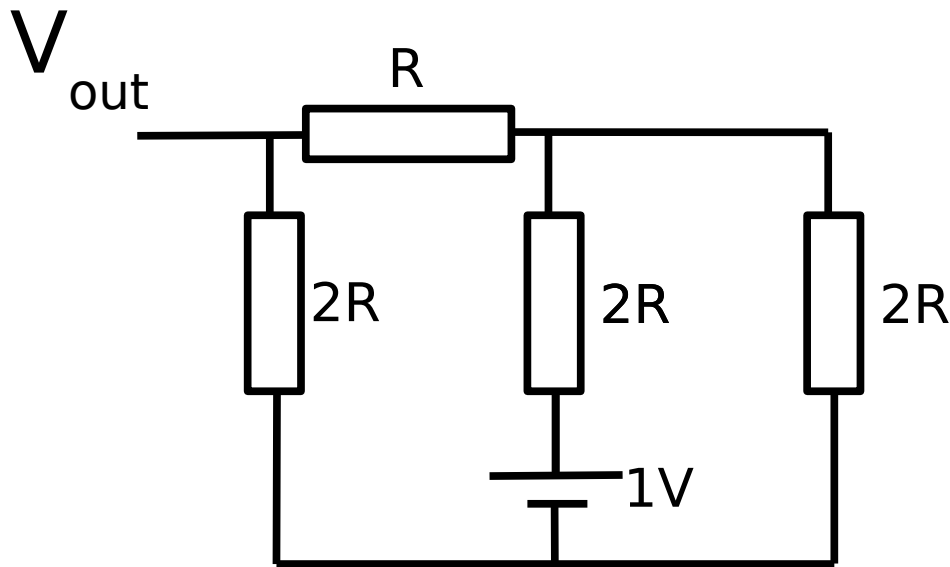
Tidying up $R+R..$

We are left with this circuit



Let's get rid of the ground signs because they are confusing.

That's better

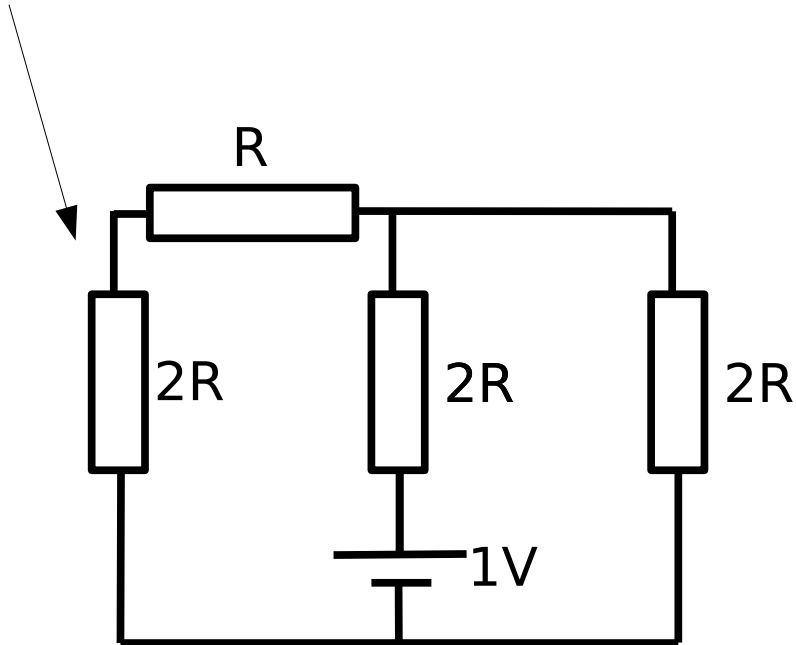


For the moment let's also get rid of V_{out} .

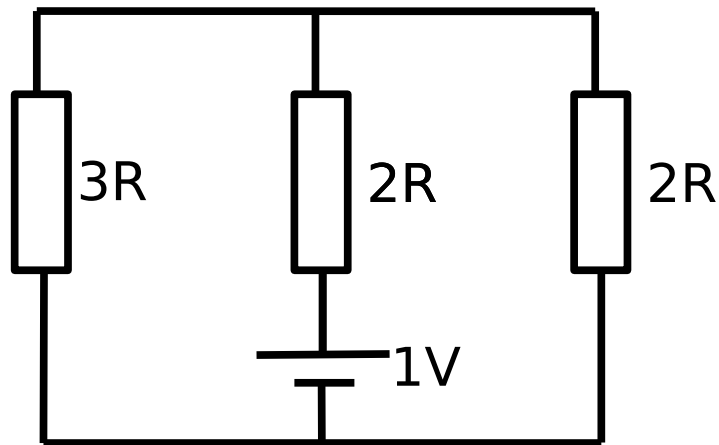
This is looking more simple



Join R and 2R together.

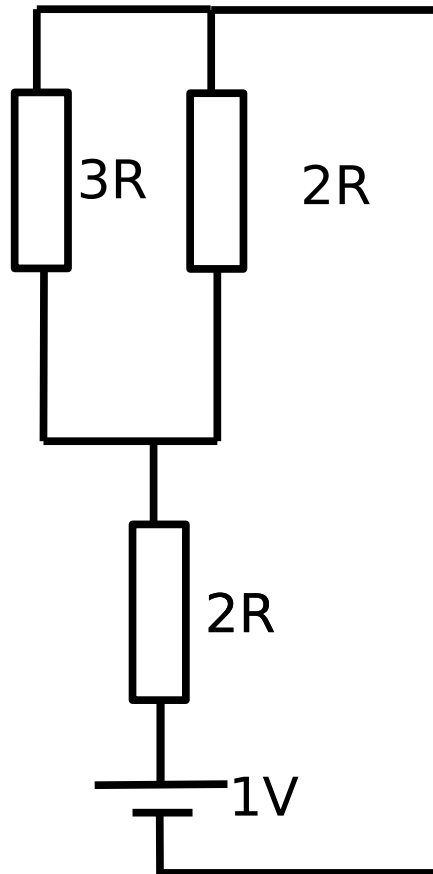


Even more manageable



Let's redraw this in a more easy to understand form..

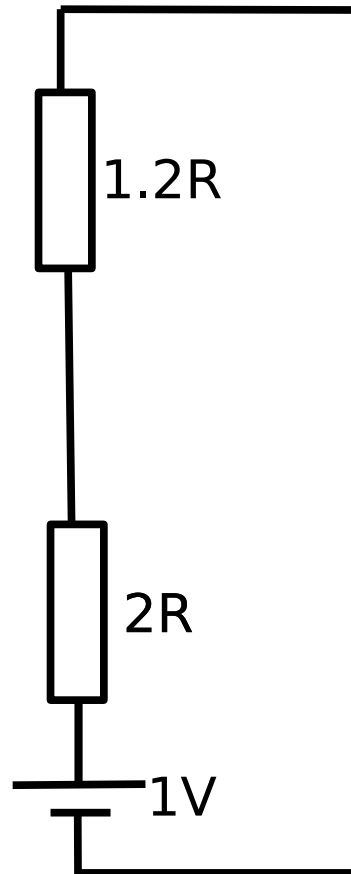
Two resistors in parallel.



$$\frac{1}{R_{\text{new}}} = \frac{1}{3R} + \frac{1}{2R}$$

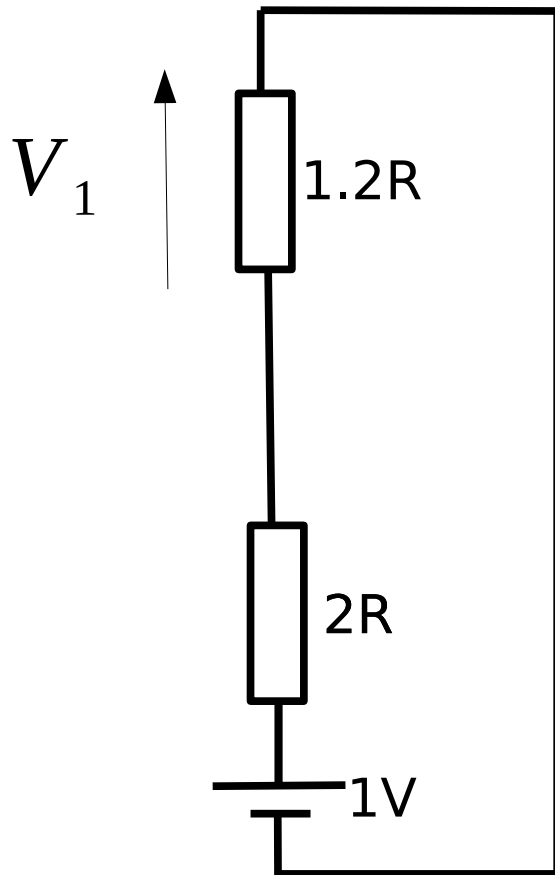
$$R_{\text{new}} = 1.2R$$

Now we just have a potential divider



What's this circuit?

Now we just have a potential divider

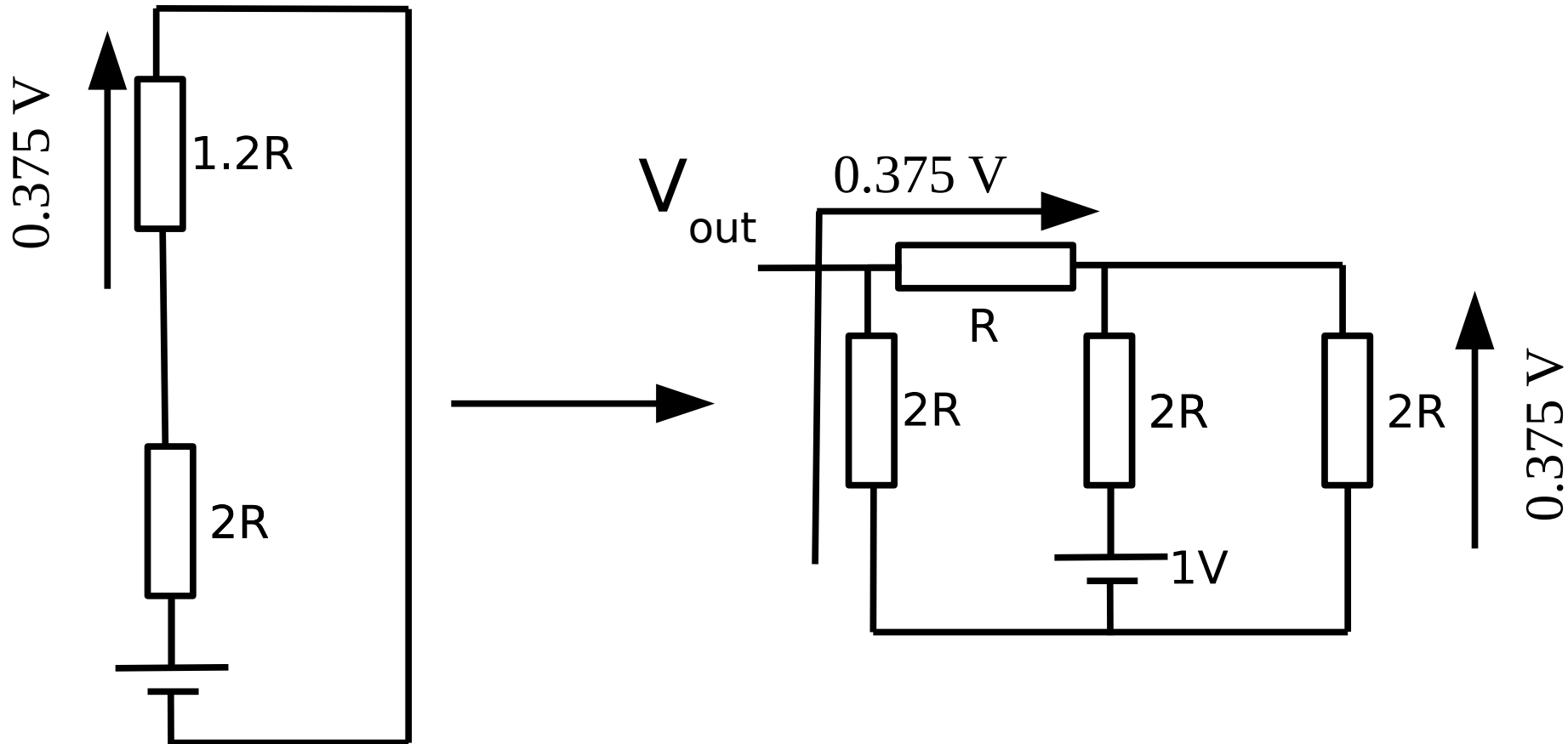


The voltage across $1.2 R$ is.

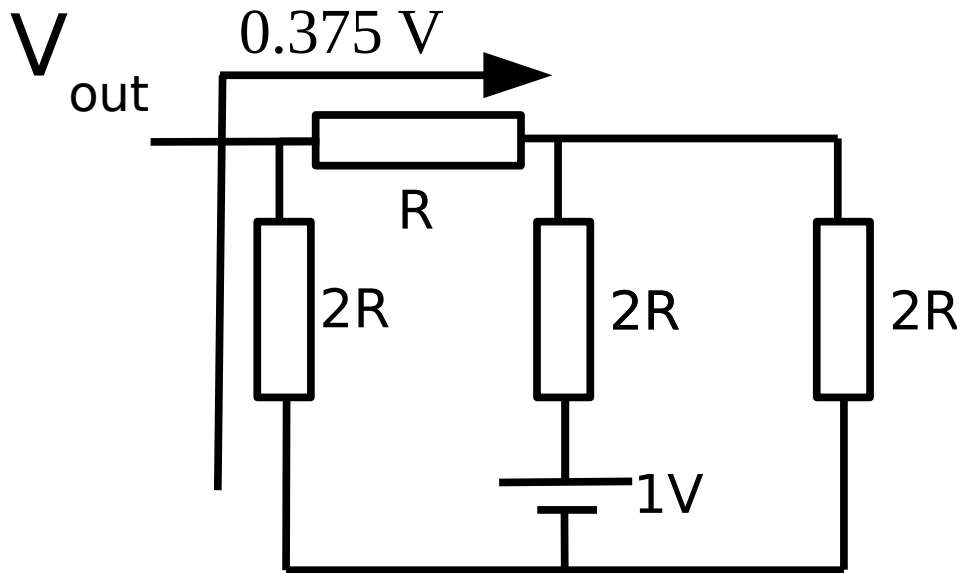
$$V_1 = 1 V \frac{1.2 R}{2 R + 1.2 R}$$

$$0.375 V$$

Superimposing this voltage on our original circuit.

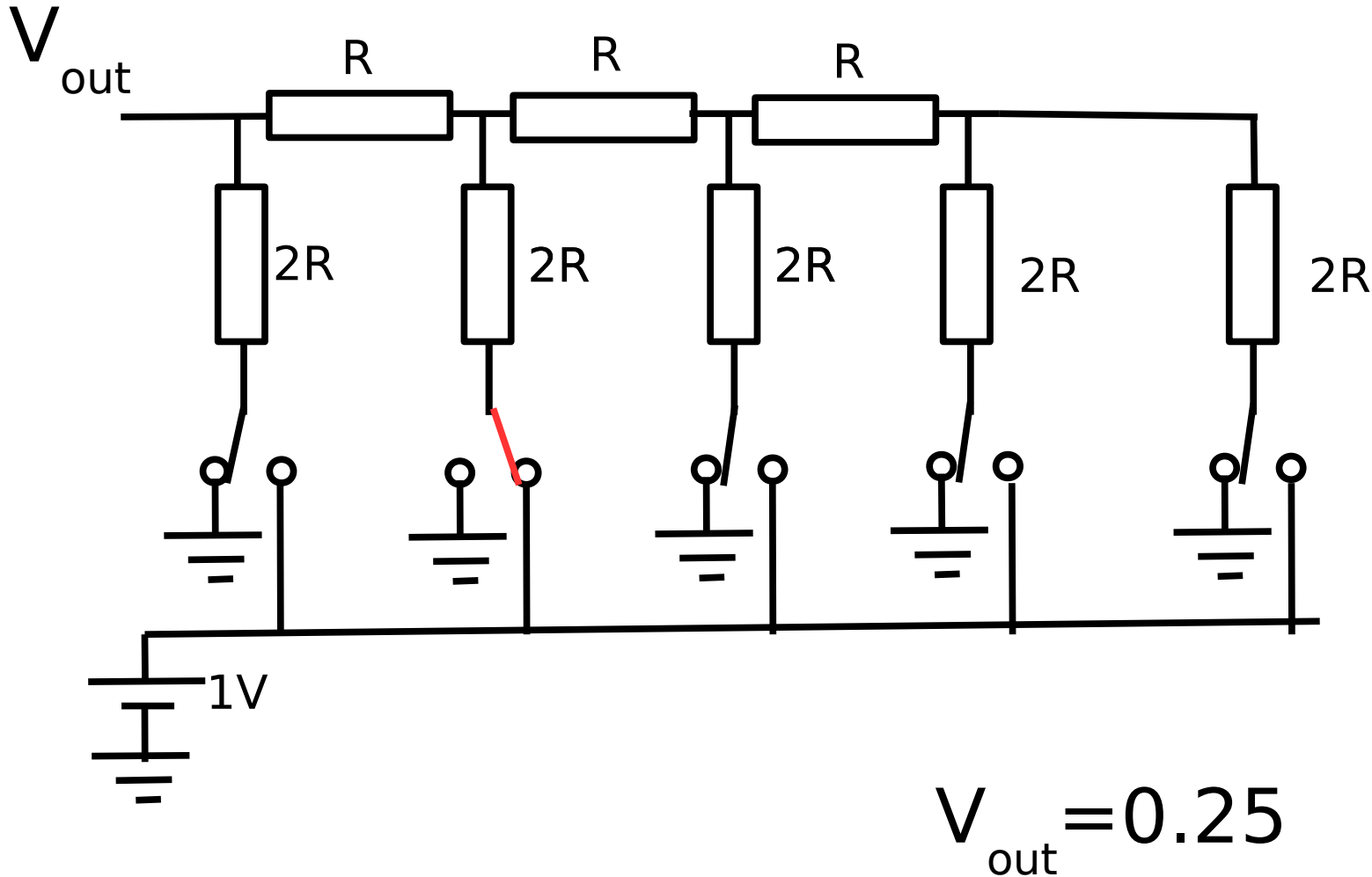


Another potential divider



$$V_{out} = 0.375 \frac{2R}{R + 2R} = 0.25 V$$

If the **second** resistor is switched on we get $V_{\text{out}} = 0.25$ on the output.

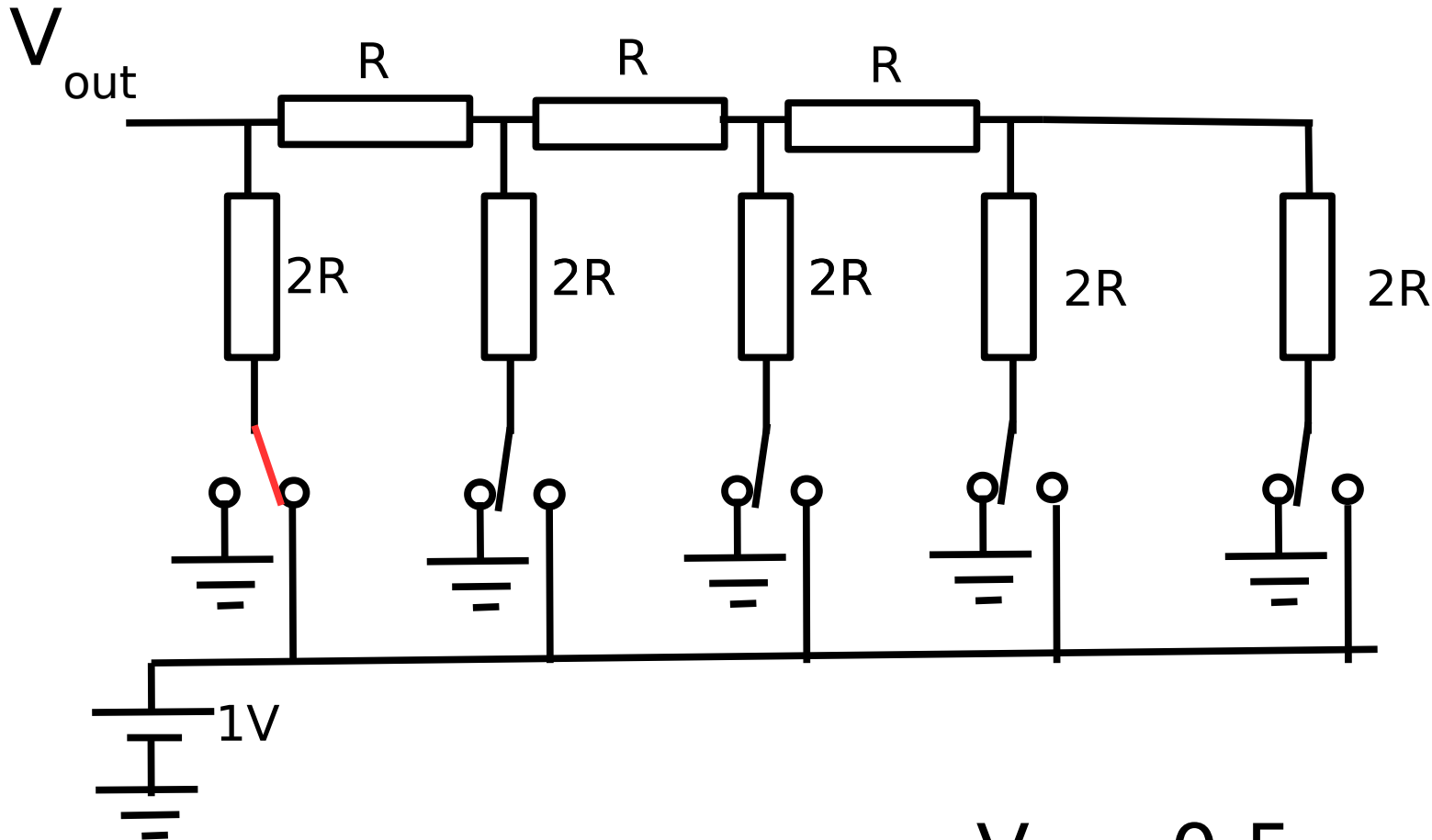


Life is short – so we won't look at any more pins



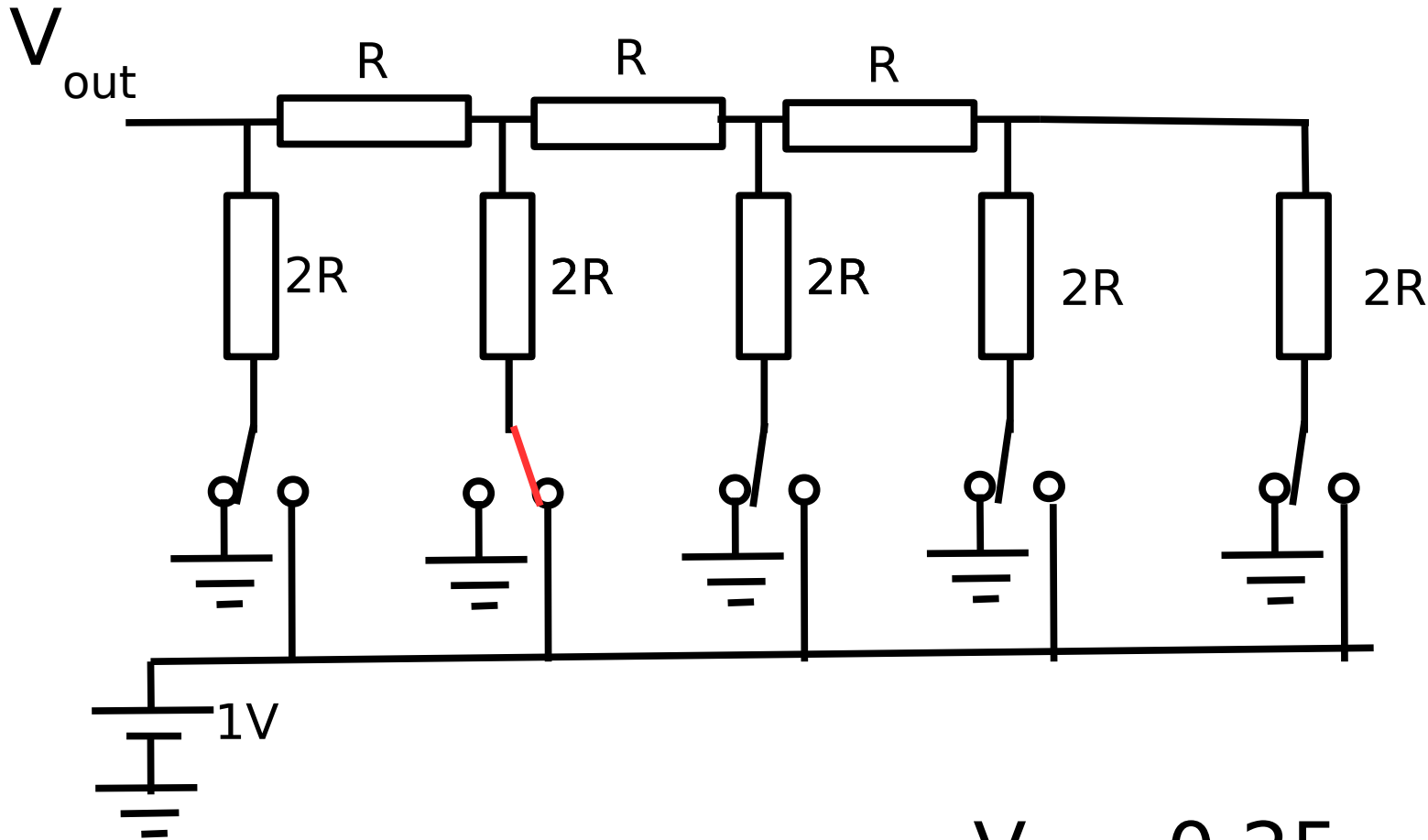
- I will just tell you what happens for the rest of the pins now.

Input 1 representing binary 10000



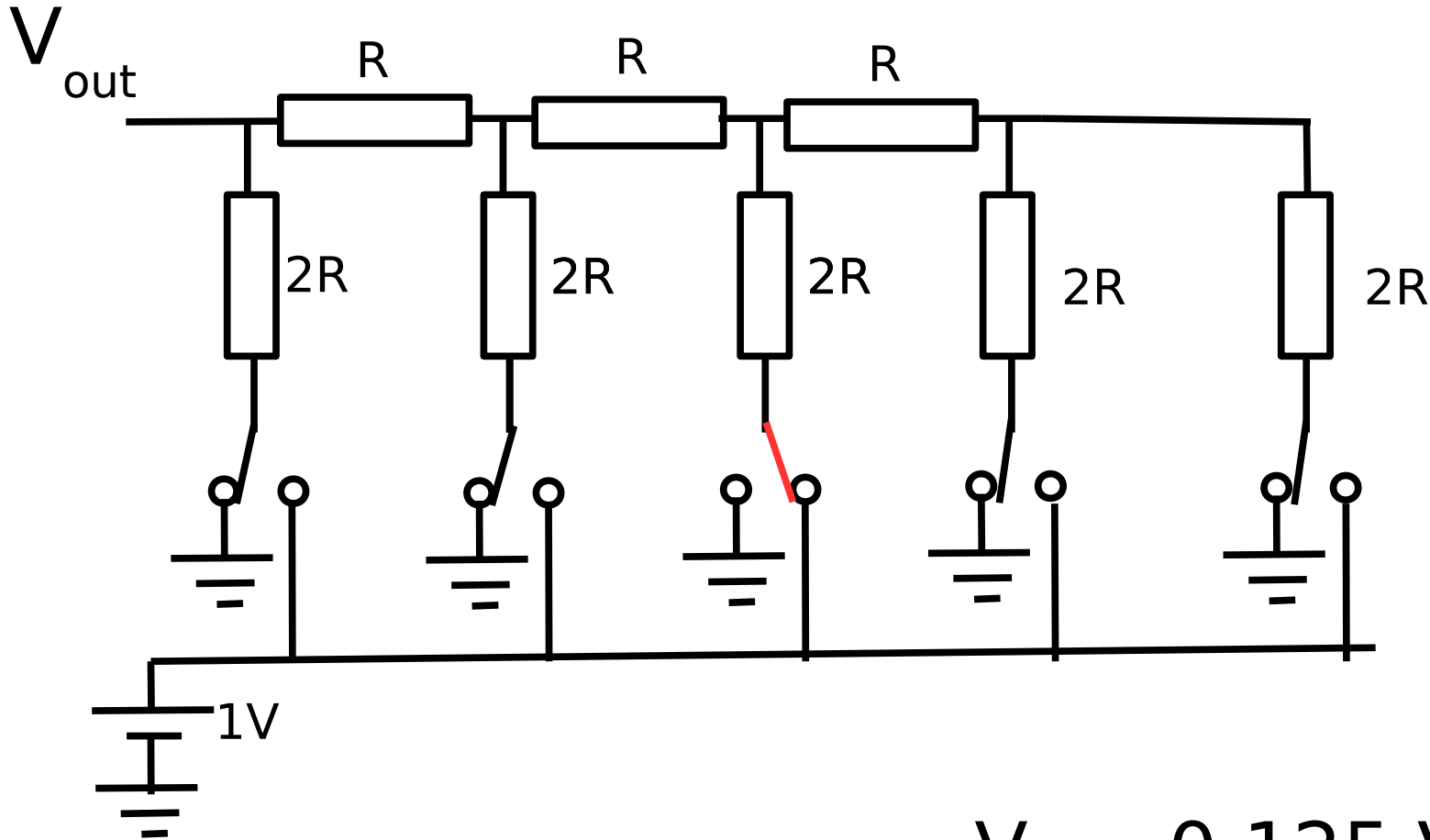
$$V_{out} = 0.5$$

Input 2 representing binary 01000



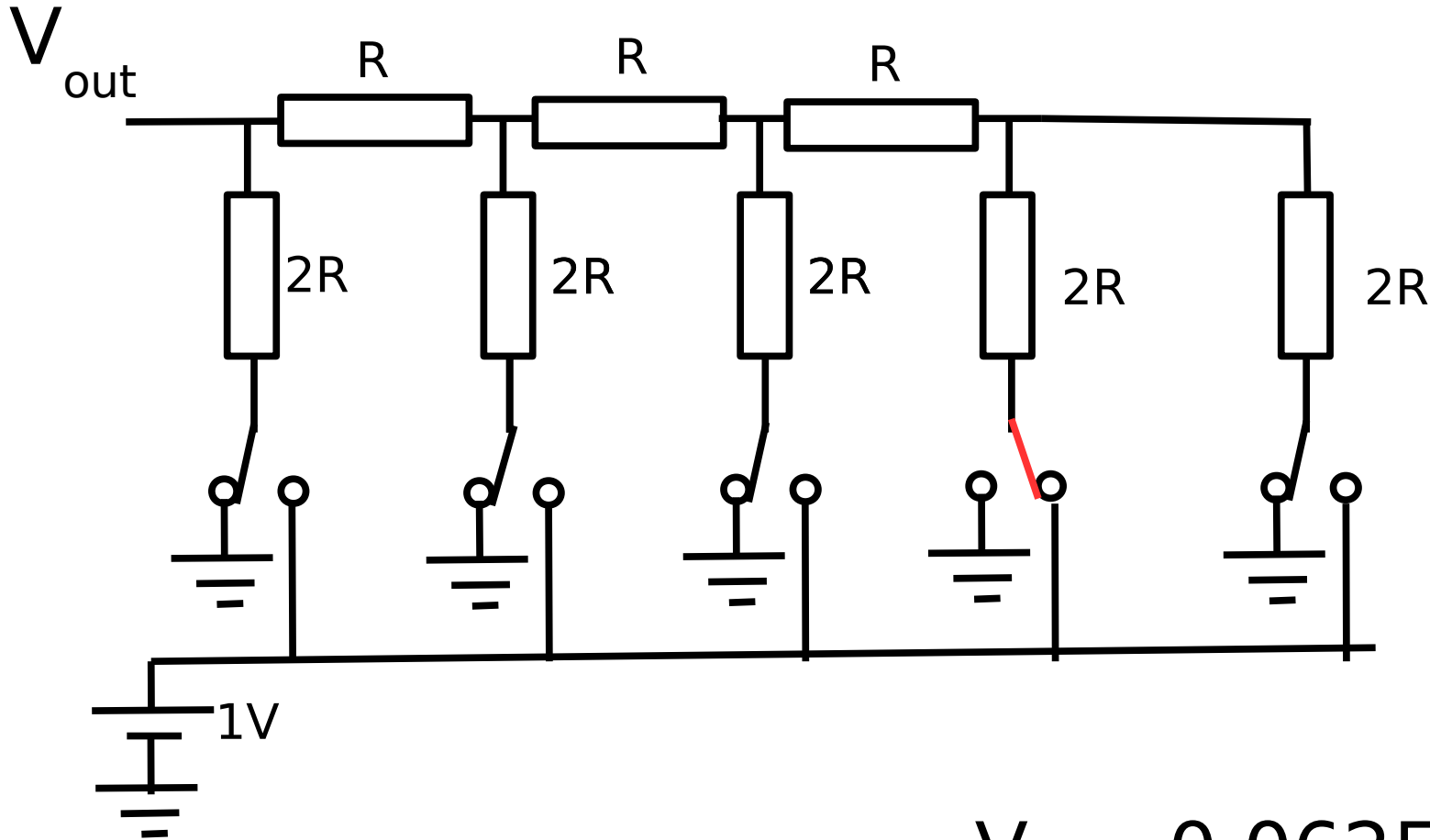
$$V_{out} = 0.25$$

Input 3 representing binary 00100



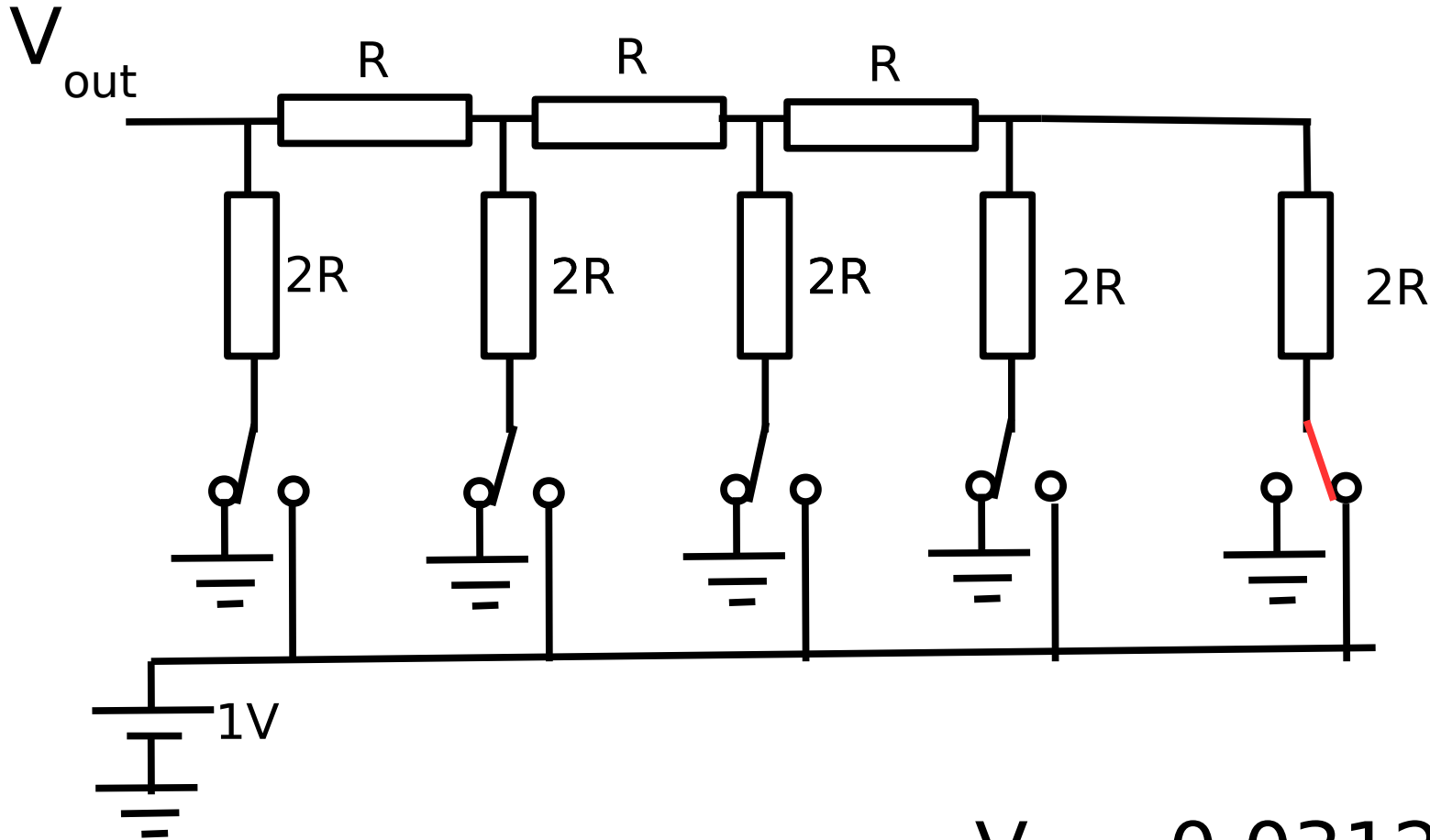
$$V_{out} = 0.125 \text{ V}$$

Input 4 representing binary 00010



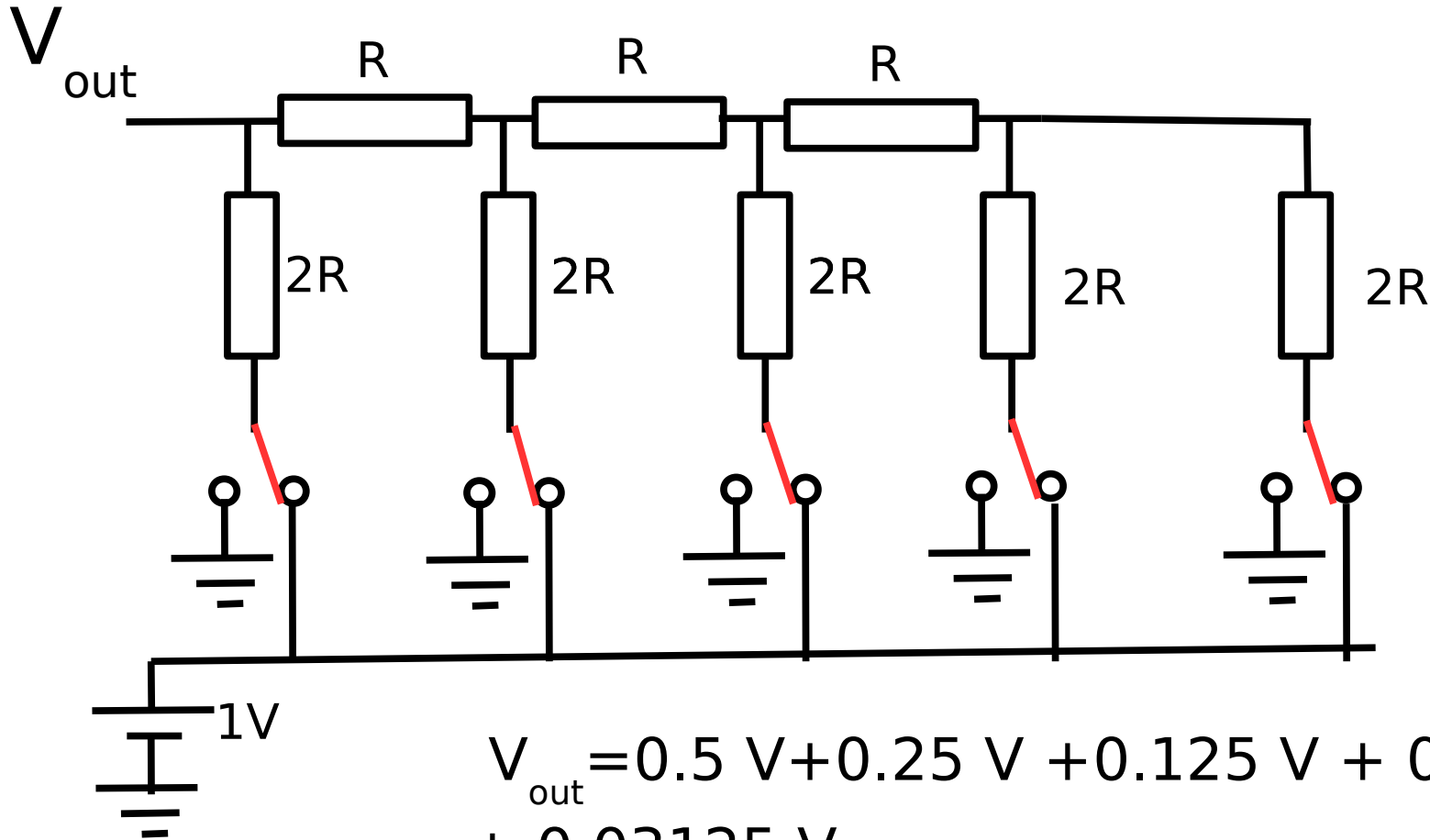
$$V_{out} = 0.0625 \text{ V}$$

Input 5 representing binary 00001



$$V_{out} = 0.03125 \text{ V}$$

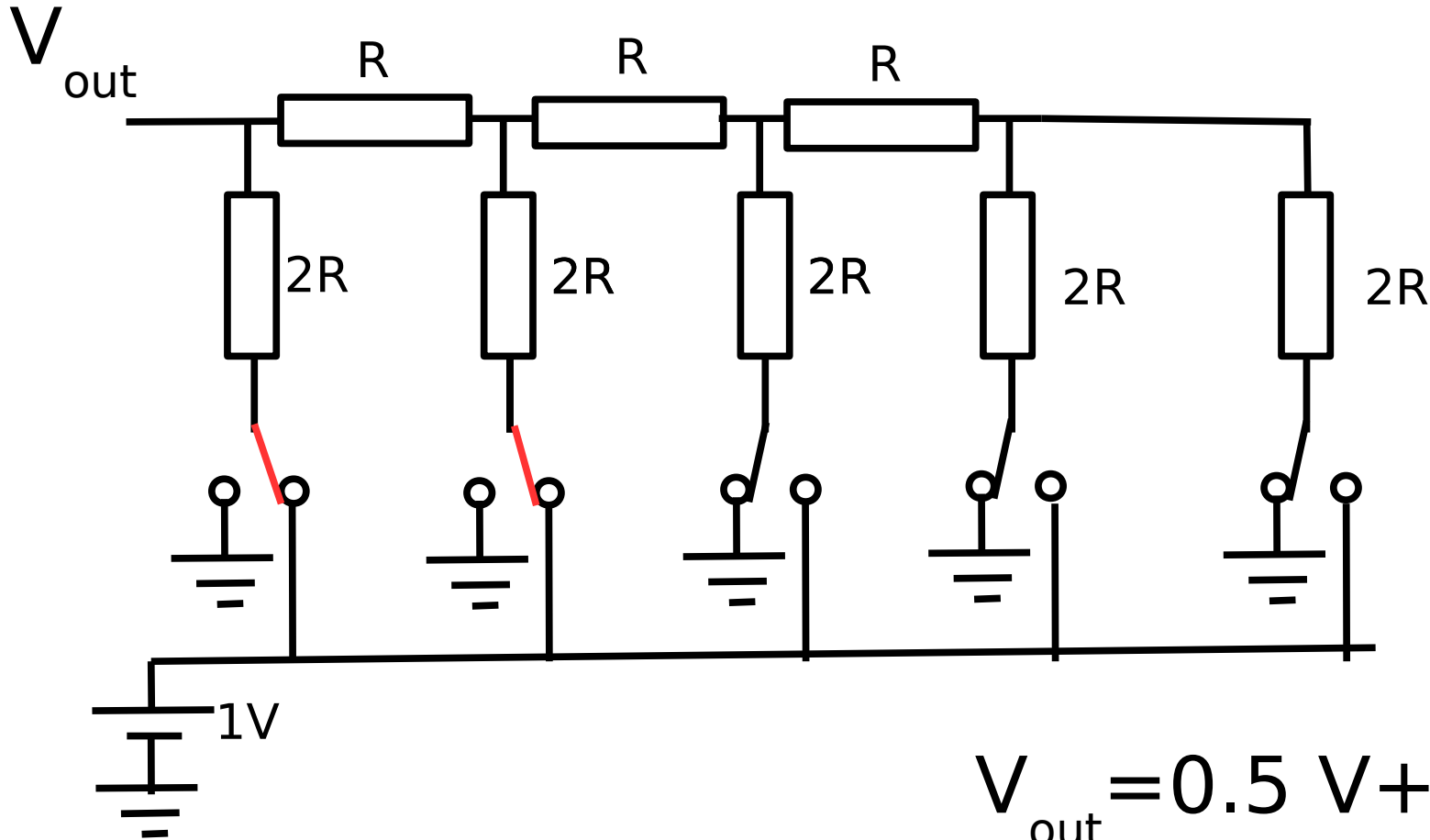
Inputs 1, 2, 3, 4, and 5 - (11111)



$$V_{out} = 0.5 \text{ V} + 0.25 \text{ V} + 0.125 \text{ V} + 0.0625 \text{ V} + 0.03125 \text{ V}$$

$$V_{out} = 1 \text{ V}$$

We can turn on any combination on
i.e. 11000



$$V_{out} = 0.5 V + 0.25 V$$

$$V_{out} = 0.75 V$$

Question



- Does this remind you of anything?

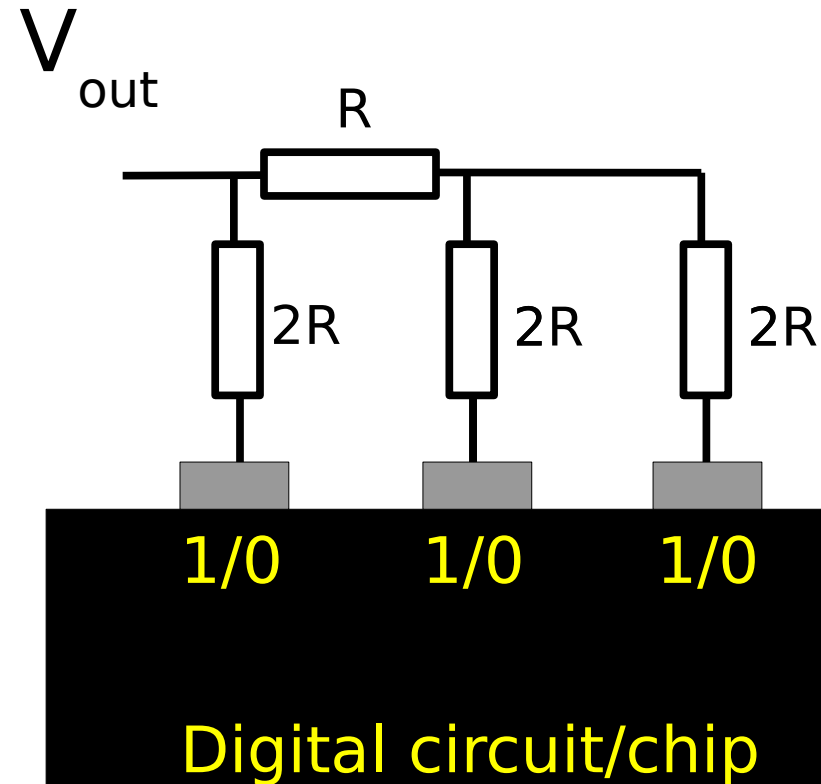
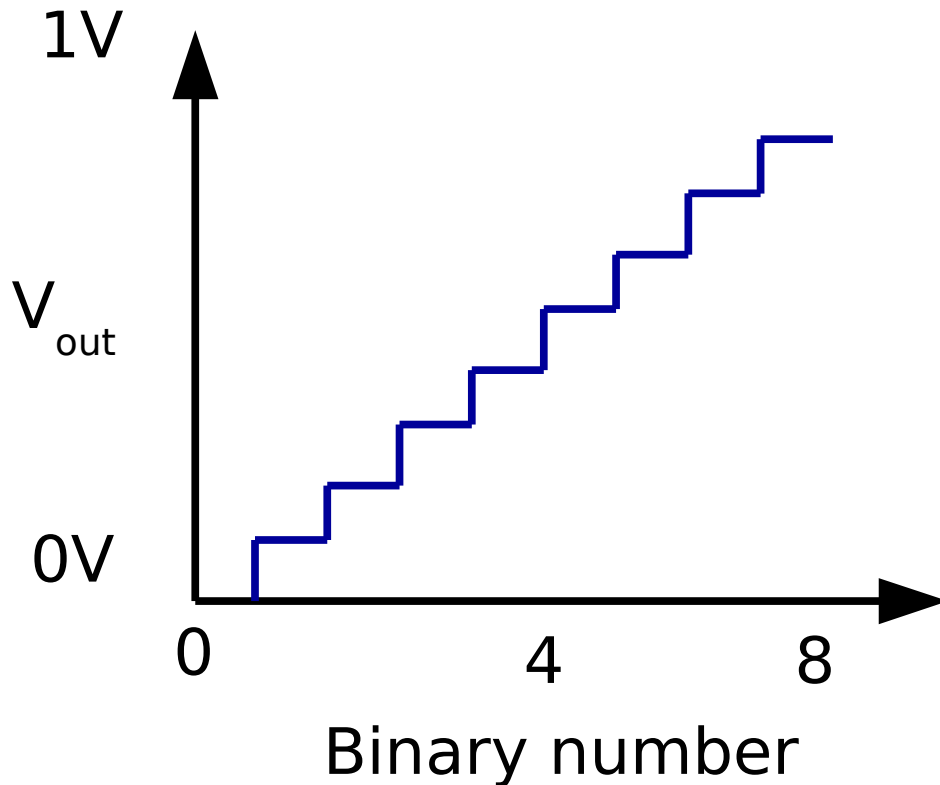


- Sort of counting in binary...

If we connect the R2R ladder to the binary output from a chip...



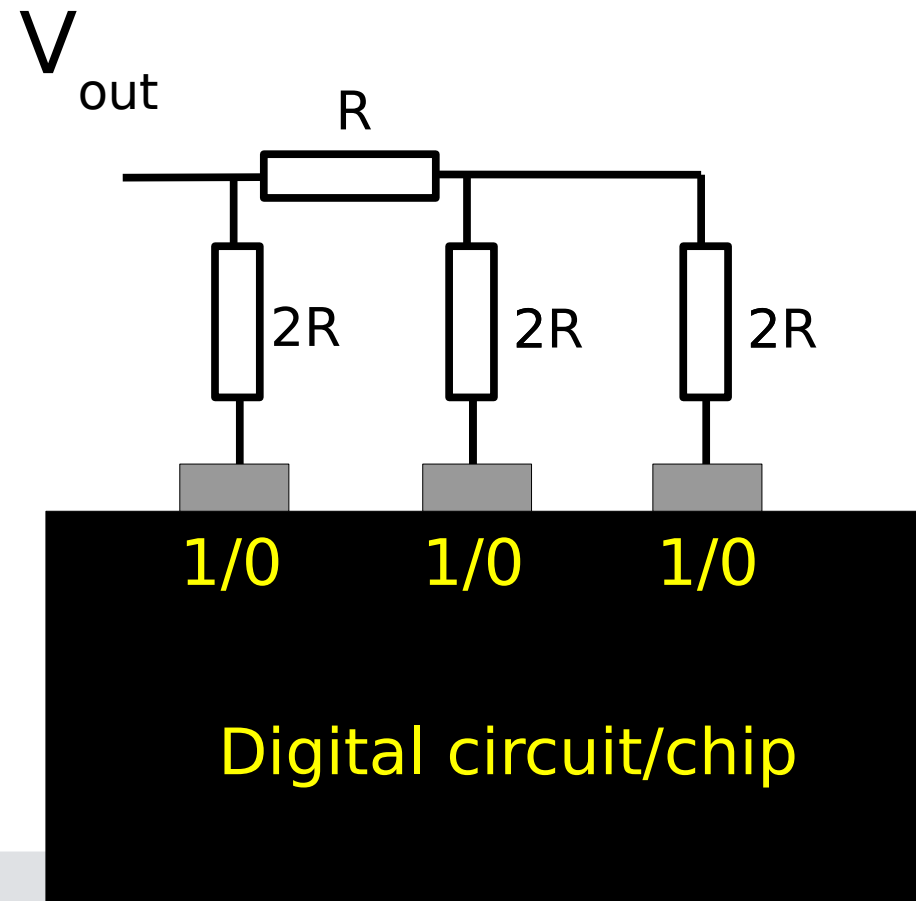
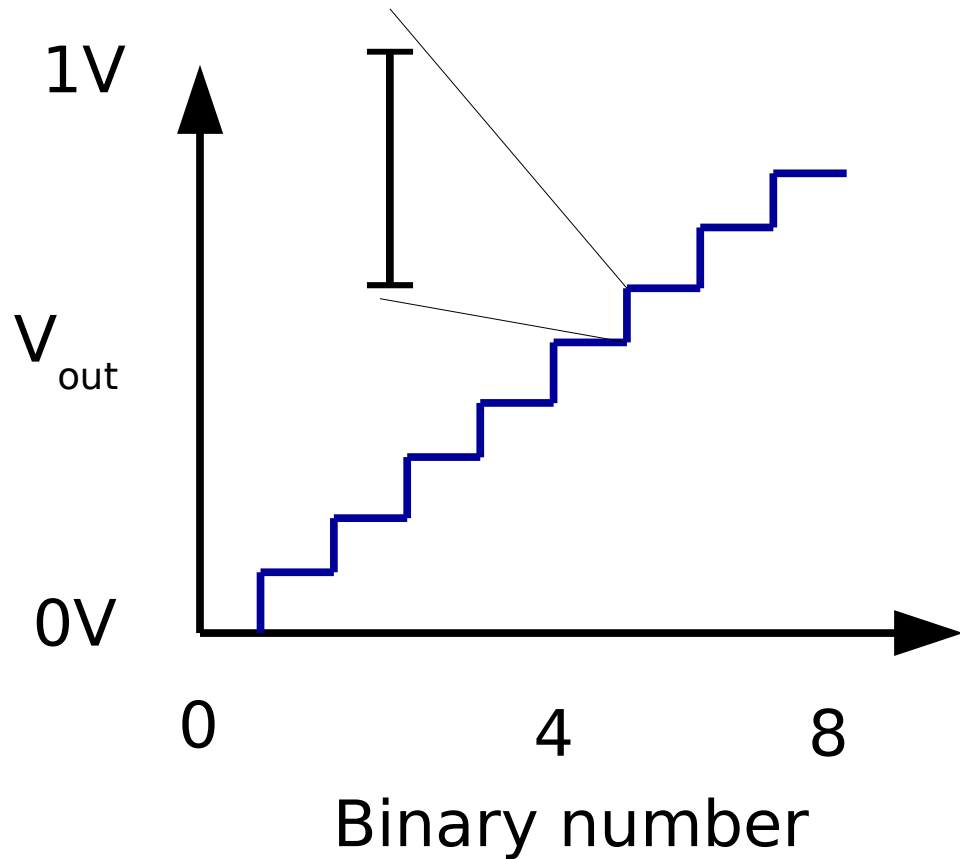
- We can generate any voltage between 0 V and 1 V



R2R ladder resolution



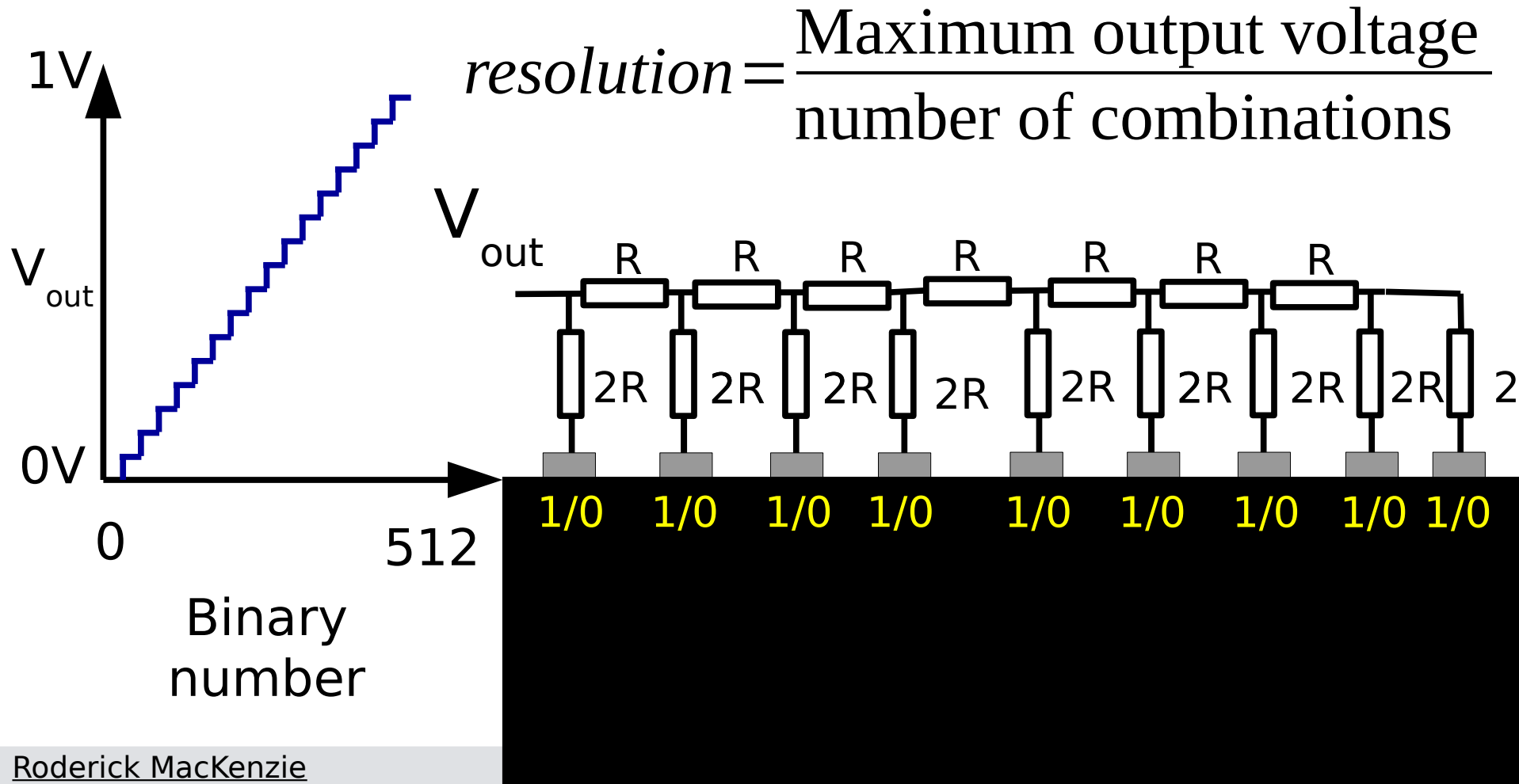
$$\text{resolution} = \frac{\text{Maximum output voltage}}{\text{number of combinations}}$$



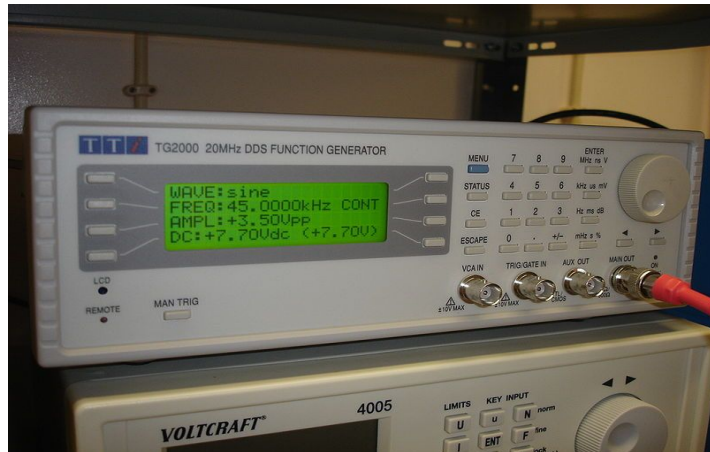
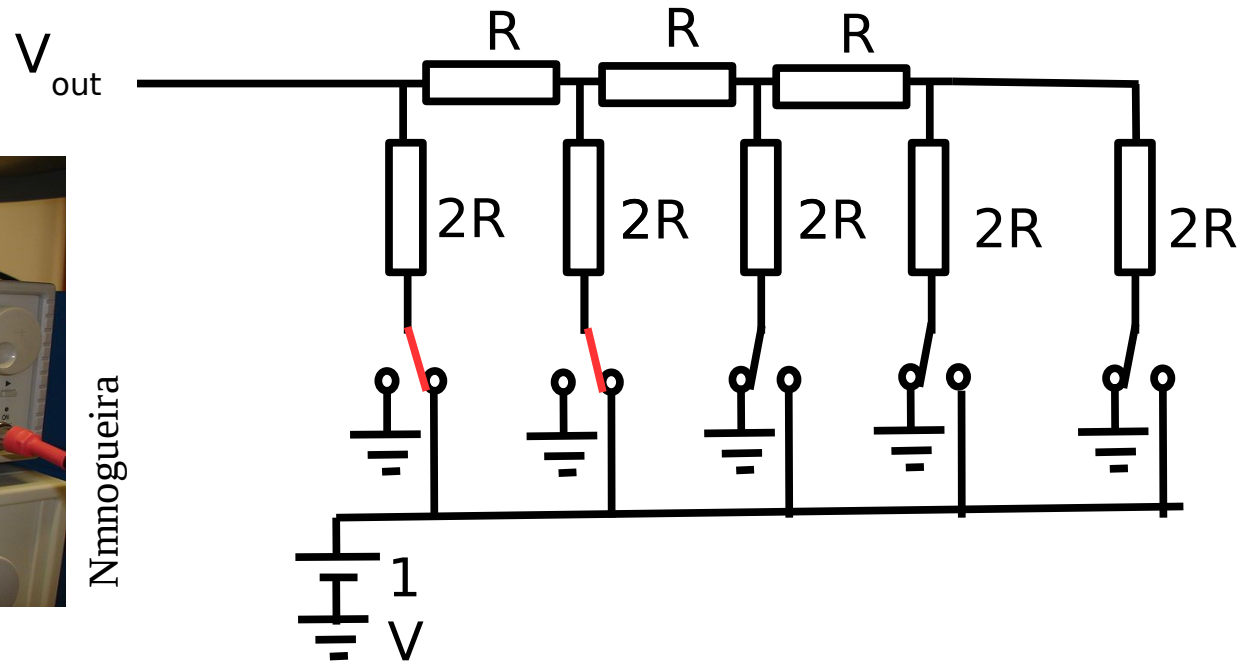
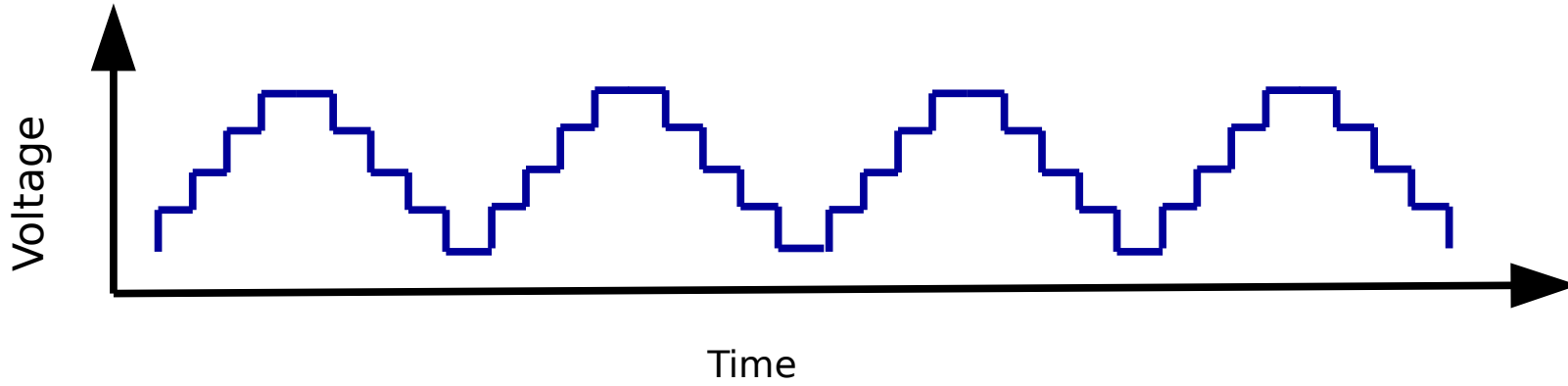
The more pins we have



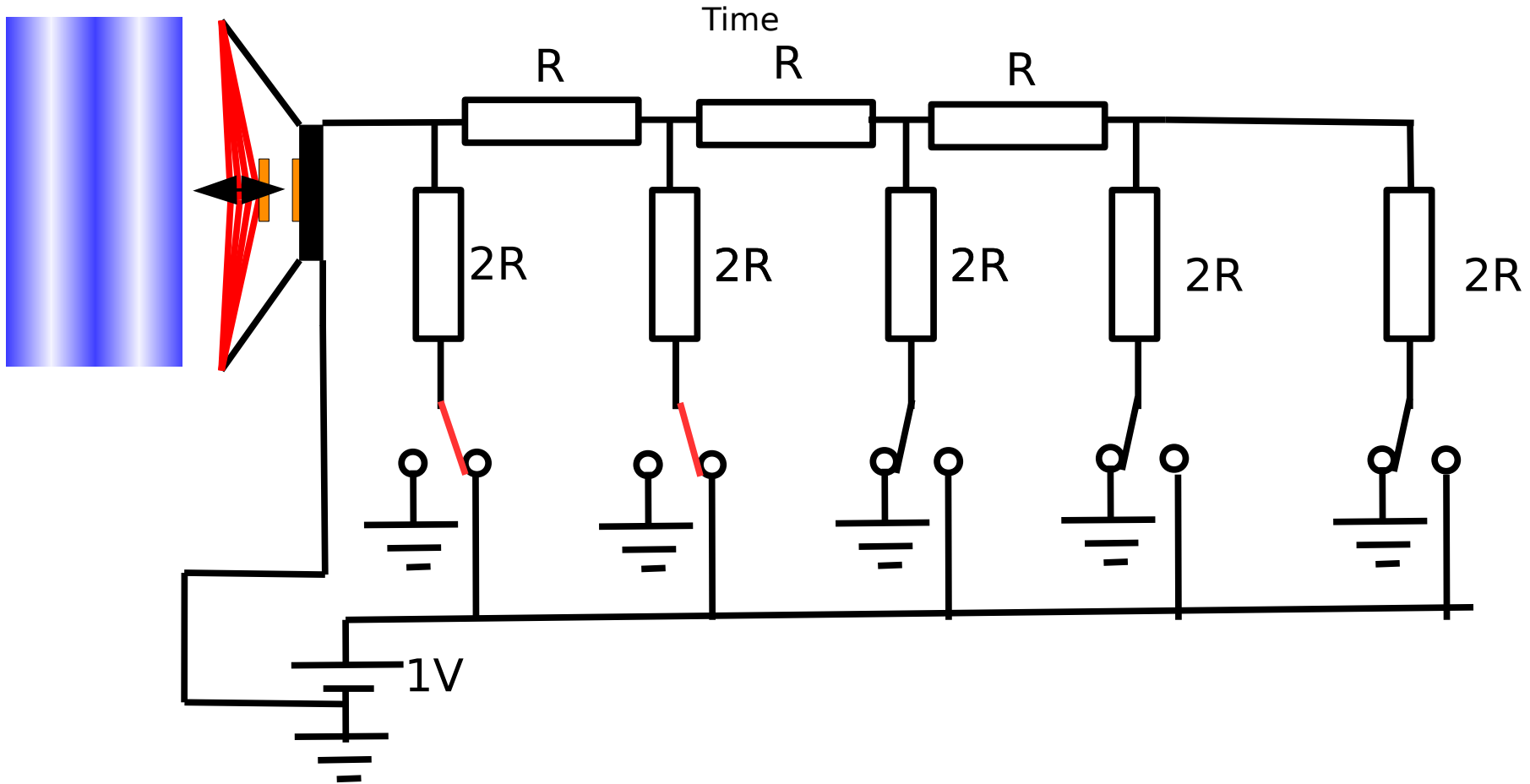
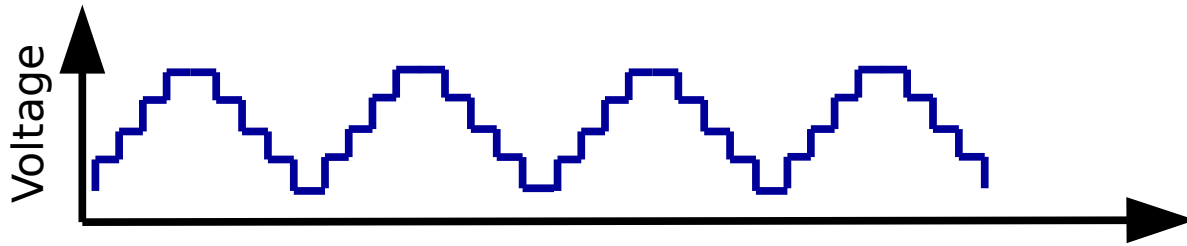
- The finer the resolution we get.



We can now make any shape analog signal we want.



If we attach a speaker we get a tone.

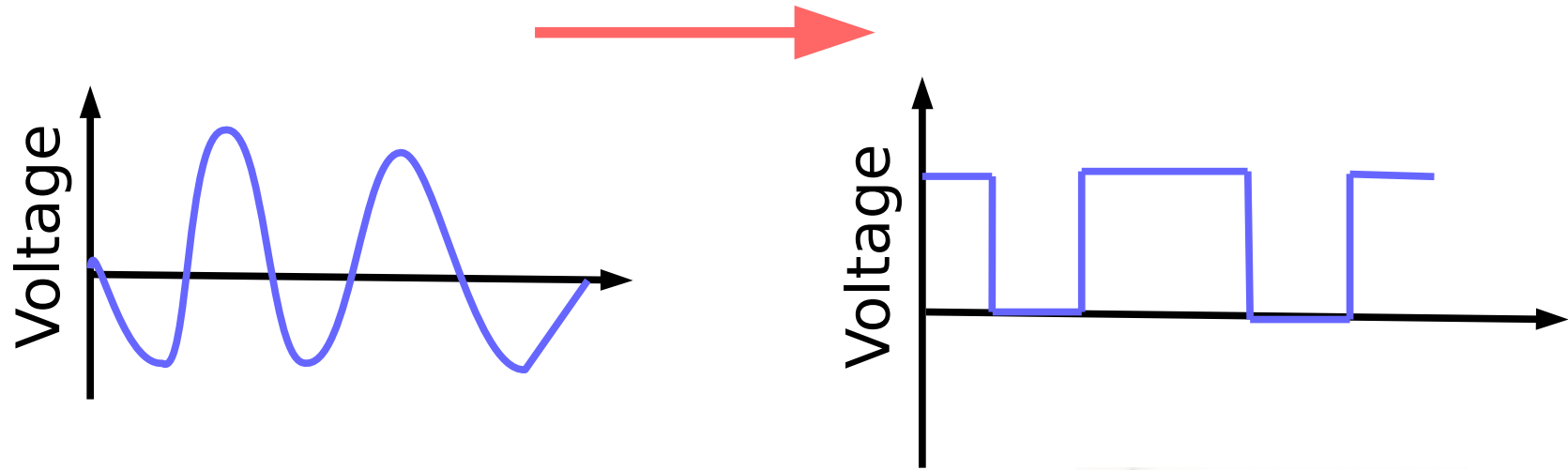




Outline of the lecture

- No recap of last lecture :)
- Recap of digital signals
- Converting between digital and analog
 - Digital to analog converters
 - **Analog to digital converters**
 - Flash converters for high speed video
- Summary

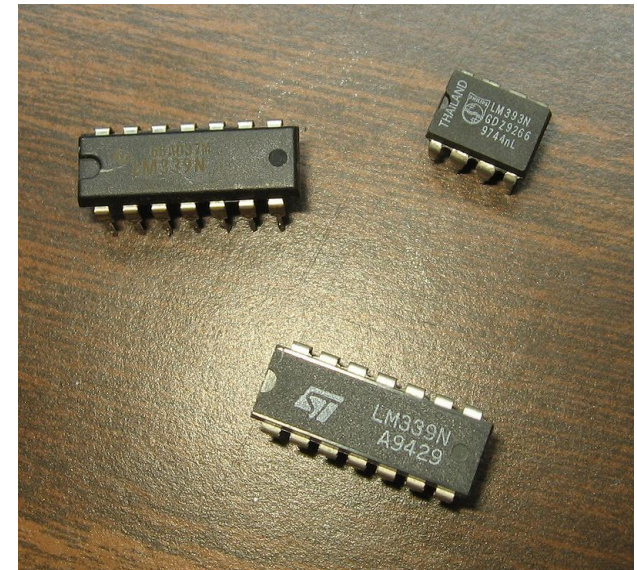
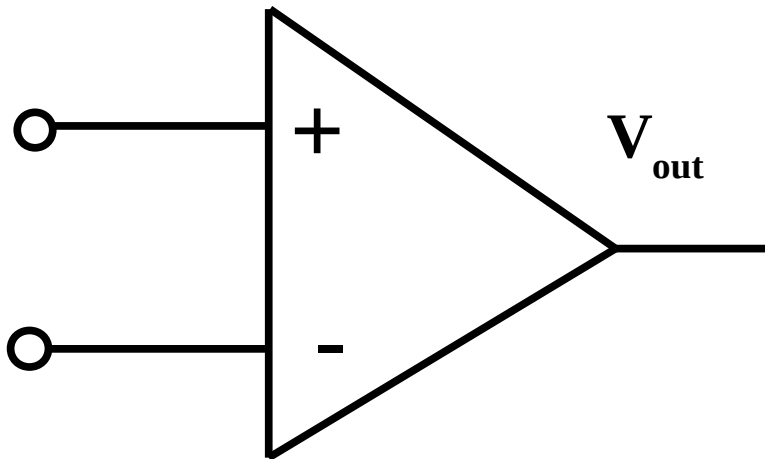
Analog to digital converter



Comparators basics



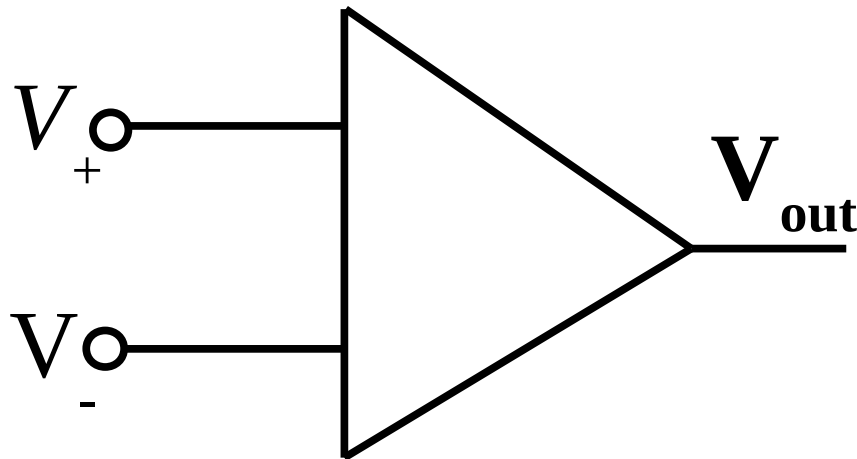
- Before we can learn about A2D converters we need to learn about comparators.



Stuuf

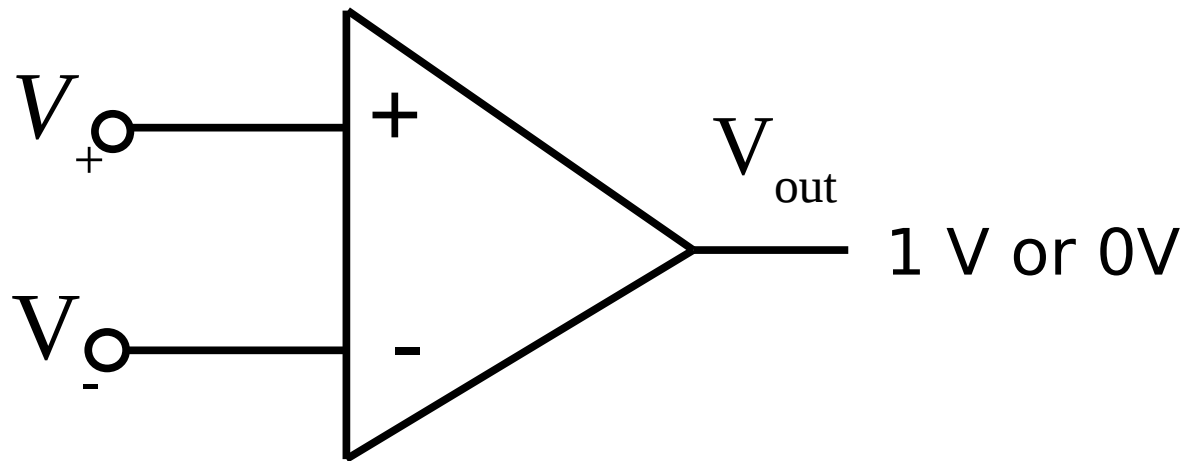
- Comparators look **just like** an **op-amp**, in fact you can use an op-amp as a low performance comparator, but you are better off getting a specially designed chip like the LM393.

- Comparators compare two voltages:



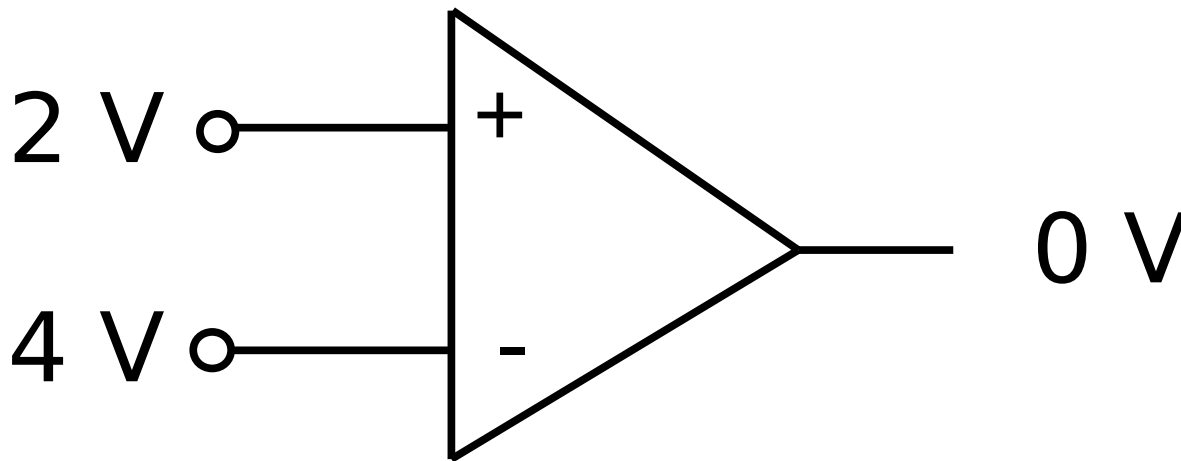
- For example...

- If V_+ is **BIGGER** than V_- it will output a **1 V**
- If V_+ is **SMALLER** than V_- it will output a **0 V**



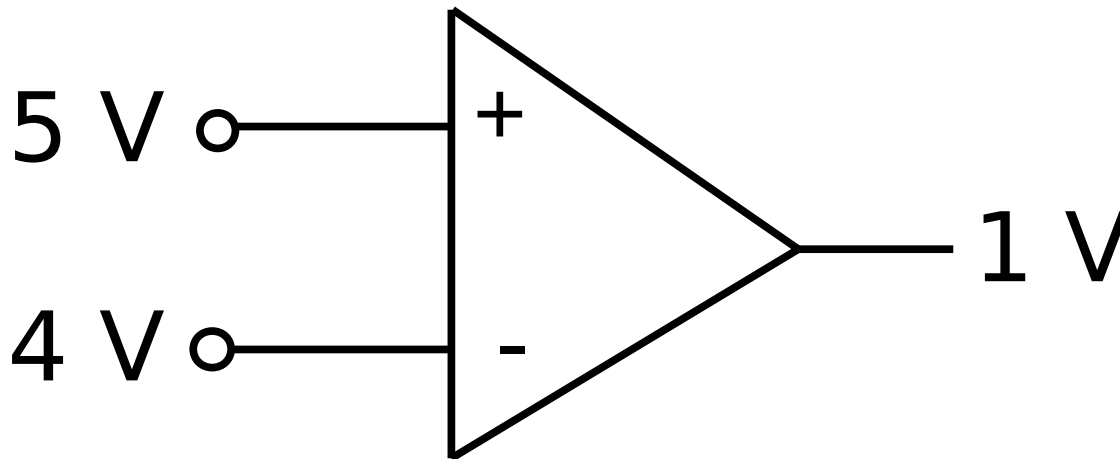
- For example...

- If $V_- = 4 \text{ V}$ and $V_+ = 2 \text{ V}$ it will output 0 V .



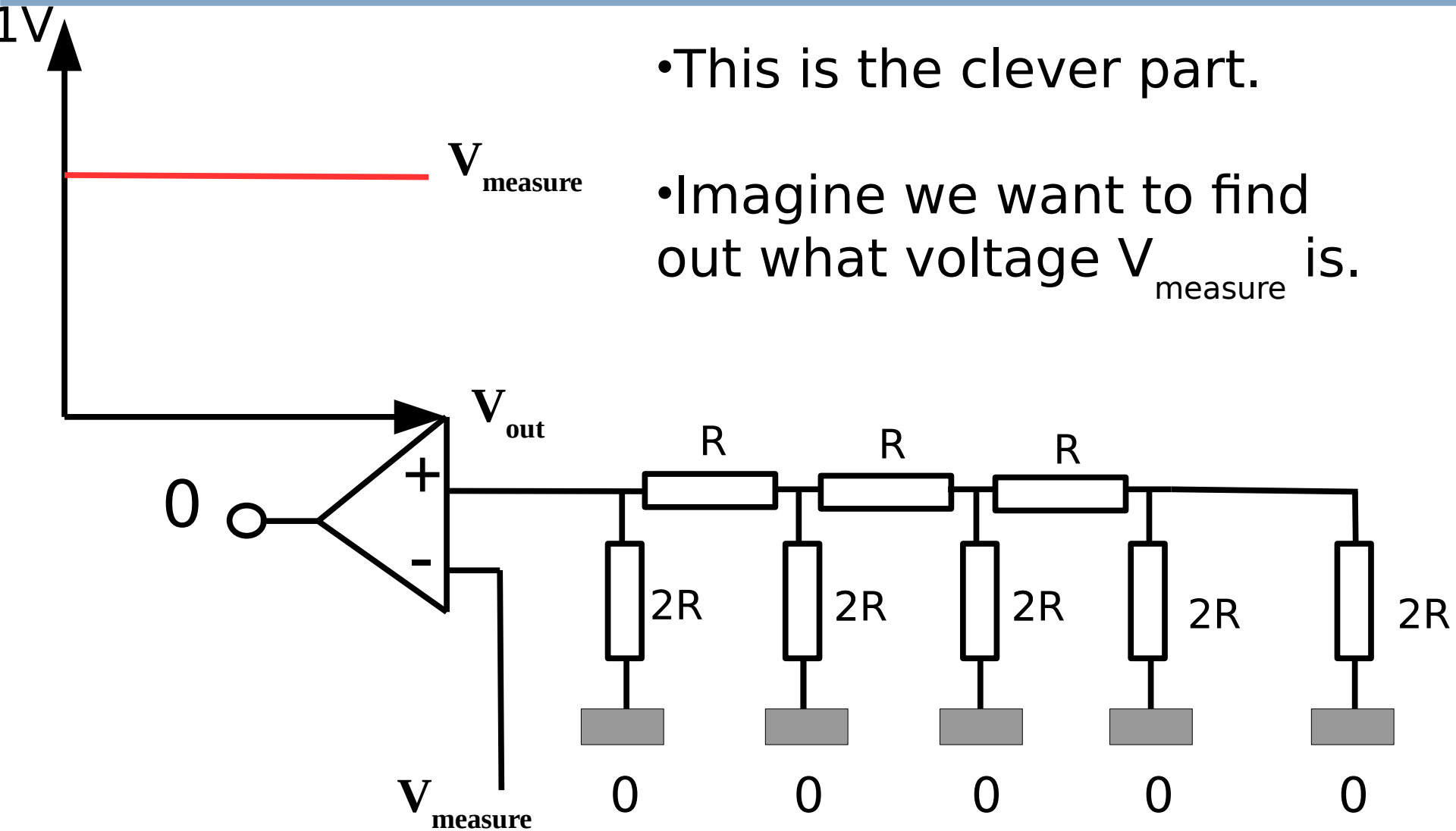
- For example...

- If $V_- = 4 \text{ V}$ and $V_+ = 5 \text{ V}$ it will output V_1 .



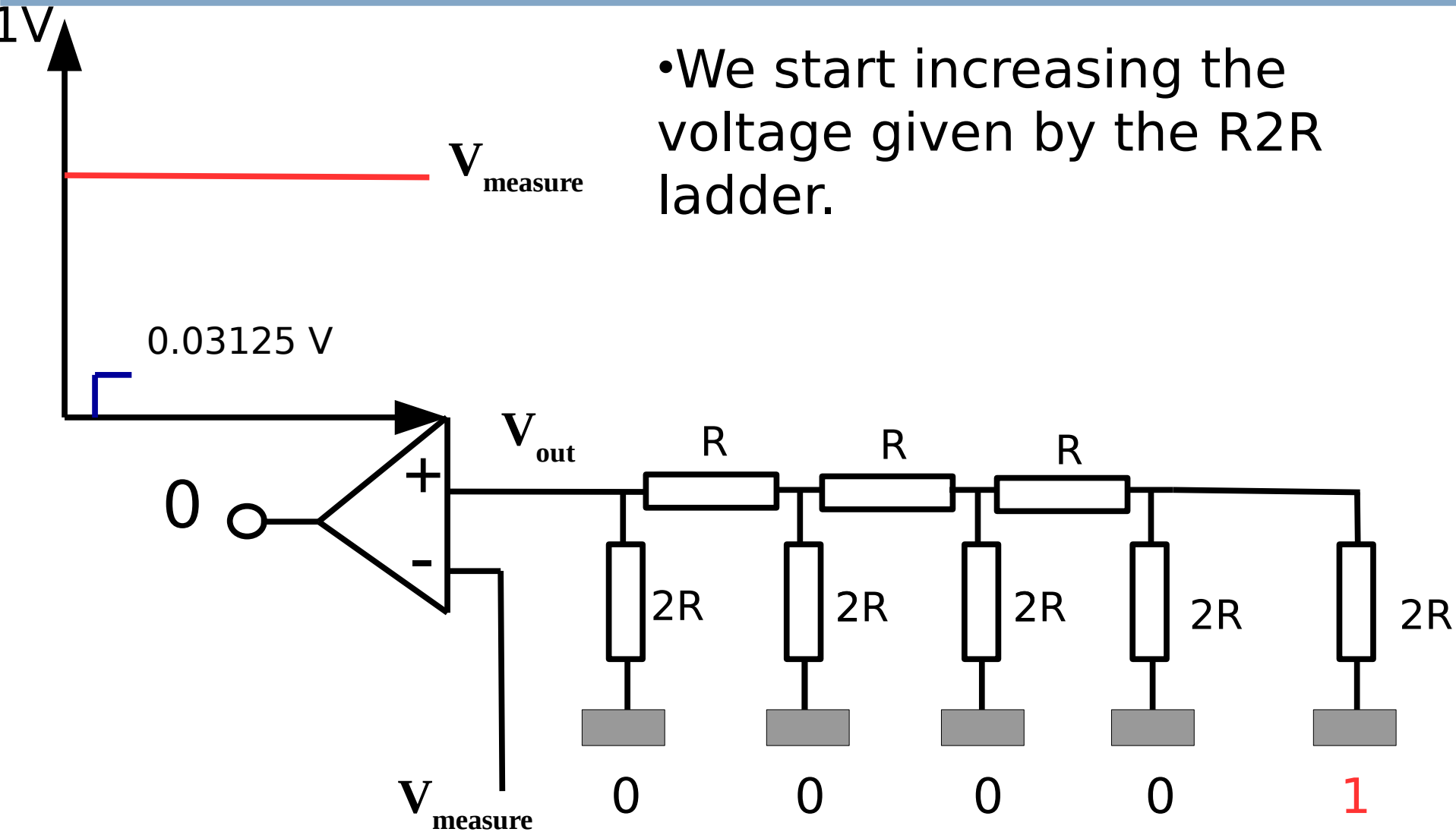
- We now know everything we need to implement an analog to digital converter.

Stick our comparator on the output of an R2R ladder



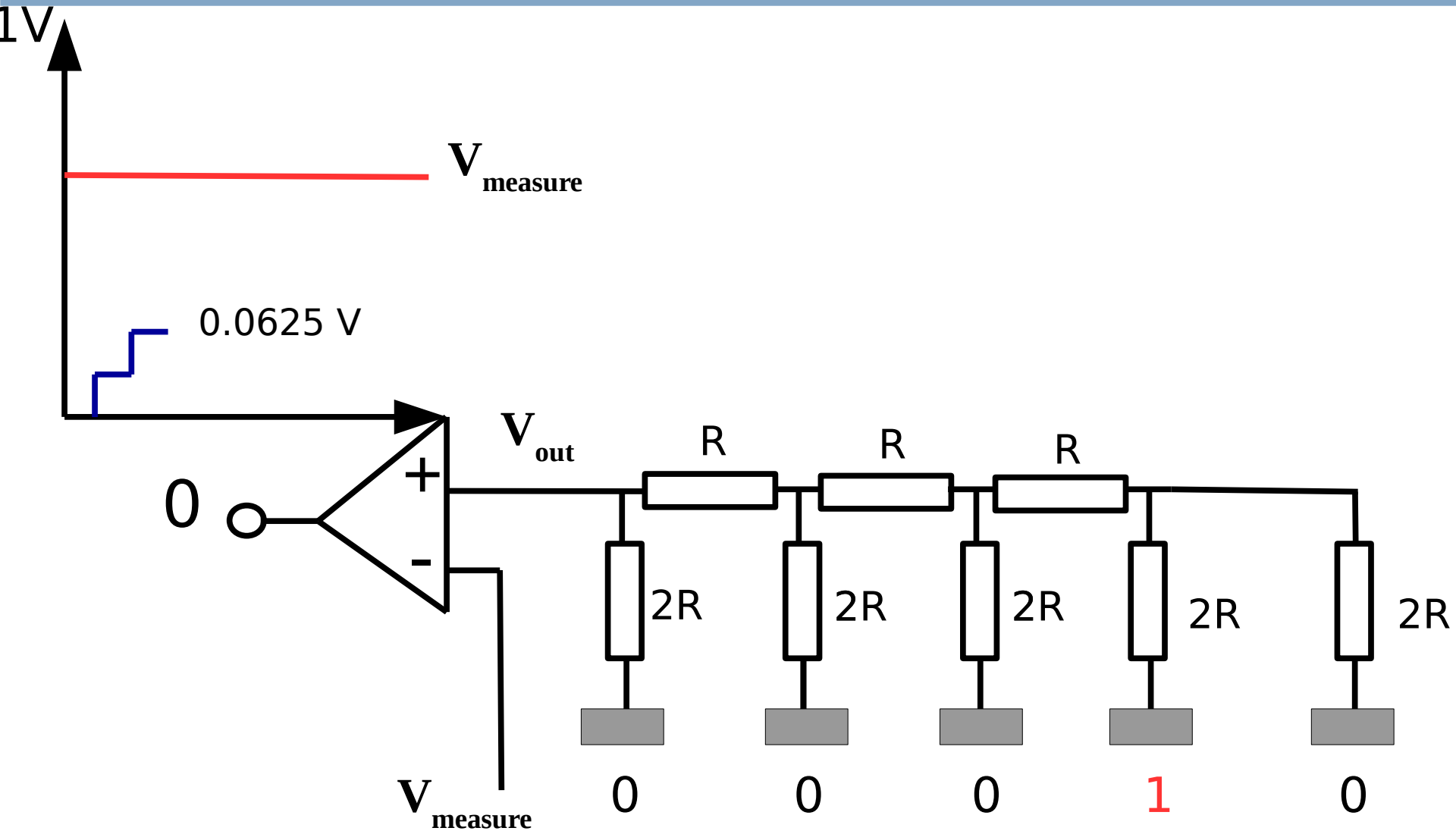
- This is the clever part.
- Imagine we want to find out what voltage V_{measure} is.

Binary 1



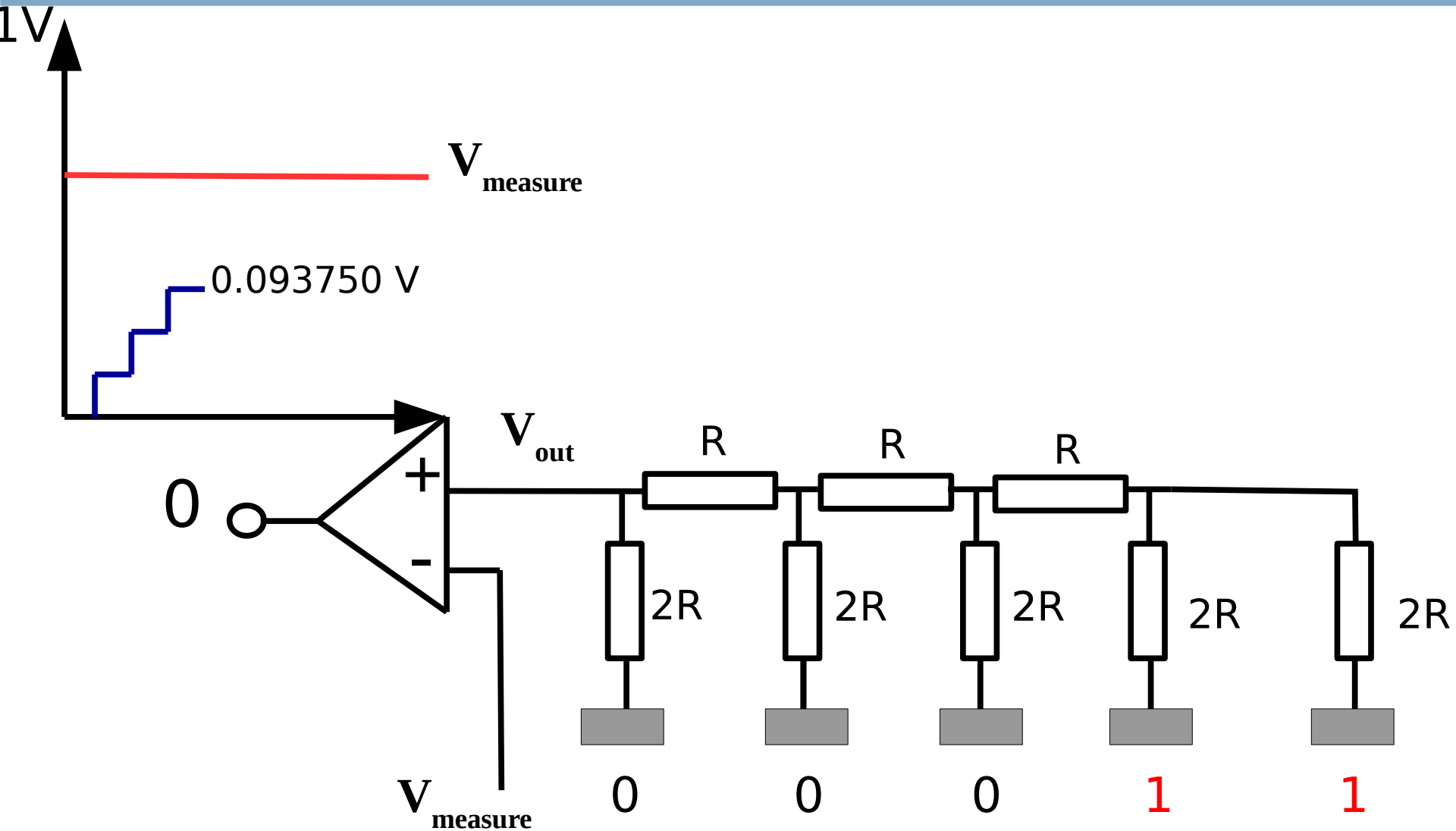


Binary 2

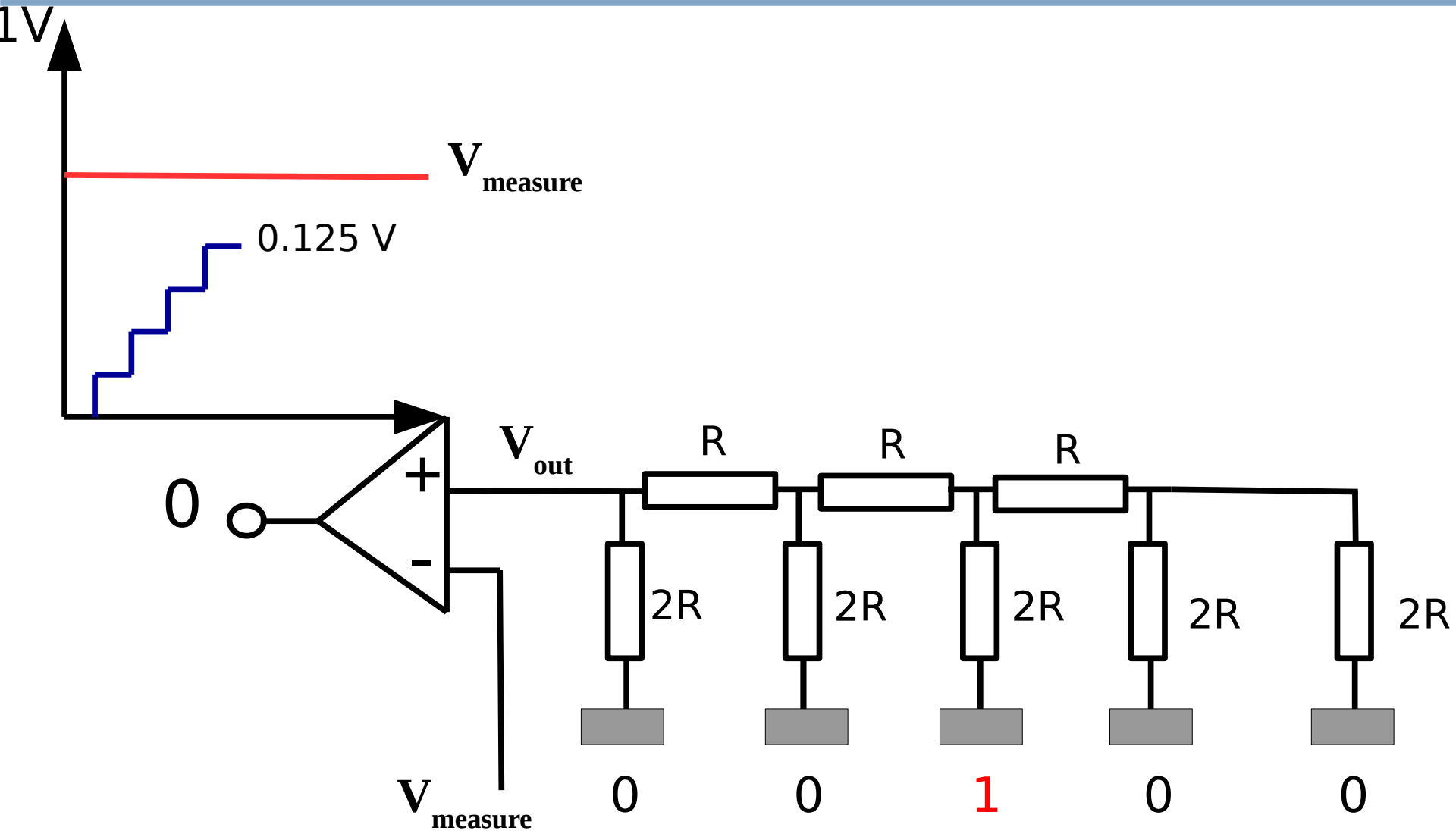




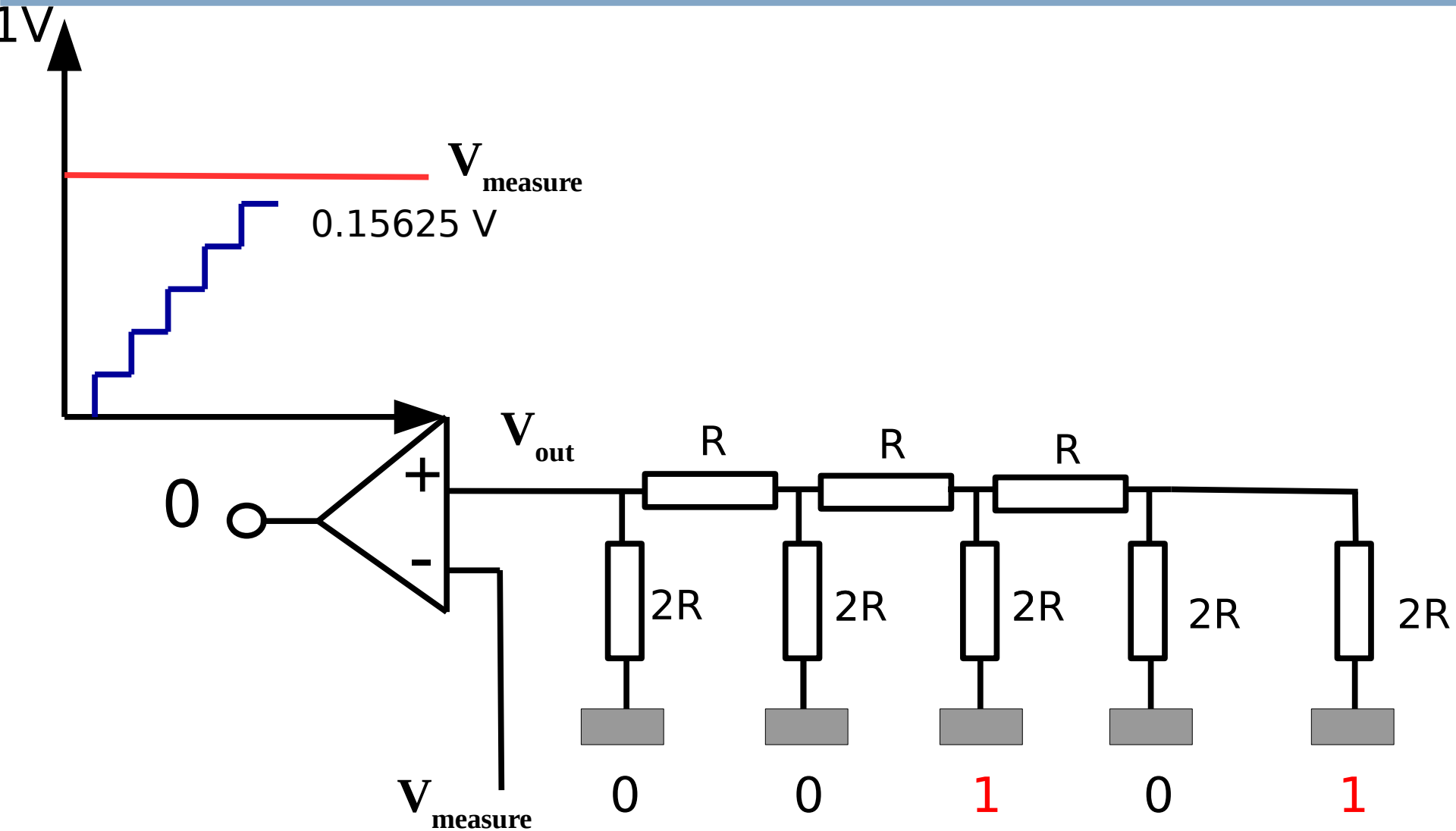
Binary 3



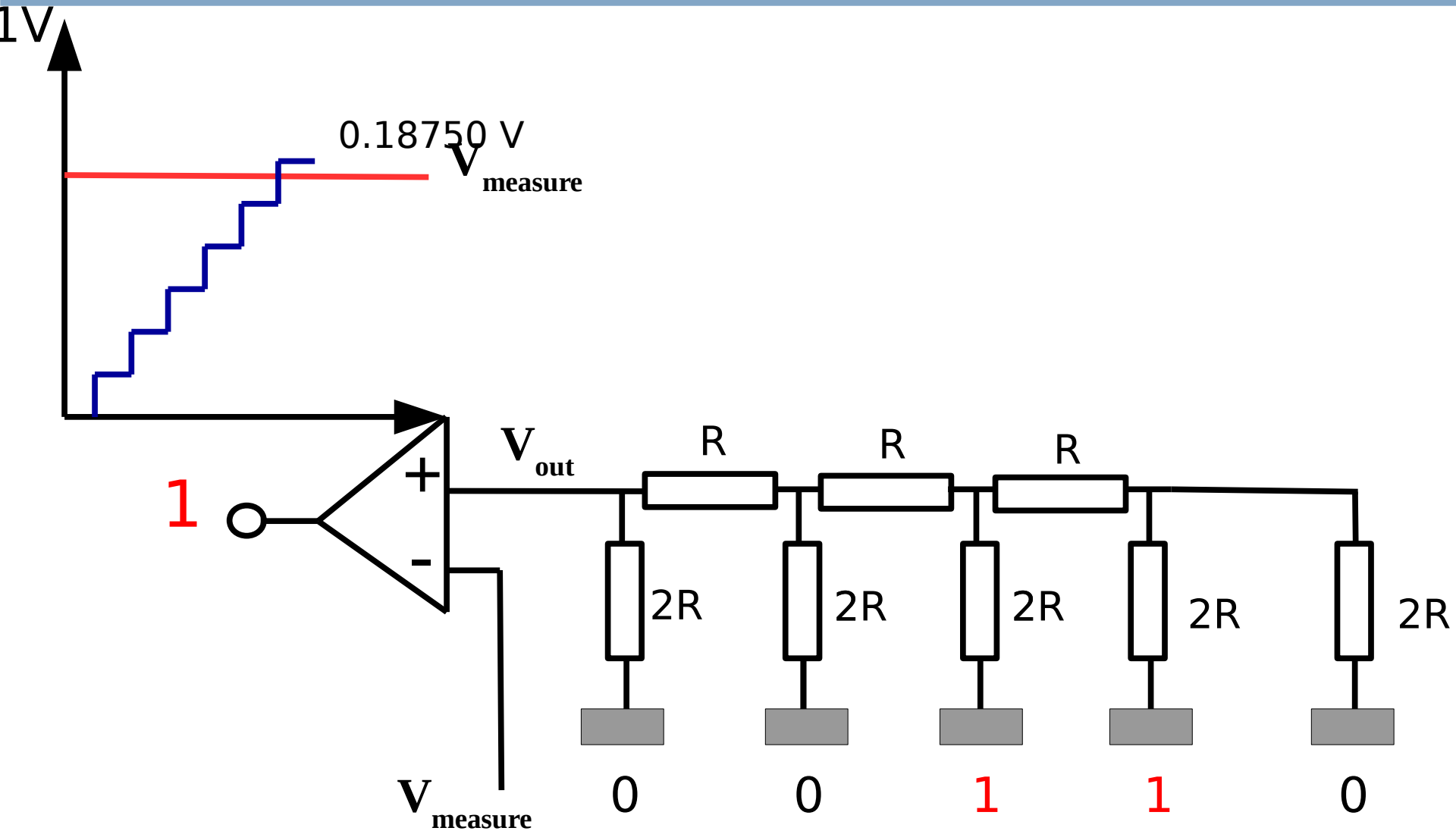
Binary 4



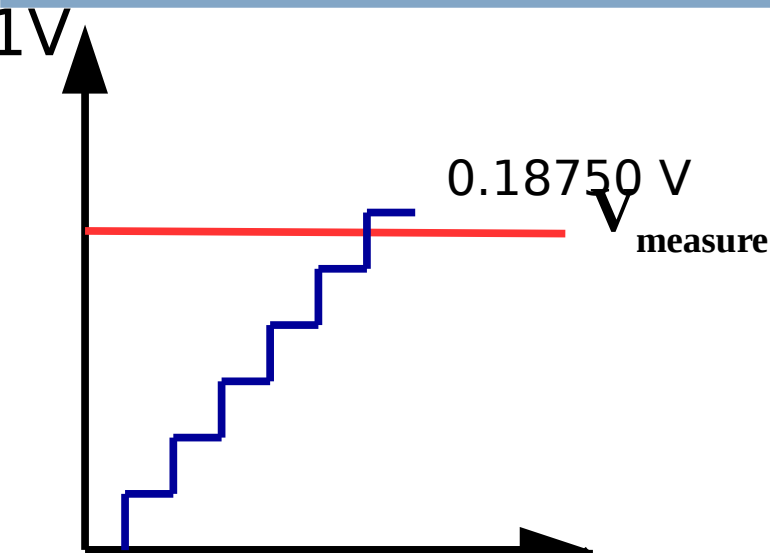
Binary 5



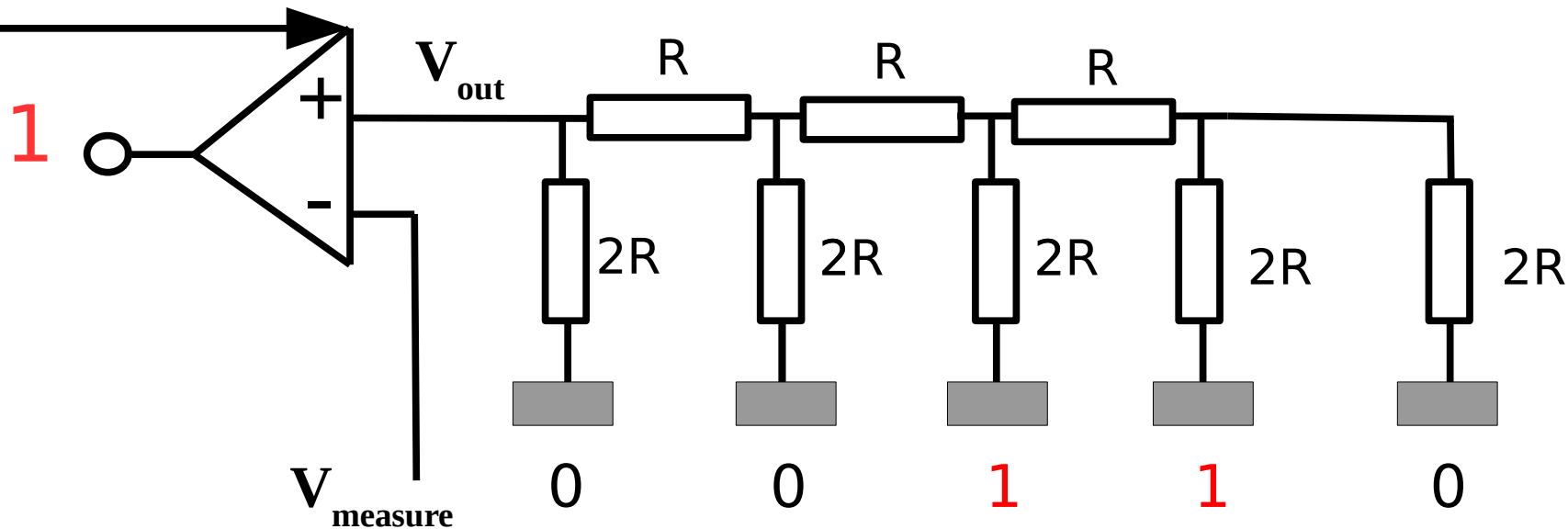
Binary 6 - and the output bit flips



Binary 6 - and the output bit flips



- The output from the compactor has now flipped.
- So we know that the voltage must be close to 0.01875 V.





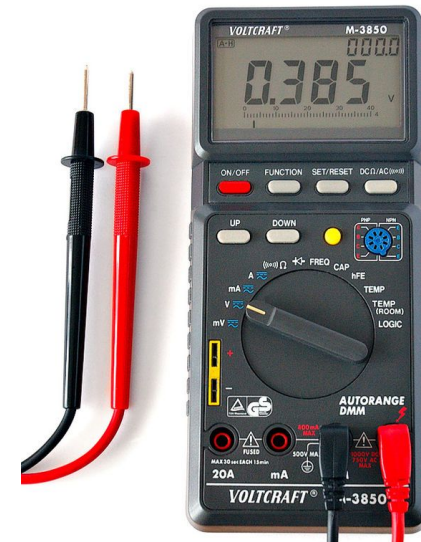
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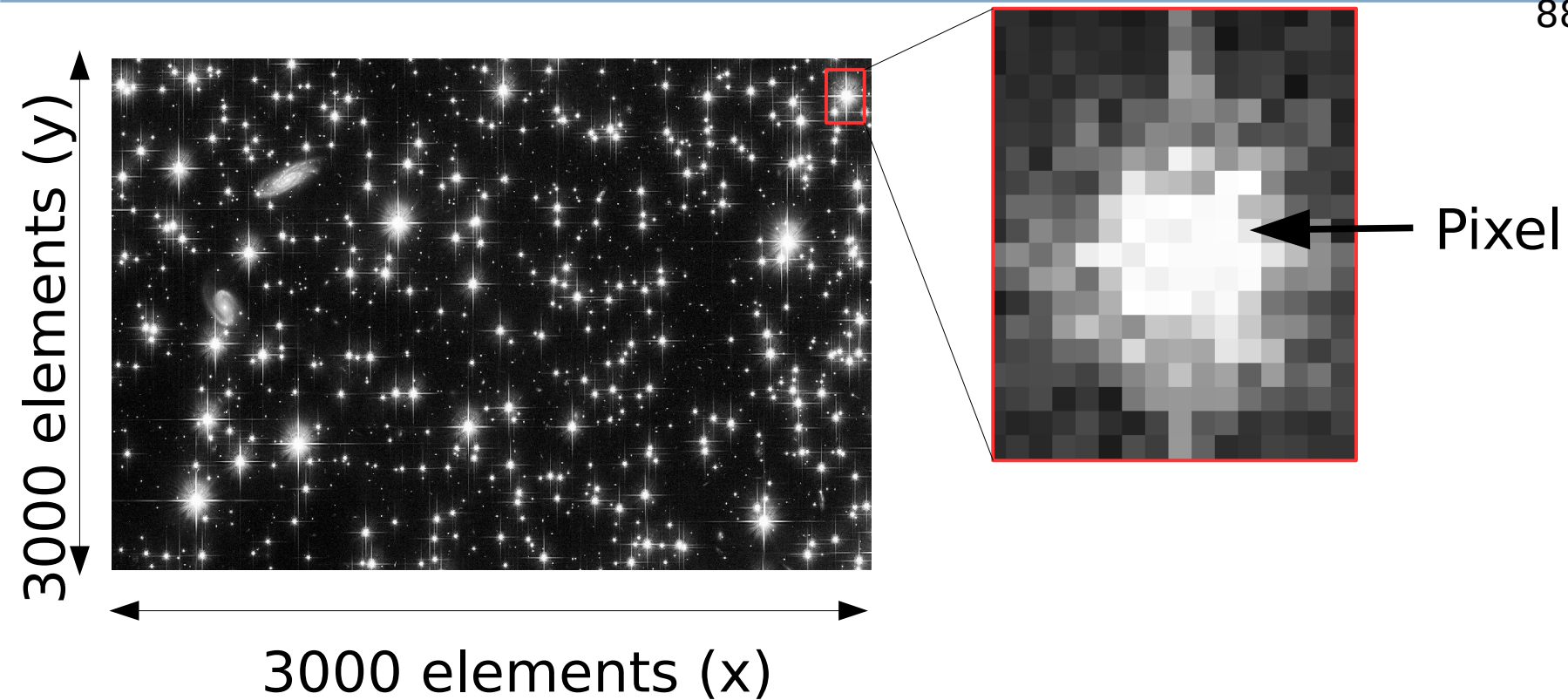
Disadvantages of R2R based converters



- The problem with the analog to digital converter based on the R2R ladder is that it takes a finite amount of time to count up.
- This means conversion is **slow**.
- However they are low cost and you do find them in lots of places – such as in volt meters.
- The **flash converter** for video and other speed applications.



André Karwath



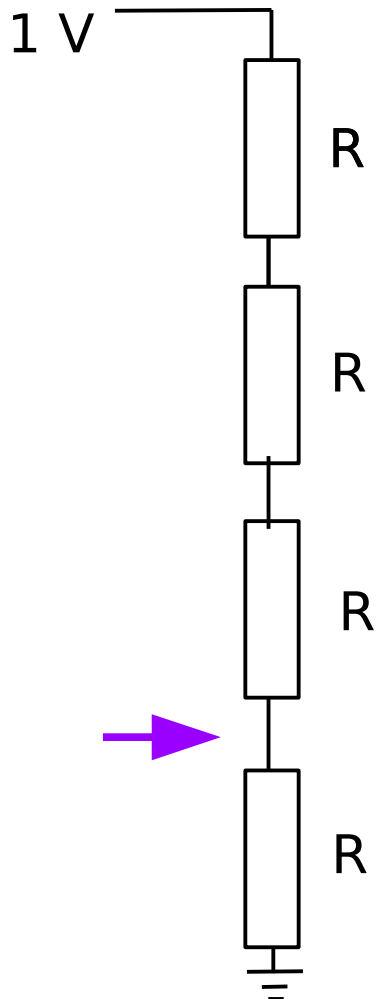
- To capture video we will need to convert all these pixels (voltages) to binary numbers instantly.

- There is no time for counting and using R2R ladders.

The Flash converter



- Think about these resistors

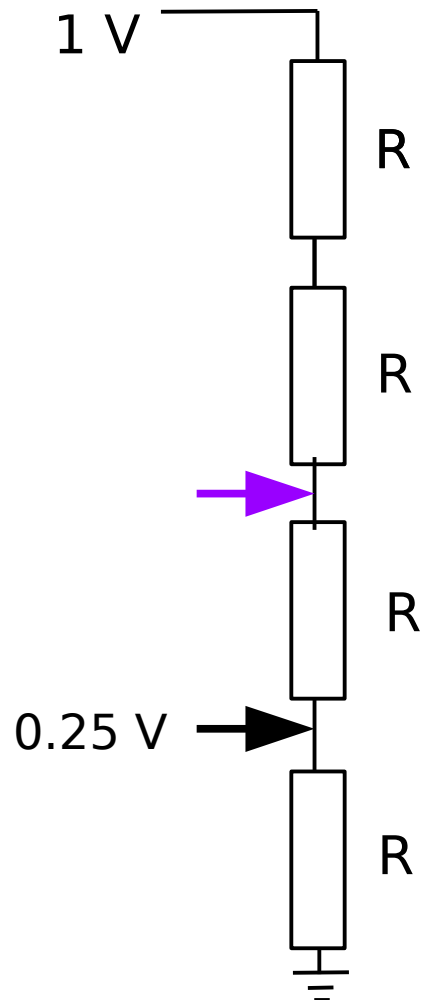


- What will the voltage here be?

The Flash converter



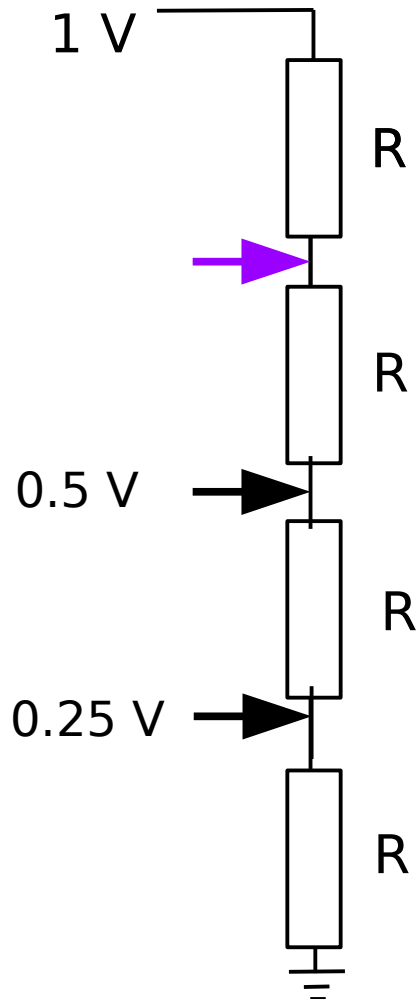
- Think about these resistors



The Flash converter



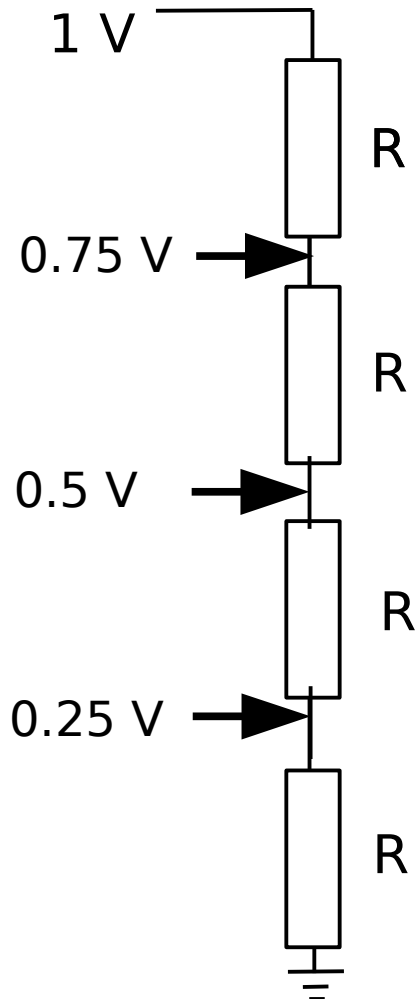
- Think about these resistors



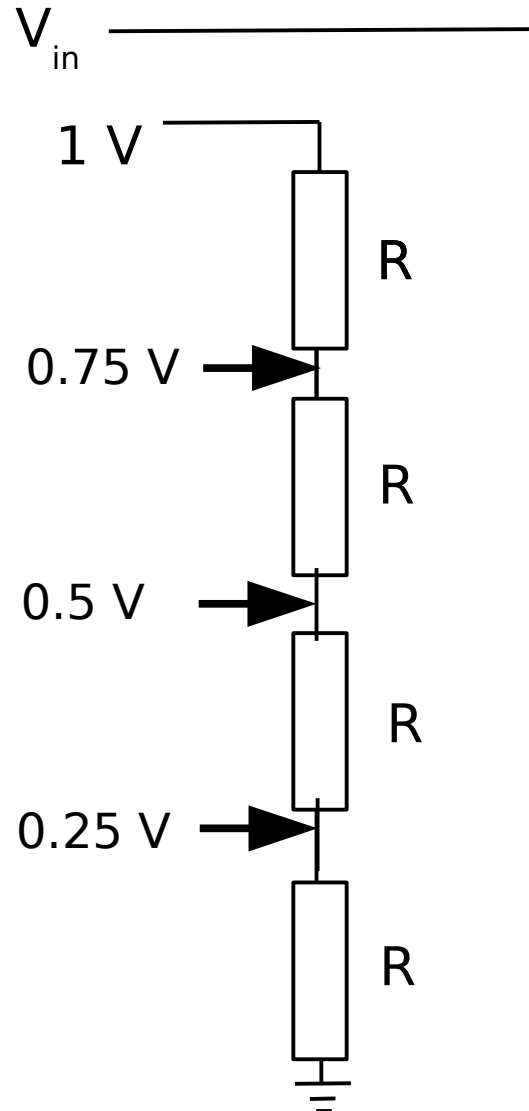
The Flash converter



- Think about these resistors

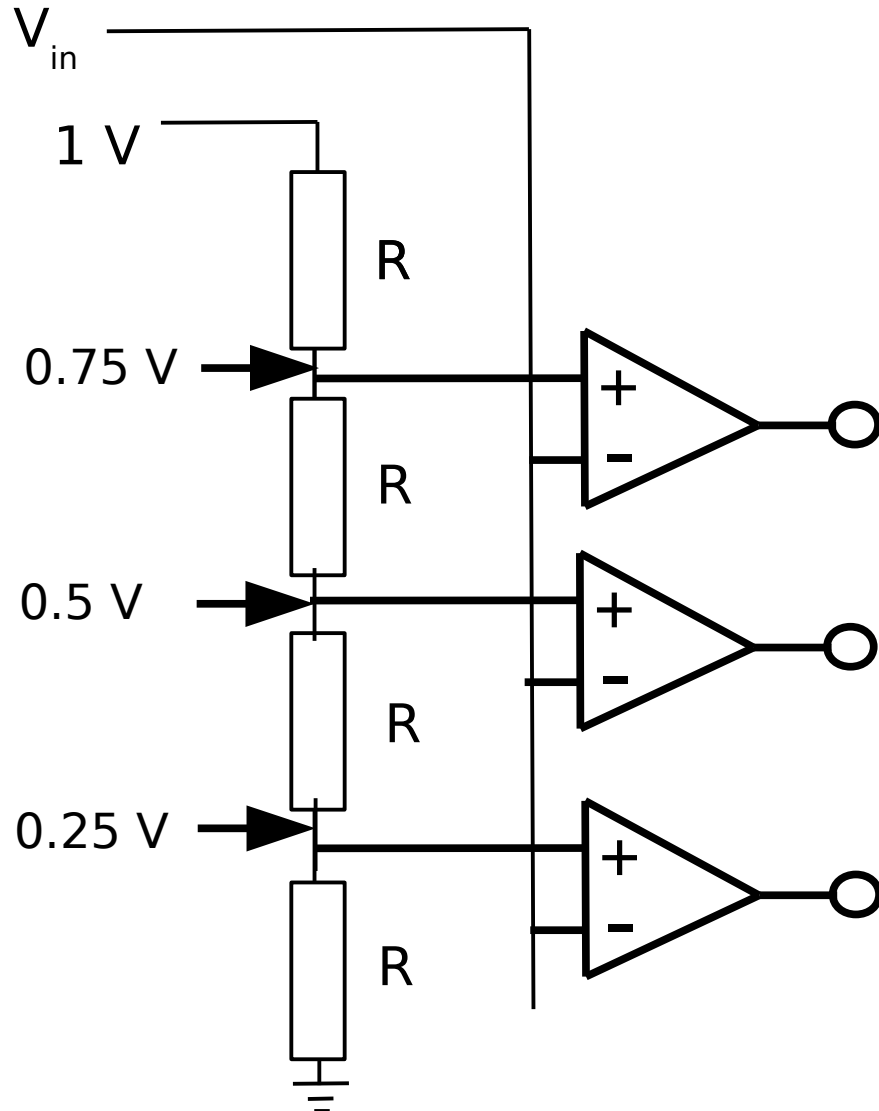


The Flash converter

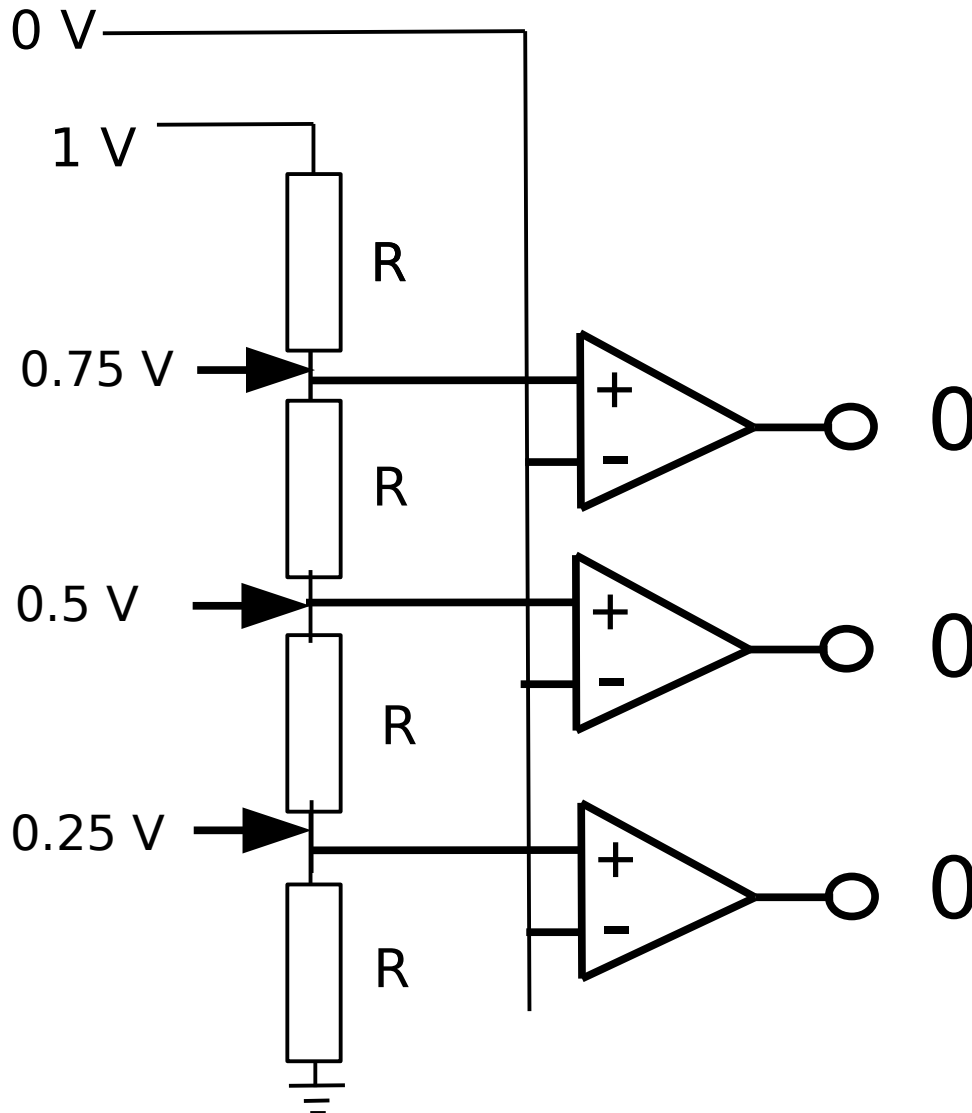


- Connect some comparitors

The Flash converter

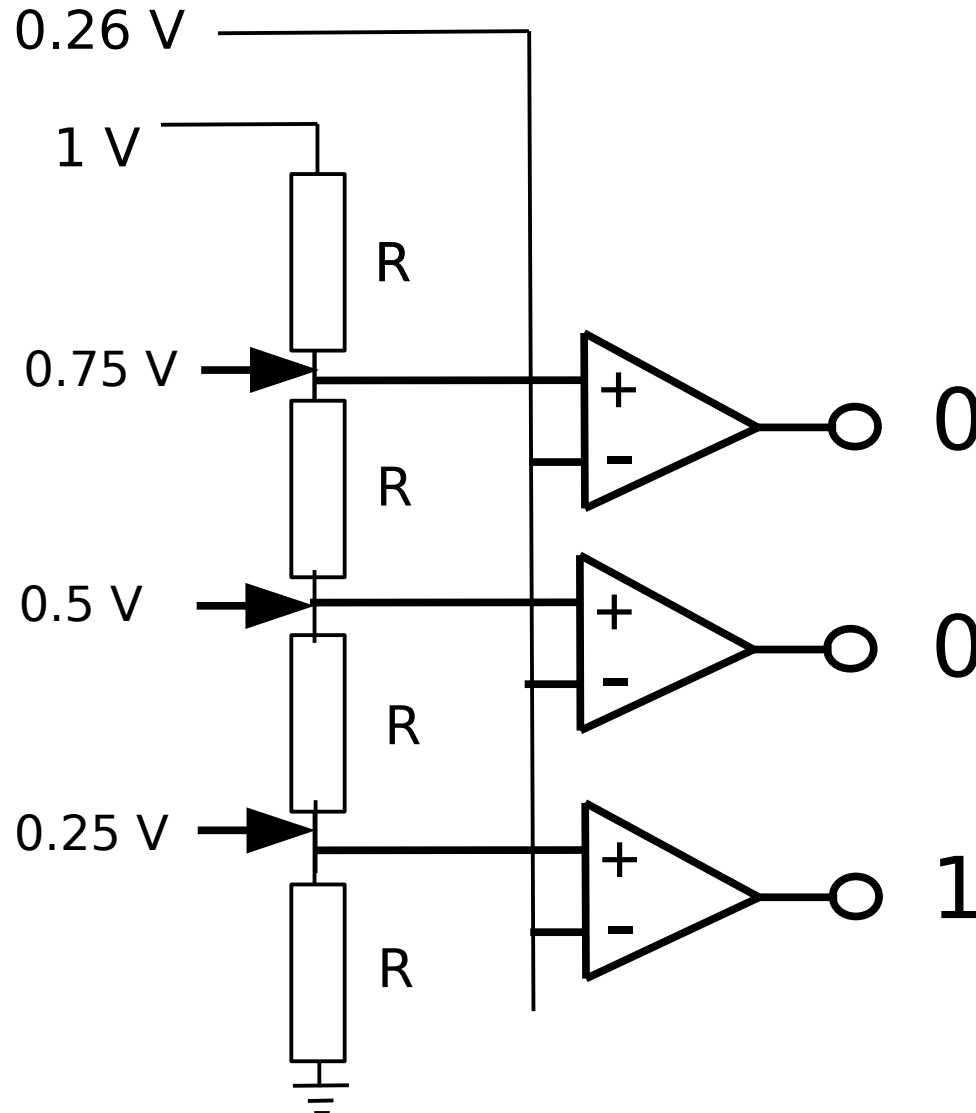


The Flash converter



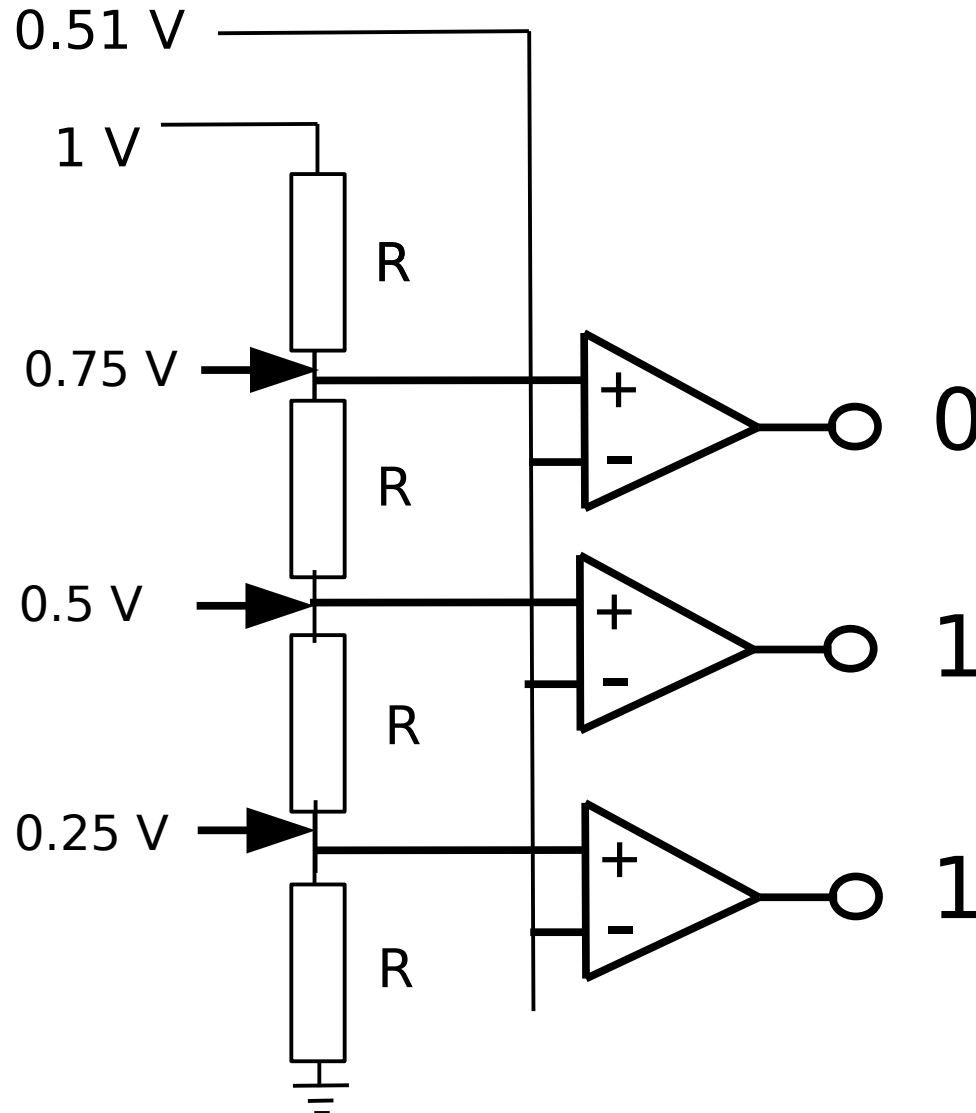
•If we have 0 V input we will get all 0's out.

The Flash converter



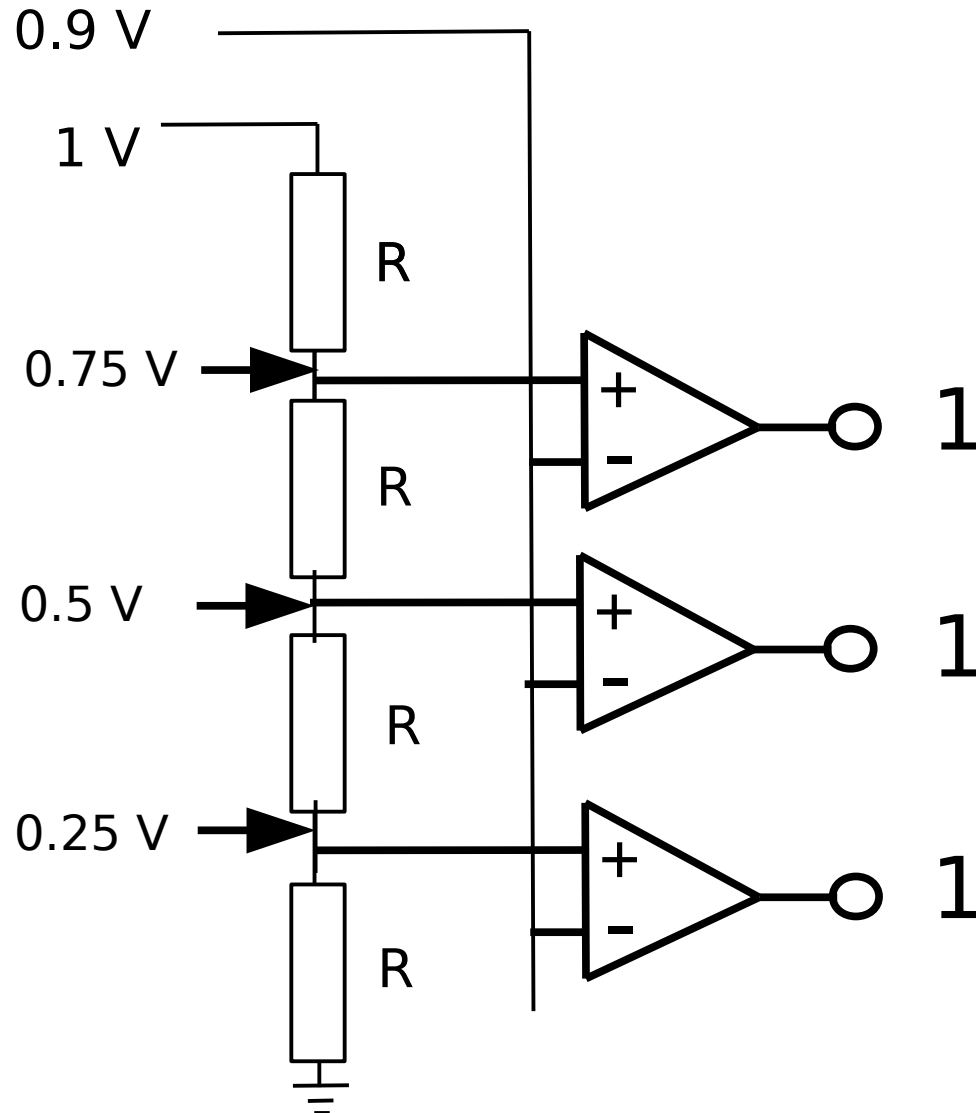
• If we have 0.26 V input we will get 001 out.

The Flash converter



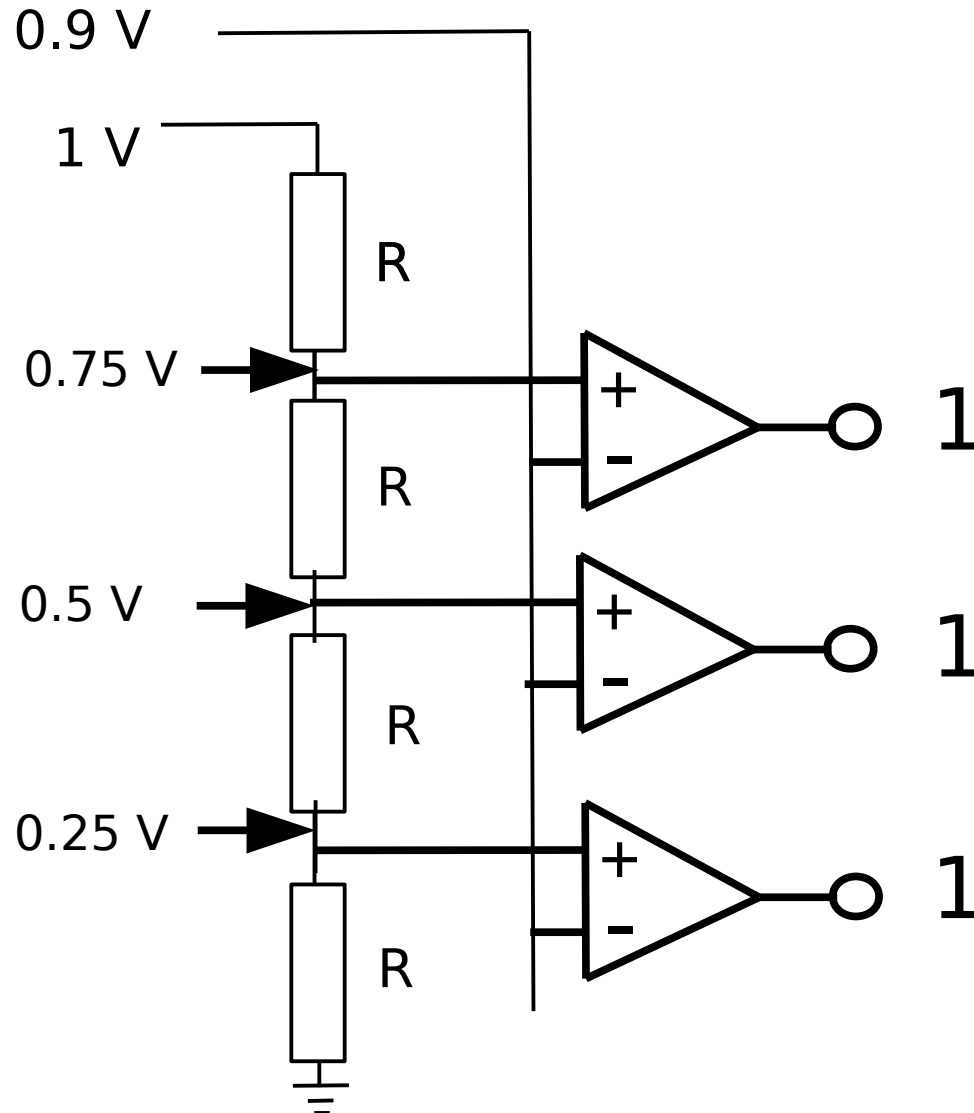
• If we have 0.51 V input we will get 011 out.

The Flash converter



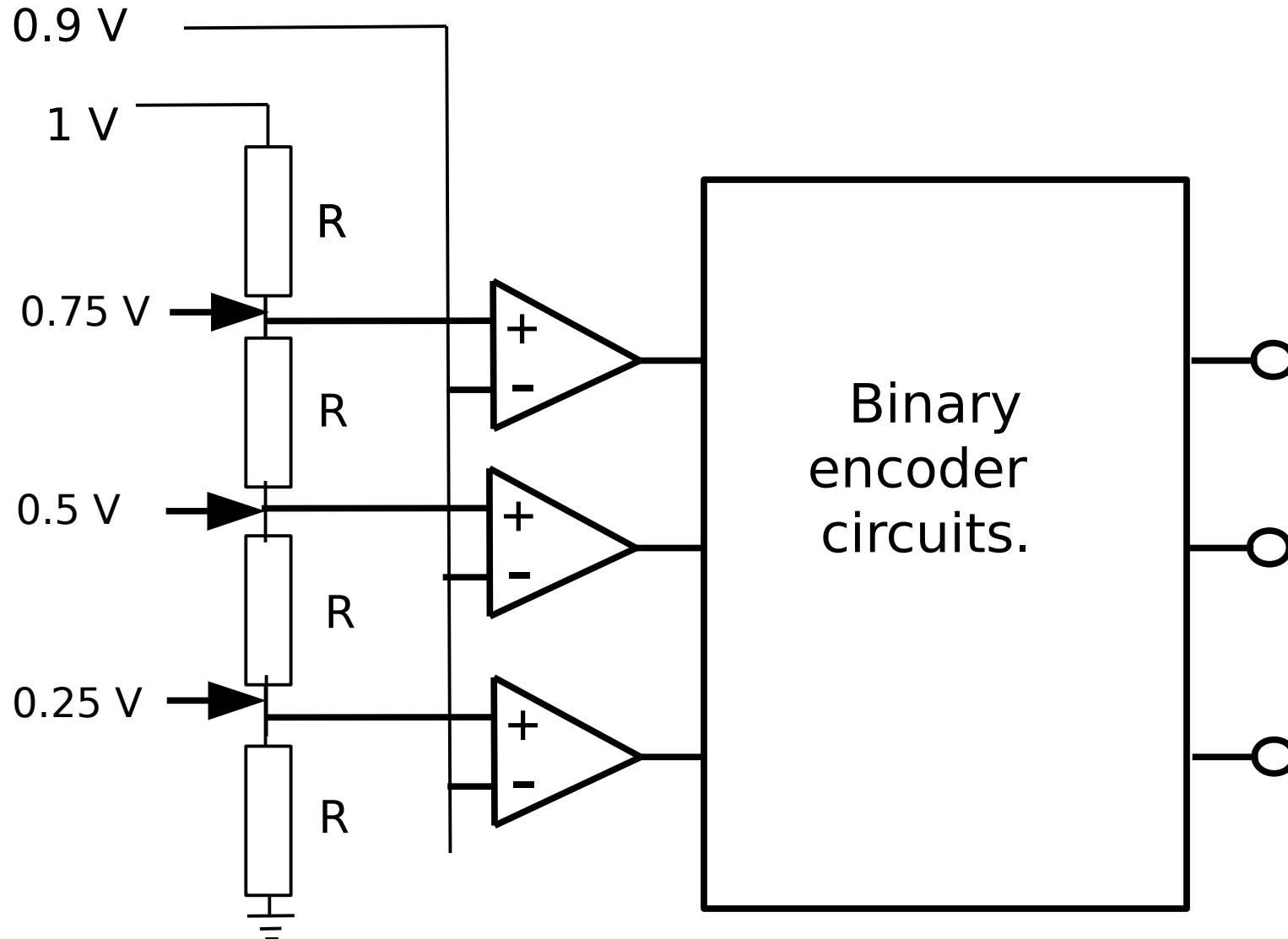
•If we have 0.9 V input we will get 111 out.

The Flash converter



- Notice the output is not binary code.
- We will therefore need a digital circuit to convert it to binary.

The Flash converter





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• **Summary**